

Genetic Algorithms

Various Operators

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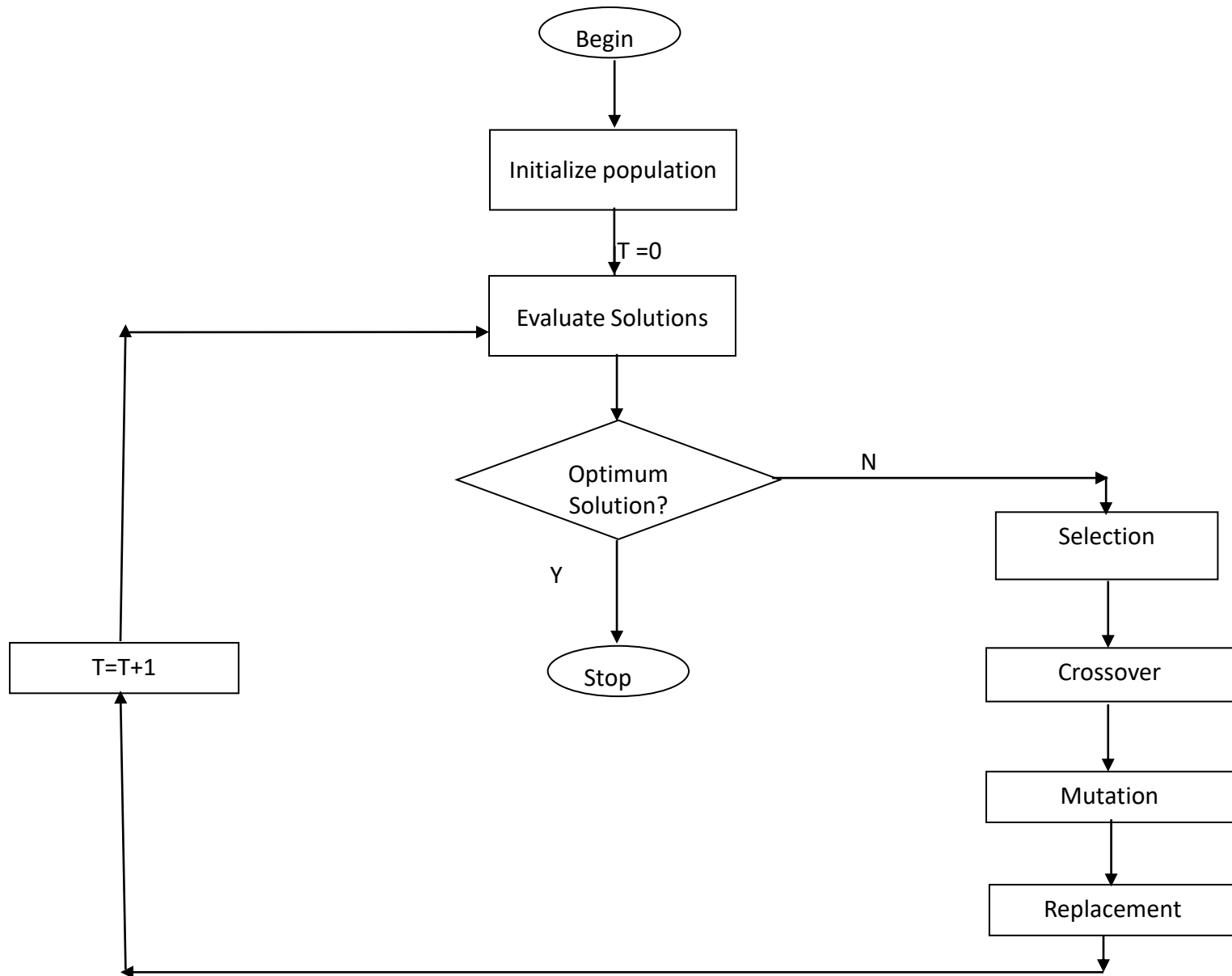
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Remember: Mechanism Of GAs



Various Strategies for the Genetic Operators

- Different GAs use different strategies.
 - Representation (encoding/decoding)
 - Crossover
 - Mutation
 - Selection
 - Replacement

Various Representations

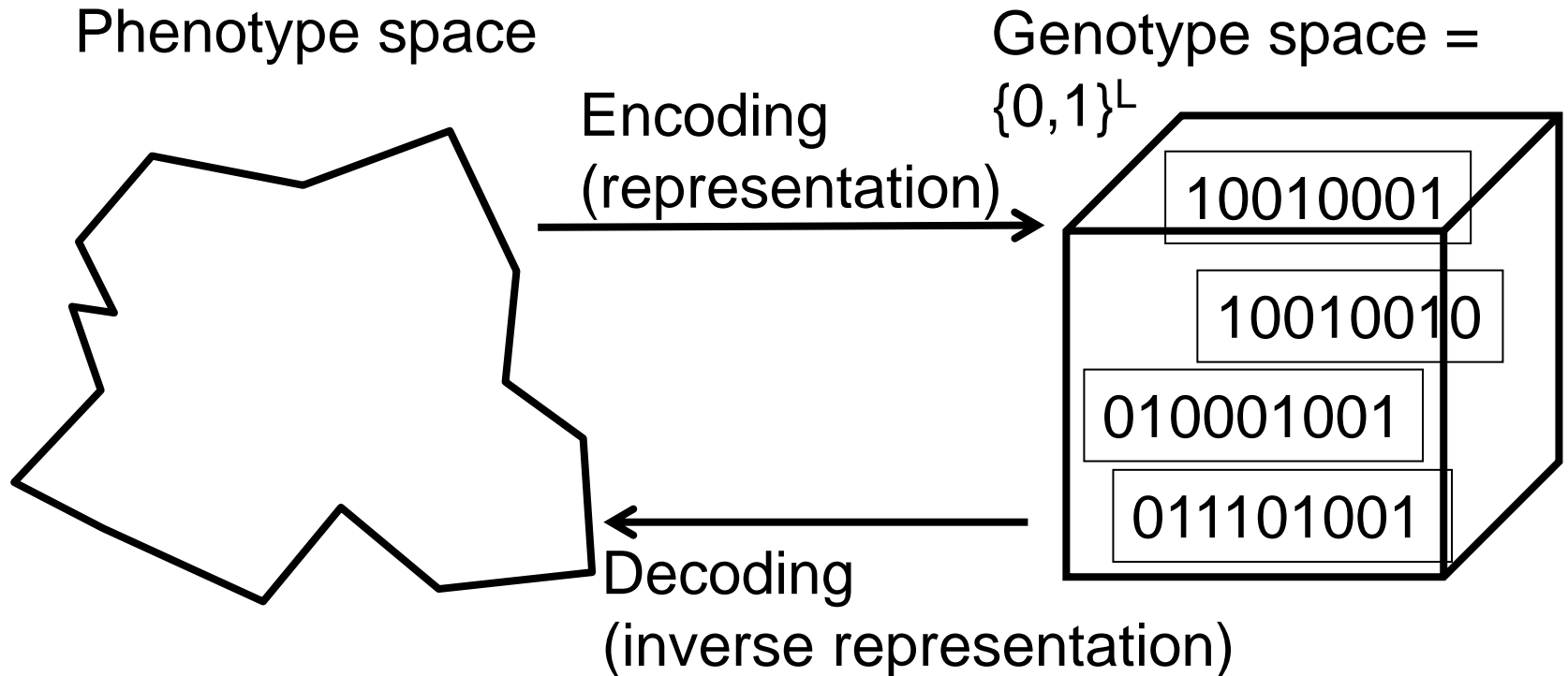
String Array?

Character Array?

Floating Point?

Permutation?

Integer?

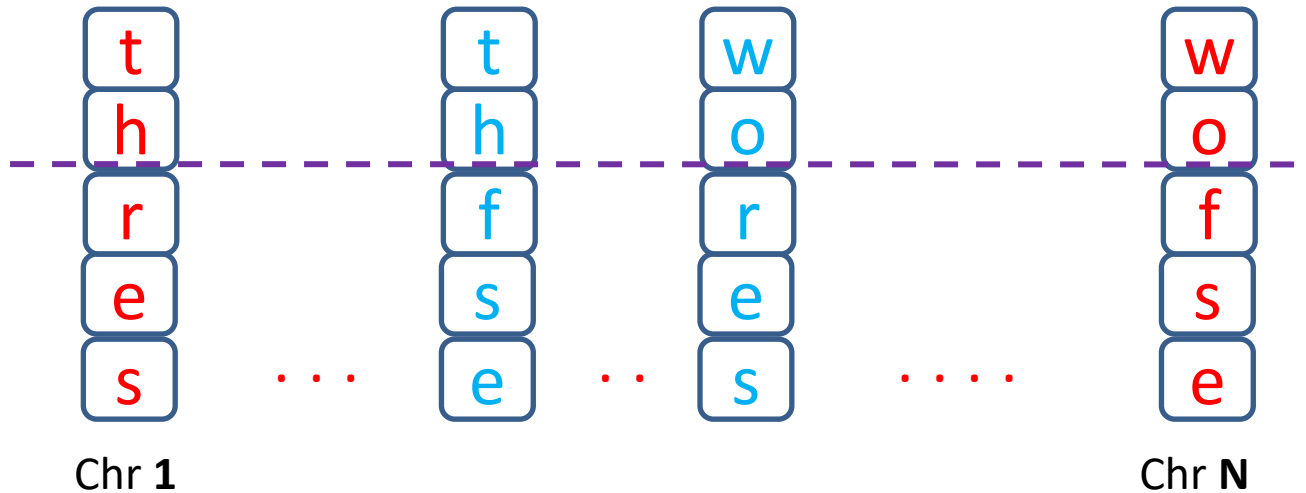


English Word Generation Example

Problem: Generate valid English word of length 5 characters

Objective fn

Crossover



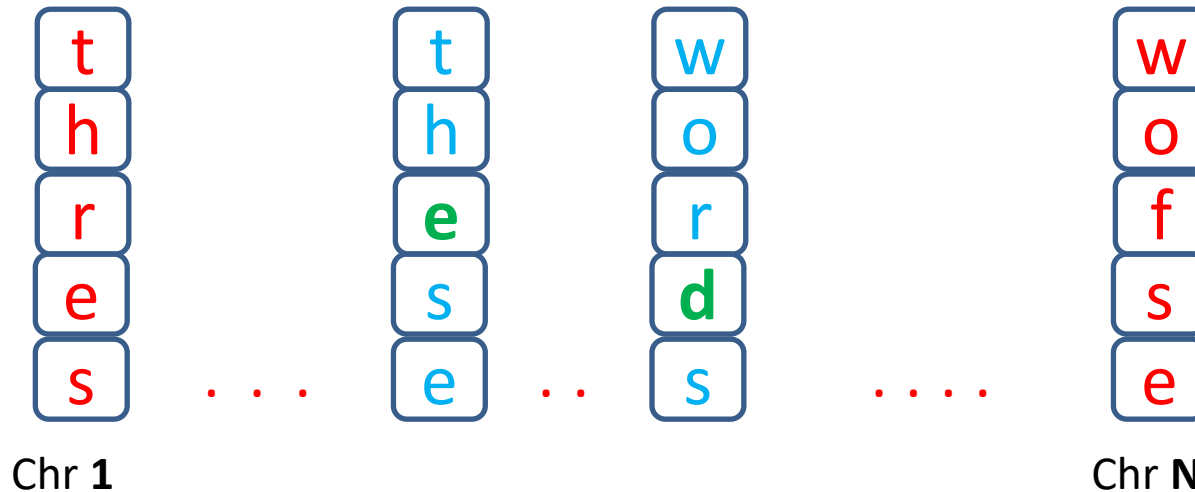
Dictionary

English Word Generation Example

Problem: Generate valid English word of length 5 characters

Objective fn

Mutation



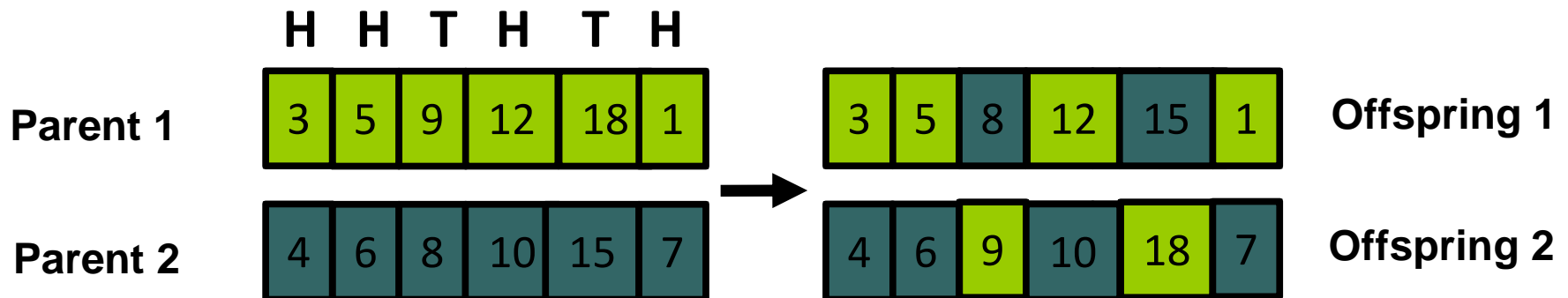
Integer Representation

- Some problems naturally have integer variables, e.g. image processing parameters
- Others take *categorical* values from a fixed set e.g. {blue, green, yellow, pink}
- N-point / uniform crossover operators work
- Extend bit-flipping mutation to make
 - **Random choice** (categorical variables)

Uniform Crossover for Integers

- Assign 'heads' to one parent, 'tails' to the other
 - Flip a coin for each gene of the first child
 - Make an inverse copy of the gene for the second child
-
- Example:

Suppose H for Parent1 and T for Parent 2



Uniform Crossover for Integers

- Inheritance is independent of position
- Applicable for binary representation
- How to implement it (programming)
- N-point crossover ???

Subset: **BAABBAABBB** **(Randomly generated)**

Parents: **1010001110** **0011010010**

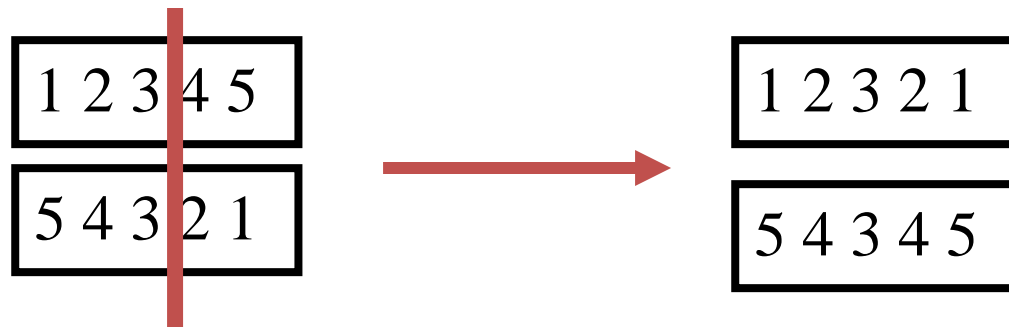
Offspring: **0011001010** **1010010110**

Permutation Representations

- Ordering/sequencing problems form a special type
- Task is (or can be solved by) arranging some objects in a certain order
 - Example: sort algorithm: important thing is which elements occur before others (order)
 - Example: Travelling Salesman Problem (TSP) : important thing is which elements occur next to each other (adjacency)
- These problems are generally expressed as a permutation:
 - if there are n variables then the representation is as a list of n integers, each of which occurs exactly once

Crossover for Permutations

- Normal crossover operators will often lead to inadmissible solutions



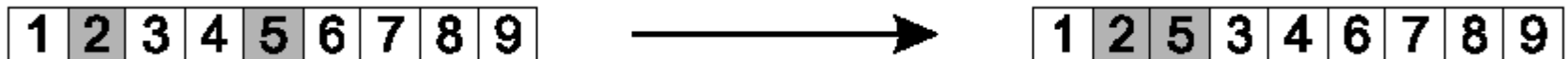
- Many specialised operators have been devised which focus on combining order or adjacency information from the two parents

Mutation operators for permutations

- Normal mutation operators lead to inadmissible solutions
 - e.g. bit-wise mutation : let gene i have value j
 - changing to some other value k would mean that k occurred twice and j no longer occurred
- Therefore must **change at least two values**
- Mutation parameter now reflects the probability that some operator is applied **once to the whole string**, rather than individually in each position

Insert Mutation for permutations

- Pick two allele (gene) values at **random**
- Move the second to follow the first, shifting the rest along to accommodate
- Note that this preserves most of the order and the adjacency information



Swap mutation for permutations

- Pick two alleles (genes) at **random** and swap their positions
- Preserves most of adjacency information (4 links broken)
- disrupts order more



Inversion mutation for permutations

- Pick two alleles at **random** and then invert the substring between them.
- Preserves most adjacency information (only breaks two links) but disruptive of order information



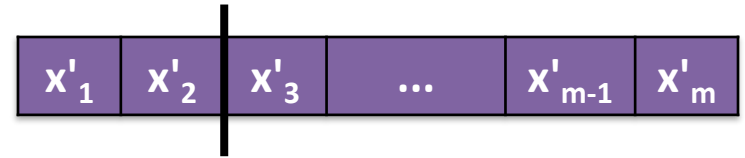
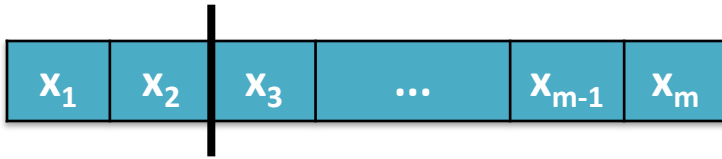
Floating-point (real values) Representation

- Many problems occur as real valued problems, e.g. continuous parameter optimization $f: \mathcal{R}^n \rightarrow \mathcal{R}$
- The chromosome will be an array of floating point variables

0.5	0.2	0.6	0.8	0.7	0.4	0.3	0.2	0.1	0.9
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- This can serve in optimization of a multi-variate function $y = f(x_1, x_2, \dots, x_m)$
- Crossover is the same as in bit-string chromosomes.
- Mutation is different

Crossover over FP Chromosomes



Mutation over FP Chromosomes

- General scheme of floating point mutations

$$\bar{x} = \langle x_1, \dots, x_l \rangle \rightarrow \bar{x}' = \langle x'_1, \dots, x'_l \rangle$$
$$x_i, x'_i \in [LB_i, UB_i]$$

- Two kinds of FP mutations:
 - Uniform
 - Non-uniform

Uniform FP Mutation

x'_i drawn randomly (uniform) from $[LB_i, UB_i]$



Given the above chromosome \mathbf{x} in a particular generation \mathbf{G} :

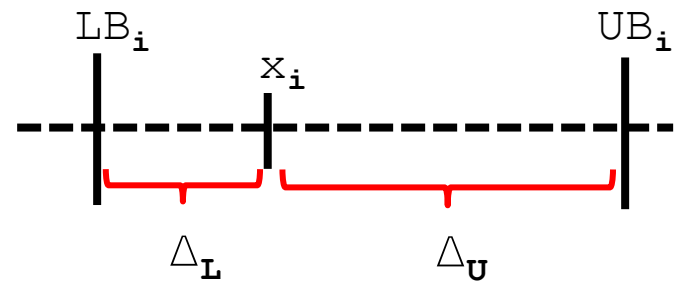
- Each gene (variable) has a range
- Gene x_i is a FP value inside chromosome \mathbf{x} at generation \mathbf{G}
- To mutate gene x_i

1. Generate random number $r_{i1} \in [0, 1]$

- $\Delta = \Delta_L$ if $r_{i1} \leq 0.5$
- $\Delta = \Delta_U$ if $r_{i1} > 0.5$
- This means equal chance to go left or right

2. Generate random number $r_{i2} \in [0, \Delta]$

- if $\Delta = \Delta_L$ then $x_{i\text{-new}} = x_i - r_{i2}$
- if $\Delta = \Delta_U$ then $x_{i\text{-new}} = x_i + r_{i2}$



$$\Delta_L = x_i - LB_i$$

$$\Delta_U = UB_i - x_i$$

Non-uniform FP Mutation

Some methods proposed such as **time-varying** range of change



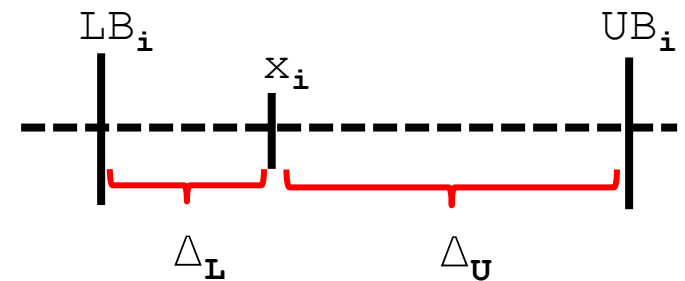
Given the above chromosome \mathbf{x} in a particular generation G :

- Each gene (variable) has a range
- Gene x_i is a FP value inside chromosome \mathbf{x} at generation G
- To mutate gene x_i

1. Generate random number $r_{i1} \in [0, 1]$
 - $y = \Delta_L$ if $r_{i1} \leq 0.5$
 - $y = \Delta_U$ if $r_{i1} > 0.5$
2. Let $\Delta(t, y)$
 - = value of mutation at generation t
 - = $y(1 - r^{(1-t/T)^b})$

where:

- r = random number $\in [0, 1]$
- t = current generation
- T = maximum number of generations
- b = dependency factor $\approx 1 \dots 5$



$$\Delta_L = x_i - LB_i$$

$$\Delta_U = UB_i - x_i$$

Non-uniform FP Mutation

- Analysis of Equation:

$$\Delta(t, y) = \text{value of mutation at generation } t$$
$$= y(1 - r^{(1-t/T)^b})$$

where:

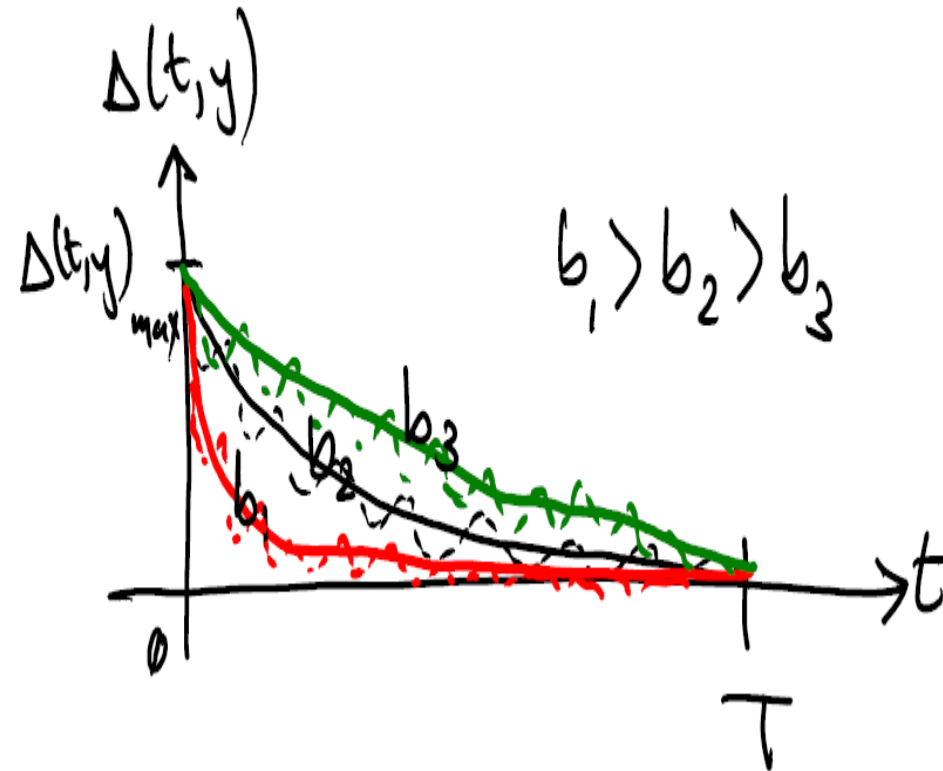
- r = random number $\in [0, 1]$
- t = current generation
- T = maximum number of generations
- b = dependency factor $\approx 1 \dots 5$
(Controls the curve of mutation)

- At $t=0$:

$$\Delta(t, y) = \text{Maximum value of mutation}$$

- At $t=T$:

$$\Delta(t, y) = 0 \quad (\text{No mutation})$$



Crossover or Mutation?

- Decades of long debate: **which one is better or necessary?**
- Answer (at least, rather wide agreement):
 - it depends on the problem, but
 - in general, it is good to have both
 - both have different roles
 - mutation-only-GA is **possible**, crossover-only-GA **would not** work. Why??

Mutation

- Causes movement in the search space (local or global)
- Restores lost information to the population
- Mutation is necessary because some important genes might be missing from all the initial population.

Crossover

- It greatly accelerates search early in evolution of a population
- It leads to effective combination of schemata (subsolutions on different chromosomes)

Crossover or Mutation?

- ✓ **Exploration:** Discovering promising areas in the search space, i.e. *gaining information* on the problem
- ✓ **Exploitation:** Optimising within a promising area, i.e. *using information*

There is co-operation AND competition between them

- **Crossover is explorative:** it makes a *big* jump to an area somewhere “in between” two (parent) areas
- **Mutation is exploitative:** it creates random *small* diversions, thereby staying near (in the area of) the parent

Crossover OR mutation?

- Only crossover can **combine information** from two parents
- Only mutation can introduce **new information** (alleles)
- Crossover does not change the allele frequencies of the population (thought experiment: 50% 0's on first bit in the population, ?% after performing n crossovers)
- To hit the **optimum** you often need a 'lucky' mutation