

70087 ExerciseTypes.CW1

Coursework 1

Submitters

sf23

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9/10. Good work. Well done.

Emarking

CW1

(a)

A best case input is any array A that the first element in A does not equal to x. Or A is an empty array. An example of this case is that $x=1$ and $A = [2, 1]$.

$T_{\text{COUNTWHILE}}(N) = c$, where c is a positive constant. So $T_{\text{COUNTWHILE}}(N) = \Theta(1)$.

A worst case input is any array A that each element in A equals to x. An example of this case is that $x=1$ and $A = [1, 1, \dots, 1]$.

$T_{\text{COUNTWHILE}}(N) = aN + b$, where a, b are positive constants. So $T_{\text{COUNTWHILE}}(N) = \Theta(N)$.

(b)

$T_{\text{cf}}(N) = 1$ if $N=0$

$T_{\text{cf}}(N) = T_{\text{cf}}(N-1) + d$ if $N > 1$

Not 1. Use some constant, c.

(c)

For the worst case, $T_{\text{cf}}(N) = T_{\text{cf}}(N-1) + d$ if $N > 1$ (a)

$T_{\text{cf}}(N-1) = T_{\text{cf}}(N-2) + d$ if $N > 2$ (b)

Replace $T_{\text{cf}}(N-1)$ in formula (a) with the definition in (b), we gain the following formula.

$T_{\text{cf}} = T_{\text{cf}}(N-2) + 2d$

By continuing, we can extract a general form $T_{\text{cf}}(N) = T_{\text{cf}}(N-i) + id$ if $N > i > 1$

Setting $i=N-1$, we have $T_{\text{cf}}(N) = T_{\text{cf}}(1) + (N-1)d$ if $N > 1$

Since $T_{\text{cf}}(1)$ is a constant, $T_{\text{cf}}(N) = \Theta(N)$.

(d)

For a best case input, $T_{\text{cw}}(N) = \Theta(1)$.

For a worst case input, $T_{\text{cw}}(N) = \Theta(N)$.

So, $T_{\text{cw}}(N) = \Omega(1)$

$T_{\text{cw}}(N) = O(N)$

There is no Θ bound because the time complexity is different depending on the input.

(e)

For the upper bound, the recursive function will be called a maximum time. $A_{\text{cw}}(N) = \Theta(N)$.

For the lower bound, it reflects the minimal space needed for a single non-recursive call.

$A_{\text{cw}}(N) = \Theta(1)$.

So, $A_{\text{cw}}(N) = \Omega(1)$

$A_{\text{cw}}(N) = O(N)$