Module IN3031 / INM378 Digital Signal Processing and Audio Programming

Tillman Weyde

t.e.weyde@city.ac.uk







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Acoustics Basics

- · Frequency unit Hertz means 1/s
- Wavelength (I or λ), frequency (f), period (p), speed (c) of sound (~340m/s)
 - Example: f = 680 Hz, $p = 1 / 680 \text{Hz} \sim 0.0015 \text{ s}$, I = c/f = 340 (m/s) / 680 Hz = .5 ms/s = .5 m
 - What is the frequency of a sound with period 10ms
- Energy increases as square of Amplitude (e.g. 5-fold amplitude means 25-fold energy)
- Harmonic sounds have components with frequencies that are integer multiples of f₀, the lowest frequency.

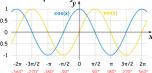


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Time and Frequency Domains

- · Audio signals vary over time: Time Domain
- The spectrum decomposes the signal into frequency components: Frequency Domain (sin and cos)
- The Fourier Transformation (and its inverse) transform between Time and Frequency Domain:







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Hearing

- Amplitude Loudness; Frequency Pitch;
 Spectrum Timbre
- Decibels: a is x dB greater than b, means x = 10 log₁₀ (a/b)
- Threshold of hearing (roughly): 0 dB SPL = 10-12 Watt/m² and the threshold of pain 130 dB SPL
- In the inner ear, the Cochlea with Basilar membrane transforms sound waves into neural signals



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Spectrum and Time

- The spectrum as calculated by the (fast) FT is as long as the signal we are analysing
 - longer signal → higher frequency resolution
- Speeding up the signal means stretching the spectrum (and inverse for k<1)

$$x(kt) \leadsto \frac{1}{|k|} X(\frac{f}{k})$$



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Digitizing Audio

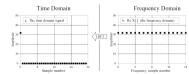
- Sampling: regularly measuring air pressure (or voltage, or any other quantity)
- Sample rate: how many measurements (per sec)
- Sample depth: resolution (# of bits) per sample value
- Storage space for audio recordings: channels * time * sample rate * sample depth



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Special Spectra

- Spectrum of a unit impulse at time 0 consists of all real 1s (cos), with 0 imaginary part. Real/imaginary ratio varies according to impulse's position in time.
- The spectrum of a constant signal with amplitude 1 is N (=length of the signal) at frequency 0, and 0 elsewhere.



This image shows only the lower half, the upper half is the mirror image of the lower.

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Correlation

Correlation is a measure of similarity

$$corr(s1,s2) = \sum_{t=0}^{N2-1} s1[t]s2[t]$$

Correlation Coefficient o

$$\rho = \frac{corr(x, y)}{\sqrt{\sum x[n]^2 \cdot \sum y[n]^2}}$$

Positive correlation coefficient of two signals means correlated signals (good mono compatibility of stereo signals), 0 means uncorrelated, negative correlation means cancellations in case of mono mixdown.



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Filtering

- Linear Filters add up samples with different coefficients depending on their 'age' to a new sample value
 - Finite Impulse Response FIR filtering applies only to input
 - Infinite Impulse Response IIR filtering also uses output samples (feedback loop)
- · FIR filtering is Convolution
 - Convolution Theorem allows calculation and design of frequency response and filter design: x*y → X·Y

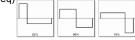


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Sound Synthesis

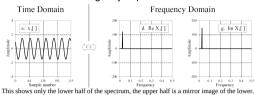
- Waveforms:
 - Sine
 - Sawtooth
 - Square
 - Pulse Width Modulation
 - Narrower pulse has more harmonics (high freq)
 - Need to compensate DC

component



Special Spectra 2

- The spectrum of a single sinusoid (sine/cosine mixture) with frequency f is 0 in all places but f (only exact if the signal length is a multiple of the frequency period).
- For a single sinusoid with (max.) amplitude 1, the spectrum at f will have magnitude I (length of signal, distribution real/imaginary depends on cosine/sine ratio)





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Cross-Correlation

Cross-correlation is a correlation at a lag

$$xcorr(s1, s2, k) = \sum_{t=0}^{N2-1} s1[t]s2[t+k]$$



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Short Term Fourier Transform

- · Window width
 - frequency vs. time resolution
- · Window function enforces periodicity
 - Hann
- Crossfading
 - necessary since signal may be not 0 at boundaries after processing
 - functions should add up to 1 in the overlapping region
 - Triangular or Hann

Sampling Theorem

- · Sampling Theorem (Nyquist Theorem):
 - When sampling with frequency fs, only frequencies less than fs/2 (Nyquist Frequency Ny) can be recorded accurately.
 - If this is not taken into account, Aliasing occurs.

Aliasing: a signal component with a frequency greater than Ny is reproduced as a lower frequency:

f_a = |((f + Ny) mod Fs)-Ny|



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Other Signal Properties

Autocorrelation: Measure of self similarity, cross-correlation of a signal with itself. $ac(x,k) = \sum_{t=0}^{N-1} x[t] \cdot x[t+k]$

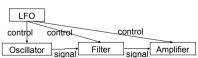
Example: If signal x contains an echo at lag *I* autocorrelation ac(x,I) will be high. If the echo is inverted (* -1), the autocorrelation with be negative.



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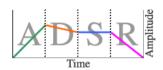
Sound Synthesis

Subtractive synthesis:



Envelop Generators

· ADSR generator.





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Image Processing Summary (1)

- What is digital image processing?
- Topics in digital image processing
- Digital image acquisition
- Digital image representation
- Elementary image processing operations
- Colour image processing
- Noise in image processing
- Basic image processing in Matlab



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Image Processing Summary (4)

- Spatial filtering
- Smoothing/sharpening filters
- 2-D convolution
- 2-D Discrete Fourier Transform (DFT)
- Frequency domain filters



Buffers and Latency in Digital Sound Systems

- · Use buffers throughout for processing speed
- · Buffers cause latency (delays between input and output)
 - Larger buffers
 - + less CPU usage, more stability
 - higher latency
 - Smaller buffers
 - more CPU, less stability
 - + lower latency



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Image Processing Summary (2)

- Digital image processing concerns the transformation of an image to a digital format and its processing by computers
- Topics: image compression, medical imaging. image restoration, remote sensing, face detection...
- Image acquisition elements: energy, optical system, sensor
- The quality of a digital image is largely determined by the number of samples and discrete intensity levels used in sampling and quantization



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Image Proc. Summary (5)

- Mask: small sub-image used for spatial filtering
- Smoothing filters are used for blurring and noise reduction
- Sharpening filters highlight fine detail or enhance detail that has been blurred.

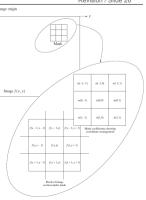


Image Processing Summary



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Image Processing Summary (3)

- An image can be represented by a 2-D array
- Resolution: spatial, gray levels
- Basic transformations: image negatives, gamma correction, addition, subtraction
- Colour models: RGB. CMY. HSI
- Noise in image processing: film grain, CCD noise...
- Matlab Image Processing Toolbox













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Image Processing Summary (6)

- 2-D convolution: moving a mask from pixel to pixel
- Most filtering takes place in the frequency domain (reason: computational efficiency)

2	2	2	
2	2	2	
2	2	2	

1	2	1
2	1	2
1	2	1



Image Processing Summary (7)

- 2-D Discrete Fourier Transform (DFT)
- Lowpass/highpass filters





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Image Processing Summary (10)

•Implementation:

- Compute the image histogram (n: total number of pixels, n_i : number of pixels with gray level r_i):

$$p_r(r_k) = \frac{n_k}{n}$$
 $k = 0, 1, 2, ..., L-1$

Compute the cumulative histogram:

$$-s_k = \sum_{j=0}^k p_r(r_j)$$

New gray level values:

$$h(r_k) = \frac{s_k - s_{min}}{(MN) - s_{min}} (L - 1)$$



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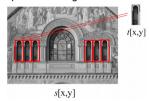
Games Audio Summary

Image Processing Summary (8)

• 2-D correlation:

$$x[m,n] \circ y[m,n] = \frac{1}{RS} \sum_{r=0}^{R-1} \sum_{s=0}^{S-1} x * [r,s] y[m+r,n+s]$$

Used for template matching





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Image Processing Summary (11)

Histogram equalisation example:

	52	55	63	67	63	52	2	2	0
	63	59	55	90	90	55	4	6	44
	63	59	68	90	68	58	1	7	55
	63	58	68	55	63	59	3	10	89
	67	52	68	59	55	63	6	16	155
n	nage	9				67	2	18	177
						68	4	22	222
						90	3	25	255

Pixels, histogram, cumulative histogram, new pixel values



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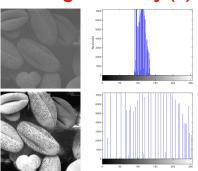
Real Time DSP

- · DSP algorithms can run in real time on generalpurpose computers
- A lot of tasks can actually be quite cheap to run (O(n) or $O(n \log n)$
- Applications: DAWs, effects racks, VoIP and video software.



Image Processing Summary (9

Histogram equalisation: method for contrast adjustment





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Image Processing Summary (12)

• Image restoration: reconstruct or recover an image that has been degraded

$$g(x,y)=h(x,y)*f(x,y)+\eta(x,y)$$

- · Noise cannot be predicted but can be approximately described in statistical way using a probability density function (PDF)
- · Minimum mean square error filtering (Wiener filtering)



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The Real Time Paradigm

- Real time DSP is done by processing a buffer of samples.
- This means there will always be some latency (delay) between input and output.
- Increasing the buffer size increases the latency, but reduces computational cost.



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Typical Sound Engine Features (e.g. FMOD)

- Support for SW and HW voices and effects
- 3D sound rendering
- · Reverb and many other effects
- . Dynamic voice management by audibility (Virtual Voices)
- · Sound processing graphs
- Allow sound designers and audio developers to work independently



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Doppler Effect

- · Doppler Effect changes frequency for moving sources
 - fp = f vs/(vs-vr)with fp: perceived frequency, f: frequency, vs: velocity of sound (~340m/s). vr: velocity relative to the listener (positive = approaching)
 - Example: car moves with 68 m/s producing a 300 Hz sound. fp for a stationary listener in front of the car is

300 Hz * 340/340-68 = 300 Hz *5/4 = 375 Hz



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Programming 3D Sounds with FMOD

- Set up the FMOD systems 3D settings: system->set3DSettings(doppler, distFactor, distRolloff);
- · Where:
 - doppler scales the intensity of the doppler effect
 - distFactor determines the length of an FMOD unit (1 means 1m – in the OpenGL template, use 10)
 - distRolloff scales the distance roll-off (1 is like real world)



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Directional Hearing and Localisation

- · Directional hearing is based mostly on binaural hearing
 - Interaural Intensity Differences (IID)
 - Interaural Time Differences (ITD)
 - IID and ITD vary over frequencies.
- · IID and ITD give only information on left-right
 - front-back and high-low are detected through head-related transfer functions (head shape, pinna)
- · Room reflection
 - absorbing and reflecting objects give clues for source location



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Programming (2D) Sounds with FMOD

· Load a sound:

FMOD::Sound *sound; result = system->createSound(filename, FMOD LOOP OFF, 0, &sound); FmodErrorCheck(result);

Create a Channel object and play the sound

FMOD::Channel channel = null; result = system->playSound(sound, NULL, false, &channel):

channel now has the channel where sound is played

// set the Volume result = channel->setVolume(0.8f);



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Custom FMOD DSPs

DSP inserts

For whole system (all channels):

system->addDSP()

For specific channel

channel->addDSP()





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Intensity and Distance

- · Intensity is power (energy per time) per area, measured in Watts/Meter²
- 0 dB (decibels) Sound Pressure Level defined as 10-12 W/m² (~threshold of hearing)
- · dBs are on a logarithmic scale
- · Intensity decreases as the square of distance
- · Power increases as the square of amplitude
- · Example: 60dB SPL at 1m means 40dB SPL at 10m (10-fold distance -> 100-fold decrease -> -10^2 = -2B = -20dB)



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3D Modelling in FMOD

- FMOD has its own 3D coordinate system and model
- Need to coordinate
 - listener positions and velocities
 - sound source positions and velocities
 - objects in 3D that occlude or obstruct sound



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Circular Buffer

 Avoid high buffer maintenance costs



x[t-k]

· Address the buffer for writing:

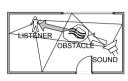
pos % bufferLength

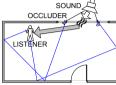
Use index delay offset

 (pos - delay) % bufferLength points to read position

Occlusion

- Obstruction: obstacle blocks direct path between sound source and listener.
- Occlusion: occluder blocks all paths from the source to the listener.







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Loops and Meter

- The metrical structure is normally maintained during loop playback.
- Common loop sizes are 4, 8 or 16 bars (although sometimes musical structures have different values, e.g. 'Eleanor Rigby' by the Beatles has a 5 bar structure)



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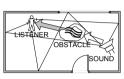
MIDI vs Audio in Loops

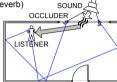
- Audio
 - can have superior quality (e.g. recorded human performance)
 - costly and lossy change of pitch/tempo
 - changing individual notes hardly possible
 - → careful planning needed, good for final production
- MIDI
 - very flexible (easy to change tempo, pitch, notes)
 - → can experiment, good for developing a soundtrack

Occlusion

- Material, size and shape of the object determine how much sound (if any) reaches the listener
- Effects: drop in amplitude, loss of high frequency components (low pass filter)

· Reflected sound is still audible (with reverb)







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Loops and Harmony

- Harmony describes the sounding of several (pitched) notes together
- In harmonic contexts, some notes sound consonant, others sound dissonant/inappropriate.
- Layered music loops need common harmonic structure (not true for sound loops)
- Each layer in the same harmonic pattern ensures they are musically 'compatible'



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Time Series Summary

FMOD for Game Music

- Supports
 - Loop
- Synchronisation based on beats and bars
- Conditional transitions and repetitions
- Integrated with FMOD Event system



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MIDI vs Audio

- MIDI representation
 - used mostly in music production
 - used to be applied in Games directly
- · MIDI is symbolic representation
 - Advantages:
 - · independent tempo and pitch
 - · easy to modify for musicians
 - · low data volume
 - Disadvantages
 - sound quality (depends on used sound library)



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Prediction by Smoothing with Moving Average

• Moving average of span k smoothes the data

$$\hat{y}_t = (y_t + y_{t-1} + \dots + y_{t-k-1})/k$$

(ŷ is the prediction)

- A low pass FIR filter with coefficients 1/k,1/k, ..., 1/k
- ●In Matlab: filter([.25,.25,.25,.25],[1],Y)

- Moving average of infinite span smoothes the data
 - $\widetilde{y}_{,-} = w y_{,+} (1-w) \widetilde{y}_{,-1}$
- A low-pass IIR filter with coefficients w and (1-w) In Matlab: filter([.25],[1,-(1-.25)],Y)
- Assumption:
 - Recent values are more important than older ones



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Residual Autocorrelation

 After linear modelling and seasonal adjustment we can study the autocorrelation of the residuals $e_t = y_t - \hat{y}_t$

Correlations					
Residua	Log Passengers Lag 1	Residuals Lag	2 Residuals		
Residual Log Passengers	1.0000	0.7896	0.6722		
Lag 1 Residuals	0.7896	1.0000	0.7832		
Lag 2 Residuals	0.6722	0.7832	1.0000		

•With linear regression we can improve the prediction based on residuals

$$\hat{e}_t = -0.000153 + 0.7918985e_{t-1}$$

•This is a form of a generalised (weighted) moving average

$$y_t = \hat{y} + e_t + \sum_{i=1}^{q} \theta_i e_{t-i}$$



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Maximum Likelihood and Regularisation

- Common approach: Linear models with least squares optimisation
- •Maximise the likelihood of the data given the prediction (assuming normal distribution)
- Regularisation helps avoid overfitting (especially with small datasets)
- Most popular: keep size of parameters low using a 'penalty term': sum of squares or absolutes of the parameters (ridge or lasso)
- Add penalty term to errors and calculate gradient to optimise (use packaged solutions)



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Linear Trend Estimation

•Linear regression: find a straight line to fit the data

$$\hat{y}_{t} = a_{0} + a_{1}t$$

• Determine a, and a, to minimise the sum or squares error $sse = \sum_{i} (\hat{y}_{i} - y_{i})^{2}$

Solve the system of equations

In Matlab: coeff = polyfit(t,y,1)



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Harmonic Modelling

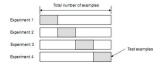
- · Fourier modelling for residuals or seasonality
 - · keep only strong components (assumption: weaker components contain noise)
 - Advantage: more efficient than autocorrelation. calculation with FFT
- Disadvantage: need to know cycle length, less robust than autocorrelation



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Cross-Validation for Regularisation

- Optimise regularisation and other parameters:
- •Divide the data into k equally sized subsets ('folds')
- Adapt the model to k-1 joint subsets, test on the remaining subset, and iterate through all folds
- Test a grid of regularisation values (or other parameters) and choose the one with best results on test sets





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Seasonal Average Method

- Seasonal averages = seasonal values total / # of years
- •General average = seasonal averages total / # of seasons
- •Multiplicative modelling: Seasonal index = seasonal average / general average
- •Additive modelling: Seasonal offset = seasonal average – general average



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Modelling Caveats

- · Overfitting:
 - to many parameters → model learns noise in the data but not the trend
- need to test on data not used in building the model
- · cross-validation can when data is scarce
- · Predictions get less reliable further away from sample data



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More Information

- Mock paper on Moodle for your reference
- If you have any questions, please get in touch