

$$1) \text{ GF}(11)$$

$$\begin{aligned} a) & (9x^5 + 4x^4 + 8x^3 + 2x^2 + 3x + 4) \\ & + (6x^5 + 2x^4 + 9x^3 + 7x^2 + 5x + 7) \\ & = 4x^5 + 6x^4 + 6x^3 + 9x^2 + 8x \end{aligned}$$

$$\begin{aligned} b) & (8x^3 + 6x^2 + 8x + 1) \times (3x^3 + 9x^2 + 7x + 5) \\ & = 24x^6 + 90x^5 + 134x^4 + 157x^3 + 95x^2 + 47x + 5 \\ & = 2x^6 + 2x^5 + 2x^4 + 3x^3 + 7x^2 + 3x + 5 \end{aligned}$$

$$c) \frac{3x^3 - 5x^2 + 10x - 3}{3x+1} = x^2 + 9x + 4 + \frac{4}{3x+1}$$

$$\begin{array}{r} 3x+1 \overline{) \begin{array}{r} x^2 - 2x + 4 \\ 3x^3 - 5x^2 + 10x - 3 \\ \underline{3x^3 + x} \\ -6x^2 + 10x - 3 \\ \underline{-6x^2 - 2x} \\ 12x - 3 \\ \underline{12x + 4} \\ -7 \end{array}} \end{array}$$

$$2) \text{ GF}(2^3) \quad \text{Modulus: } x^3 + x + 1$$

$$\begin{aligned} a) & (x^2 + x + 1) \times (x^2 + x) \\ &= (x^4 + x^3 + x^2 + x^2 + x) \div (x^3 + x + 1) \\ &= (x^4 + x) \div (x^3 + x + 1) \\ &= x \end{aligned}$$

$$b) (x^2) - (x^2 + x + 1) = x + 1$$

$$c) \frac{x^2 + x + 1}{x^2 + 1} = 1 + x + 1 = x$$