Price Property Checker of ESELSystem1 for the ESEL System

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1 Header

```
section ESELHeader parents circus_toolkit
```

This section gives all basic definitions that will be used in all three *Circus* models. And gateway related definitions are only used in the ESEL System 2.

First of all, three constants are defined. MAX_ESEL and MAX_PID stand for maximum number of displays and maximum number of product categories (or, products for short) in the system separately. And constant $MAX_GATEWAY$ stands for maximum number of gateways.

```
MAX\_ESEL: \mathbb{N}
MAX\_PID: \mathbb{N}
```

Then all displays and products are identified by a tag plus a unique number which are defined in the free types ESID and PID below where the constructors ES and PD are the tags for displays and products. For an instance, number ten of the display is given ES 10 or ES(10). Similarly, GID gives all identities for gateways.

```
\begin{split} ESID ::= ES\langle\langle 1 ... MAX\_ESEL \rangle\rangle \\ PID ::= PD\langle\langle 1 ... MAX\_PID \rangle\rangle \end{split}
```

The type of product price is defined as an abbreviation to natural numbers \mathbb{N} .

```
Price == \mathbb{N}
```

The unit response is defined as a free type with two constants: uok and ufail.

```
UStatus ::= uok \mid ufail
```

The response from this program to the environment is a set of product identities of which the price is not updated successfully due to 1) no linked ESEL ID to the product or 2) failed update to its linked ESEL. The first reason is given the status constant NA and the second is provided the constructor $fail\langle\langle ESID\rangle\rangle$.

```
FStatus ::= fail \langle \langle ESID \rangle \rangle \mid NA
```

Two channels are provided to update the map from ESEL ID to product ID. *updateallmap* will clear all stored map and use the input map as new map, while *updatemap* just updates a partial map. In this map, one ESEL can be linked to up to one product. However, one product may associate with multiple ESELs.

```
channel updateallmap : ESID \rightarrow PID channel updatemap : ESID \rightarrow PID
```

Similarly, two channels are provided to update the price information. *updateallprice* will clear all price information and use the input price information as new price, while *updateprice* just updates price partially.

```
channel updateallprice : PID \rightarrow Price
channel updateprice : PID \rightarrow Price
```

The *update* channel gives a signal to the program to start update process.

```
channel update
```

The failures channel returns all failed products and related error reasons after update. Since one product may associate with multiple displays, the return status is a power set of FStatus to denote which specific displays that the product links are updated unsuccessfully. But it is worth noting that NA and fail must not occur in a product's return set at the same time because they can not be both no associate display and associate display update fail.

```
channel failures : PID \rightarrow \mathbf{P} FStatus
```

The internal *resp* event is used to collect update responses from all displays and *terminate* event is for completing the collection.

```
channel resp: PID \times FStatus
channel terminate
channelset RespInterface == \{ | resp, terminate | \}
```

This *uupdate* event is to update one ESEL to the specific price, and *ures* for update response from this ESEL. And *udisplay* is used to synchronise the show of price on all ESELs at the same time and *finishdisplay* is used to wait for display completion of all ESELs. That is the similar case for *uinit* and *ufinishinit* that are for initialisation synchronisation.

```
channel uupdate : ESID \times Price
channel ures : ESID \times UStatus
channel uinit, finishuinit
channel udisplay, finishudisplay
```

And display is used to synchronise the show of price on all gateways (or ESELs) at the same time and finishdisplay is used to wait for display completion of all gateways (or ESELs). That is the similar case for init and finishinit that are for initialisation synchronisation.

```
channel init, finishinit channel display, finishdisplay
```

The channels below are for communication between the ESEL system and displays. The *write* event writes price to a display, and the *read* event reads price from the display. *ondisplay* turns on the related display and *offdisplay* turns off it conversely.

```
\begin{array}{ll} \textbf{channel} & \textit{write} : \textit{ESID} \times \textit{Price} \\ \textbf{channel} & \textit{read} : \textit{ESID} \times \textit{Price} \\ \textbf{channel} & \textit{ondisplay} : \textit{ESID} \\ \textbf{channel} & \textit{offdisplay} : \textit{ESID} \\ \end{array}
```

2 Price Checker

section ESELPriceChecker parents ESELHeader

```
process PriceChecker = \mathbf{begin}
              state State == [dummy : \{0\}]
              Init == [(State)' \mid dummy' = 0]
              AOnDisplay \stackrel{\frown}{=} eid : ESID \bullet ondisplay.eid \rightarrow
                            (||| e : (ESID \setminus (\{eid\})) \parallel \varnothing \parallel \bullet (offdisplay.e \to \mathbf{Skip}))
              AOffDisplay = (||| e : ESID \parallel \varnothing \parallel \bullet (offdisplay.e \to \mathbf{Skip}))
              ACheckMap \stackrel{\frown}{=} p : Price ; eid : ESID ; pid : PID \bullet
                            (updateallmap.(\{eid \mapsto pid\}) \rightarrow updateallprice.(\{pid \mapsto p\}) \rightarrow
                            update \rightarrow write.eid.p \rightarrow (
                                                 (read.eid.p \rightarrow AOnDisplay(eid); failures.(\{\}) \rightarrow \mathbf{Skip})
                                          \Box (read.eid?x: (x \neq p) \rightarrow AOffDisplay;
                                                       failures.(\{pid \mapsto \{(fail\ eid)\}\}) \rightarrow \mathbf{Skip})
              ACheckNoMap \stackrel{\frown}{=} p : Price ; eid : ESID ; pid : PID \bullet
                            (updateallmap.(\{\}) \rightarrow updateallprice.(\{pid \mapsto p\}) \rightarrow update \rightarrow p)
                            AOffDisplay ; failures.(\{pid \mapsto \{NA\}\}) \rightarrow \mathbf{Skip})
               ACheck = \mathbf{var} \ p : Price \ ; \ eid : ESID \ ; \ pid : PID \bullet
                            ACheckMap(p, eid, pid) \square ACheckNoMap(p, eid, pid)
              • Init; AOffDisplay; (\mu X \bullet (ACheck); X)
end
channelset ESELSystemInterface == \{ | updateallprice, updateprice, | updatepr
                            updatemap, updateallmap, update, ondisplay, offdisplay,
                            write, read, failures |}
section ESELSystem1 Checker parents ESELPriceChecker, ESELSystem1
process ESELSystem1Checker =
              (PriceChecker | ESELSystemInterface | ESELSystem1)
```