

# Covariance and correlation

```
>> load hospital.mat  
>> X = [hospital.Weight hospital.BloodPressure]
```

X =

```
176 124 93  
163 109 77  
131 125 83  
186 119 74  
172 136 93  
177 114 86  
.....
```

```
>> C=cov(X)
```

C =

```
706.0404 27.7879 41.0202  
27.7879 45.0622 23.8194  
41.0202 23.8194 48.0590
```

```
>> Y = [hospital.Age hospital.BloodPressure]
```

Y =

```
38 124 93  
43 109 77  
49 119 74  
45 136 93  
48 114 86  
.....
```

```
>> D=corrcoef(Y)
```

D =

```
1.0000 0.1341 0.0806  
0.1341 1.0000 0.5118  
0.0806 0.5118 1.0000
```

See also:

**hospital.m** file provided with this model answer

**Corrcov()** - convert covariance matrix to correlation matrix

**R = corrcov(C)** returns the correlation matrix R corresponding to the covariance matrix C.

**[R,sigma] = corrcov(C)** also returns sigma, a vector of standard deviations.

## Compare Correlation Matrices Obtained by Two Different Methods

Compare the correlation matrix obtained by applying **corrcoef** on a covariance matrix with the correlation matrix obtained by direct computation using **corrcoef** on an input matrix.

Load the hospital data set and create a matrix containing the **Weight** and **BloodPressure** measurements. Note that **hospital.BloodPressure** has two columns of data.

```
>> load hospital
>> X = [hospital.Weight hospital.BloodPressure];
>> C = cov(X)
```

C =

```
706.0404  27.7879  41.0202
27.7879  45.0622  23.8194
41.0202  23.8194  48.0590
```

```
>> R1 = corrcoef(C)
```

R1 =

```
1.0000  0.1558  0.2227
0.1558  1.0000  0.5118
0.2227  0.5118  1.0000
```

```
>> R2 = corrcoef(X)
```

R2 =

```
1.0000  0.1558  0.2227
0.1558  1.0000  0.5118
0.2227  0.5118  1.0000
```

## Optional (advanced): Find Standard Deviations from Covariance Matrix

Find the vector of **standard deviations from the covariance matrix**, and show the relationship between the standard deviations and the covariance matrix.

Load the hospital data set and create a matrix containing the **Weight**, **BloodPressure**, and **Age** measurements. **Note that hospital.BloodPressure** has two columns of data.

```
>> load hospital
>> X = [hospital.Weight hospital.BloodPressure hospital.Age];
>> C = cov(X)
```

C =

```
706.0404  27.7879  41.0202  17.5152
27.7879  45.0622  23.8194   6.4966
41.0202  23.8194  48.0590   4.0315
17.5152   6.4966   4.0315  52.0622
```

C is square, symmetric, and positive semidefinite. The diagonal elements of C are the variances of the four variables in X.

Compute the correlation matrix and standard deviations of X from the covariance matrix C.

```
>> [R,s1] = corrcov(C)
```

R =

```
1.0000  0.1558  0.2227  0.0914
0.1558  1.0000  0.5118  0.1341
0.2227  0.5118  1.0000  0.0806
0.0914  0.1341  0.0806  1.0000
```

s1 =

```
26.5714
 6.7128
 6.9325
 7.2154
```

Compute the square root of the diagonal elements in C, and then compare s1 with s2.

```
>> s2 = sqrt(diag(C))
```

s2 =

```
26.5714
 6.7128
 6.9325
 7.2154
```

**s1 and s2 are equal and correspond to the standard deviation of the variables in X.**

## Decision Trees

Please go to the example on data set **fisheriris** provided at:

[https://uk.mathworks.com/help/stats/compactclassificationtree.predict.html?searchHighlight=predict&s\\_tid=doc\\_srchttitle#bst08bg-4](https://uk.mathworks.com/help/stats/compactclassificationtree.predict.html?searchHighlight=predict&s_tid=doc_srchttitle#bst08bg-4)