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Normalisation

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Database CW2

Exercise 1. 15/25

1.

(a) $A \rightarrow BC$

(b) $B \rightarrow AC$

(c) $C \rightarrow AB$

	Minimal cover
C is extraneous in $A \rightarrow BC$ because $C \in \{A\}^+ = \{B\} + \{C\}$	(a) $A \rightarrow B$ (b) $B \rightarrow AC$ (c) $C \rightarrow AB$
A is extraneous in $B \rightarrow AC$ because $A \in \{B\}^+ = \{A\} + \{C\}$	(a) $A \rightarrow B$ (b) $B \rightarrow C$ (c) $C \rightarrow AB$
B is extraneous in $C \rightarrow AB$ because $B \in \{C\}^+ = \{A\} + \{B\}$	(a) $A \rightarrow B$ (b) $B \rightarrow C$ (c) $C \rightarrow A$

The minimal cover for the given FD set is $\{A \rightarrow B, B \rightarrow C, C \rightarrow A\}$. Correct

2.

	Minimal cover
$RU \rightarrow S$ and $S \rightarrow RU$ is redundant. We can remove one.	(a) $P \rightarrow S$, (b) $PQ \rightarrow ST$, (c) $S \rightarrow RU$, (d) $PT \rightarrow V$
S is extraneous in $PQ \rightarrow ST$ because $P \rightarrow S$ makes $S \in \{P\}^+$	(a) $P \rightarrow S$, (b) $PQ \rightarrow T$, (c) $S \rightarrow RU$, (d) $PT \rightarrow V$

The minimal cover for the given FD set is $\{P \rightarrow S; PQ \rightarrow T; S \rightarrow RU; PT \rightarrow V\}$

-10 Incorrect: The minimal cover is: $P \rightarrow S, PQ \rightarrow T, S \rightarrow RU, RU \rightarrow S, PT \rightarrow V$. Where did the $RU \rightarrow S$ go?

Exercise 2. 25/25

(a) One key is AB.

$\{AB\}^+ = \{A, B\} + \{C\} + \{D, E\} + \{F\} + \{G, H\} + \{I, J\} = \{A, B, C, D, E, F, G, H, I, J\}$

(b) Firstly, calculate the canonical cover. Correct

$A, B \rightarrow C$

$A \rightarrow D, E$

$B \rightarrow F$

$F \rightarrow G, H$

$D \rightarrow I, J$

According to the cover, we gain:

$R1(A, B, C), R2(A, D, E), R3(B, F), R4(F, G, H), R5(D, I, J)$ Correct

Exercise 3. 15/25

(1) R1(A, C, B, D, E), $A \rightarrow B, C \rightarrow D$

Candidate key {A, C, E}

a) the Strongest Normal Form:

Check for 1NF: It's in 1NF because it contains only atomic values.

Check for 2NF: It's not in 2NF because it contains partial dependencies. Partial Dependency occurs when a non-prime attribute is functionally dependent on part of a candidate key. For {B}, it is functionally dependent on {A}, which is part of the candidate key {A, C, E}

Correct

b) Decompose into BCNF:

Ra (A, B)

Rb (C, D) Correct

Rc (A, C, E)

(2) R2(A, B, F), $AC \rightarrow E, B \rightarrow F$

Since $AC \rightarrow E$ is ignored because it is not related to the relation.

R2(A, B, F), $B \rightarrow F$

Candidate key {A, B}

a) the Strongest Normal Form:

Check for 1NF: It's in 1NF because it contains only atomic values. Correct

Check for 2NF: It's not in 2NF because it contains partial dependencies. For a non-prime attribute {F}, it is functionally dependent on {B}, which is part of the candidate key {A, B}. So, this is partial dependency and makes the relation not in 2NF.

b) Decompose into BCNF:

Ra (B, F) Correct

Rb (A, B)

(3) R3(A, D), $D \rightarrow G, G \rightarrow H$

Since $D \rightarrow G, G \rightarrow H$ should be ignored because it is not related to this relation schema.

R3(A, D)

Candidate key {A, D}

a) the Strongest Normal Form:

Check for 1NF: It's in 1NF because it contains only atomic values.

Check for 2NF: Cannot decide this because we do not know any functional dependency about it.

b) Decompose into BCNF:

Ra (A, D)

-5 The relation is already in BCNF

Rb (D, G)

Rc (G, H)

(4) R4(D, C, H, G), $A \rightarrow I, I \rightarrow A$

Since $A \rightarrow I, I \rightarrow A$ should be ignored because it is not related to this relation schema.

R4(D, C, H, G)

Candidate key {D, C, H, G}

a) the Strongest Normal Form:

Check for 1NF: It's in 1NF because it contains only atomic values.

Check for 2NF: Cannot decide this because we do not know any functional dependency about it.

Check for 3NF: A is not prime because it is not a member of candidate key {D, C, H, G}.

It is not in 3NF. Neither the LHS of every nontrivial FD is a superkey, nor every attribute on the RHS of a FD is prime.

b) Decompose into BCNF:

-5 The relation is already in BCNF

Ra (D, C, H, G)

Rb (A, I)

Exercise 4. 9/25

(1) $C \rightarrow D, C \rightarrow A, B \rightarrow C$

(a)

$\{A\}^+ = \{A\}$

$\{C\}^+ = \{C, D, A\}$

$\{B\}^+ = \{B, C, D, A\}$

$\{D\}^+ = \{D\}$

candidate key: {B} Correct

(b) The highest normal form

Check for 1NF: It's in 1NF because it contains only atomic values.

Check for 2NF: It's not in 2NF because it contains partial dependencies. For non-prime attribute {D}, it depends on {C}.

Check for 3NF: It's not in 3NF because it contains transitive dependencies. One transitive dependency is $B \rightarrow C$ and $C \rightarrow D$.

-2 This relation is in 2NF. $C \rightarrow D$ and $C \rightarrow A$ violates 3NF as non-prime attributes are determined by another non-prime attribute.

(c) Decompose into BCNF:

Ra (C, D)

Rb (A, C) Correct

Rc (B, C)

(2) $B \rightarrow C, D \rightarrow A$

(a)

$\{A\}^+ = \{A\}$

$\{B\}^+ = \{B, C\}$

$\{C\}^+ = \{C\}$

$\{D\}^+ = \{D, A\}$

candidate key: {B, D} Correct

(b) The highest normal form

Check for 1NF: It's in 1NF because it contains only atomic values.

Check for 2NF: It's in 2NF because it contains no partial dependencies.

Check for 3NF: It's in 3NF because it contains no transitive dependencies.

Check for BCNF: It's not in BCNF because for all non-trivial FDs, not every LHS of every FD is a superkey.

-2 Incorrect, this relation is 1NF. $D \rightarrow A$ and $B \rightarrow C$ makes A and C partially functionally dependent on BD.

(c) Decompose into BCNF:

Ra (B, C)

Rb (A, D) Correct

Rc (B, D)

(3) $ABC \rightarrow D, D \rightarrow A$

(a)

$\{A\}^+ = \{A\}$

$\{B\}^+ = \{B\}$

$\{C\}^+ = \{C\}$

$\{D\}^+ = \{D, A\}$

$\{ABC\}^+ = \{A, B, C, D\}$

candidate key: $\{A, B, C\}$, $\{B, C, D\}$ Correct

(b) The highest normal form

Check for 1NF: It's in 1NF because it contains only atomic values.

Check for 2NF: It's in 2NF because it contains no partial dependencies.

Check for 3NF: It's not in 3NF because it contains transitive dependencies.

-2 The highest normal form is 3NF when using ABC as the key. $D \rightarrow A$ violates BCNF as D is not part of the key. If you use BCD as the key then you get a lower normal form.

(c) Decompose into BCNF:

Ra (A, D)

Rb (B, C, D)

-1 This decomposition is not dependency preserving, pulling AD out does not preserve ABC. There is no dependency preserving decomposition for this question.

(4) $A \rightarrow B$, $BC \rightarrow D$, $A \rightarrow C$

(a)

$\{A\}^+ = \{A, B, C\}$

$\{B\}^+ = \{B\}$

$\{C\}^+ = \{C\}$

$\{D\}^+ = \{D\}$

$\{BC\}^+ = \{B, C, D\}$

candidate key: $\{A, D\}$ -2 The key is only A

(b) The highest normal form

Check for 1NF: It's in 1NF because it contains only atomic values.

Check for 2NF: It's not in 2NF because it contains partial dependencies. For $\{B\}$, it is functional dependent on $\{A\}$, which is part of the candidate key $\{A, D\}$.

-2 Relation is in 2NF. $BC \rightarrow D$ violates 3NF as D is determined by non-prime attributes B and C

Check for 3NF: It's not in 3NF because it is not in 2NF.

(c) Decompose into BCNF:

Ra (B, C, D)

Rb (A, B)

Rc (A, C)

BCD, ABC is adequate as it does not cause any violations, you don't need to break it down further. (No marks deducted)

(4) $AB \rightarrow C$, $AB \rightarrow D$, $C \rightarrow A$, $D \rightarrow B$

(a)

$\{A\}^+ = \{A\}$

$\{B\}^+ = \{B\}$

$\{C\}^+ = \{C, A\}$

$\{D\}^+ = \{D, B\}$

$\{AB\}^+ = \{A, B, C, D\}$

candidate key: $\{A, B\}$, $\{C, D\}$ -2 Missing two candidate key (AD and BC)

(b) The highest normal form

Check for 1NF: It's in 1NF because it contains only atomic values.

Check for 2NF: It's in 2NF because it contains no partial dependency.

Check for 3NF: It's not in 3NF because it contains transitive dependency.

-2 The highest normal form is 3NF when using AB as the key. $D \rightarrow A$ and $C \rightarrow A$ violated BCNF as D and C are not part of the key.

(c) Decompose into BCNF:

Ra (A, C)

Rb (B, C)

Rc (B, D)

Rd (A, D)

-1 This decomposition is not dependency persevering. There is no dependency persevering decomposition for this question.