

1) Decimal to Binary

a)
$$\begin{array}{r|l} 10 & 0 \\ 5 & 1 \\ 2 & 0 \\ 1 & 1 \end{array} \quad 1010$$

b)
$$\begin{array}{r|l} 1369 & 1 \\ 684 & 0 \\ 342 & 0 \\ 171 & 1 \\ 85 & 1 \\ 42 & 0 \end{array} \quad \begin{array}{r|l} 21 & 1 \\ 10 & 0 \\ 5 & 1 \\ 2 & 0 \\ 1 & 1 \\ 0 & \end{array} = 10101011001$$

c)
$$\begin{array}{r|l} 9234876 & 0 \\ 4617438 & 0 \\ 2308719 & 1 \\ 1154359 & 1 \\ 577179 & 1 \\ 288589 & 1 \\ 144294 & 0 \end{array} \quad \begin{array}{r|l} 72147 & 1 \\ 36073 & 1 \\ 18036 & 0 \\ 9018 & 0 \\ 4509 & 1 \\ 2254 & 0 \\ 1127 & 1 \\ 563 & 1 \\ 281 & 1 \\ 140 & 0 \\ 70 & 0 \\ 35 & 1 \\ 17 & 1 \\ 8 & 0 \\ 4 & 0 \\ 2 & 0 \\ 1 & 1 \end{array}$$

d)
$$\begin{array}{r|l} 49263749 & 1 \\ 24631874 & 0 \\ 12315937 & 1 \\ 6157968 & 0 \\ 3078984 & 0 \\ 1539492 & 0 \\ 769746 & 0 \\ 384873 & 1 \end{array} \quad \begin{array}{r|l} 192436 & 0 \\ 96218 & 0 \\ 48109 & 1 \\ 24054 & 0 \\ 12027 & 1 \\ 6013 & 1 \\ 3006 & 0 \\ 1503 & 1 \end{array} \quad \begin{array}{r|l} 751 & 1 \\ 375 & 1 \\ 187 & 1 \\ 93 & 1 \\ 46 & 0 \\ 23 & 1 \\ 11 & 1 \\ 5 & 1 \end{array} \quad \begin{array}{r|l} 2 & 0 \\ 1 & 1 \\ 0 & \end{array}$$

$$= 1011101111011010010000101$$

$$= 10001100111010011011100$$

Decimal to Binary using 2's complement

a)
$$\begin{array}{l} -20 \xrightarrow{2^5} 010100 \\ \quad \quad \quad \xrightarrow{2^0} 101011 \end{array} \xrightarrow{+1} 101100$$

$$-3925 \xrightarrow{2^{15}} 0111101010101 \xrightarrow{+1} 1000010101010$$

b)
$$\begin{array}{l} -10 \xrightarrow{2^4} 01010 \\ \quad \quad \quad \sim 10101 \end{array} \xrightarrow{+1} 10110$$

$$-104596 \xrightarrow{2^{19}} 011001100010010100 \xrightarrow{+1} 100110011101101011$$

Unsigned binary to hex

a)
$$\begin{array}{cccccccccccccccccccc} 31 & 30 & 29 & 28 & 27 & 26 & 25 & 24 & 23 & 22 & 21 & 20 & 19 & 18 & 17 & 16 & 15 & 14 & 13 & 12 & 11 & 10 & 9 & 8 & 7 & 6 & 5 & 4 & 3 & 2 & 1 & 0 \\ 1 & 1 & 0 & 0 & 1 & 1 & 1 & 1 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 \end{array} = CFS66ED829$$

$$\begin{array}{r|l} 890568335145 & 9 \\ 55656720946 & 2 \\ 3478548184 & 8 \\ 217409261 & D \\ 1358078 & E \end{array} \quad \begin{array}{r|l} 849259 & 6 \\ 53078 & 6 \\ 3317 & 5 \\ 207 & F \\ 12 & C \end{array} = CFS66ED829$$

b)
$$\begin{array}{cccccccccccccccccccc} 31 & 30 & 29 & 28 & 27 & 26 & 25 & 24 & 23 & 22 & 21 & 20 & 19 & 18 & 17 & 16 & 15 & 14 & 13 & 12 & 11 & 10 & 9 & 8 & 7 & 6 & 5 & 4 & 3 & 2 & 1 & 0 \\ 1 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 1 & 1 \end{array} = 878E38E8F3$$

$$\begin{array}{r|l} 58226678003 & 3 \\ 36387917375 & F \\ 227424835 & 3 \\ 142146302 & E \\ 9883768 & 8 \\ 555235 & 3 \end{array} \quad \begin{array}{r|l} 34702 & E \\ 2168 & 8 \\ 135 & 7 \\ 8 & 8 \end{array} = 878E38E8F3$$

1) 1010110101011100011001010100101010101010 = ADSC6S4AAA

744524489330	A	44380	C	
4653621770	A	2773	S	
2908513610	A	173	D	
181782106	4	10 =	A	
11361381	S			
710086	6			

ADSC6S4AAA

101000101010101010101010101111111000000 = AZAAAAABFCO

698648018880	0	41642	A	
43665501180	C	2602	A	
2729093823	F	162	2	
170568363	B	10 =	A	
16660526	A			
666282	A			

AZAAAAABFCO

Binary to Octal

111111000001111100000001110101011
neg +1
000000111100001111110001010101 = -760376125

130163557	S	3921	3
16264192	2	496	0
2033649	1	62	6
262206	6	7	7
31775	7	0	0

0101010101011111111111110000000 = 25257777600

2862769564	0	1365	S	
42761086	6	170	2	
5695135	7	21	S	
699391	7	2	2	
87423	7	0	0	
10927	7	0	0	

25257777600

1110001110000001111111100000101010 +1
000110001111100000001111010110 = -16176063726

1912680342	6
236010042	2
29076255	7
3734531	3
466816	0
58352	0
7292	6
911	2

113	1
14	6
1	1
0	
16176003726	

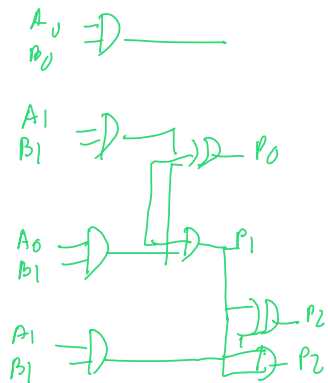
101010101010000010101010101111000

010101010101111010101010001000 -5253725240

0729244429	0	341	5	-5253725240
716166663	1	42	2	
89619444	4	5	5	
11109930	2	0		
1398741	5			
174842	2			
21865	7			
2731	3			

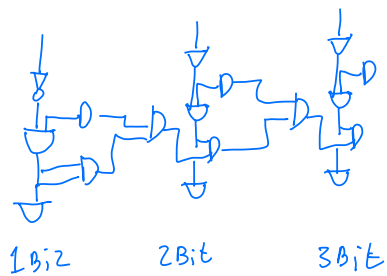
2) Boolean circuit

a) Multiplication of 2 2bit Numbers



A ₁	A ₂	B ₁	B ₂	P ₃	P ₂	P ₁	P ₀
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0
0	0	1	0	0	0	0	0
0	0	1	1	0	0	0	0
0	1	0	0	0	0	0	0
0	1	0	1	0	0	0	1
0	1	1	0	0	0	1	0
0	1	1	1	0	0	1	1
1	0	0	0	0	0	0	0
1	0	0	1	0	0	1	0
1	0	1	0	0	1	0	0
1	0	1	1	0	1	1	0
1	1	0	0	0	0	0	0
1	1	0	1	0	0	1	1
1	1	1	0	0	1	1	0
1	1	1	1	1	0	0	1

b) 2's Complement



A ₂	A ₁	A ₀	
0	0	0	000
0	0	1	111
0	1	0	100
0	1	1	011
1	0	0	001
1	0	1	110
1	1	0	101
1	1	1	010

3) Multiplications in binary

a) -5×8

$-5 = 1011 = MP$

$8 = 01000 = Q$

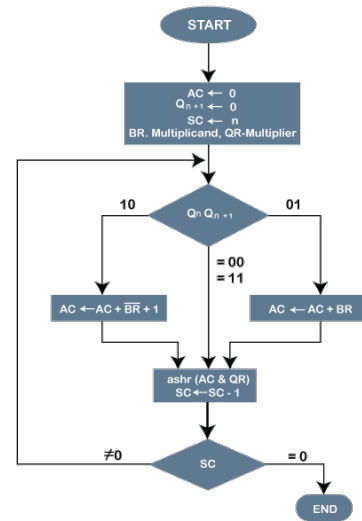
$n = 6$

PP	Q	Q _n	Operation
0000	1000	0	.
0000	0100	0	Shift
0000	0010	0	Shift
0000	0001	0	Shift
0101	0001	0	PD-MP
0010	1000	1	Shift

$PD = PD - MP$

$$\begin{array}{r} 0000 \\ + 0101 \\ \hline 0101 \end{array}$$

$001010001 = -40$



b) $11 \times (-10)$

$11 = 0101$

$-10 = 10110$

$-11 = 10101 = MP$

PP	Q	Q _n	Operation
00000	101100	0	.
00000	01011	0	Shift
10101	01011	0	PD-MP
11010	10101	1	Shift
11101	01010	1	Shift
01000	01010	1	PD+MP
00100	00101	0	Shift
11001	00101	0	PD-MP
11100	10010	1	Shift

$$\begin{array}{r} 00000 \\ + 10101 \\ \hline 10101 \end{array}$$

$$\begin{array}{r} 11101 \\ + 01011 \\ \hline 101000 \end{array}$$

$$\begin{array}{r} 00100 \\ 10101 \\ \hline 11001 \end{array}$$

$1110010010 = -110$

c) 2x3

$$\begin{aligned} 2 &= 010 & -2 &= 110 \\ 3 &= 011 & -3 &= 101 \end{aligned}$$

PD	Q	Q ₁	Operation
000	010	0	
000	001	0	Shift
101	001	0	PD-MD
110	100	1	Shift
001	100	1	PD+MD
000	110	0	Shift

$$\begin{array}{r} 006 \\ 101 \\ \hline 165 \end{array}$$

$$\begin{array}{r} 110 \\ 011 \\ \hline 1001 \end{array}$$

$$000110 \approx 6$$

-4 x -8

$$4 = 0100 \quad -4 = 1100$$

$$8 = 01000 \quad -8 = 11000$$

PD	Q	Q ₁	Operation
0000	1100	0	
0000	0110	0	Shift
0000	0011	0	Shift
1000	0011	0	PD-MD
0100	0001	1	Shift
0010	0000	1	Shift

$$\begin{array}{r} 0000 \\ 01000 \\ \hline 01000 \end{array}$$

$$00100000 \approx 32$$