# Adding Physical Models to GMAT

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#### Abstract

This document describes the steps needed to add a new PhysicalModel to GMAT. It includes information about populating the orbital A-matrix and the orbital State Transition Matrix. It does not include information about adding new states (e.g. quaternions for attitude dynamics) to the propagation state vector.

# 1 Overview

GMAT's Propagation Subsystem consists of a collection of classes that work together to evolve elements of a mission over time. The base classes for this subsystem are shown in Figure 1. The Propagation subsystem is driven from one of several commands designed to use a propagation configuration. Commands that work with the propagation subsystem are all derived from the PropagationEnabledCommand base class. Those classes all use the interfaces in the PropSetup class and in the Propagator and ODEModel classes to function, so they are not described here. Instead, this document describes the interfaces that are needed in the classes derived from PhysicalModel that the ODEModel depends on to function correctly. This overview is intended to provide background information about the interactions between classes that may help in building new physical models.

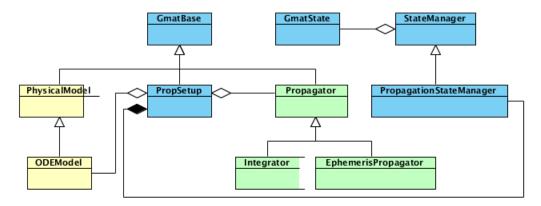


Figure 1: Base Classes of the Propagation Subsystem

The classes shown in Figure 1 play the following roles:

## **GmatState**

This class models a collection of real number data with an associated epoch. It contains a vector of real data, an epoch, a mapping between data elements and other associated elements in the vector, IDs for the data elements, and strings describing each element. GMAT's propagation subsystem constructs

and uses a GmatState object as the core data structure that evolves over time. This object, called the propagation state vector, is designed to be flexible, and to grow or shrink depending on the needs of the mission being modeled.

## PropSetup

The PropSetup class is a container class that collect a PropagationStateManager, Propagator, and optionally an ODEModel into a single object for use by a PropagationEnabledCommand. The PropSetup objects present the publicly visible elements of an instance of a configured propagation configuration. For example, changes to the "Propagator" in the GMAT GUI actually make changes to a PropSetup object.

# Propagator

Propagator is the base class for all of GMAT's evolution operators. The Propagator class defines the interface for advancing a propagation state vector from some initial time  $t_i$  to a final time  $t_f$ . Derived classes implement the specific evolution operator, and hence determine if an ODEModel is required.

# Integrator

Numerical integration is performed in GMAT by a class derived from the Integrator base class. Integrators require an ODEModel to function correctly. The Integrator class is further subclassed into a RungeKutta class, a PredictorCorrector class, and other classes based on the numerical integration algorithm needed.

# **Ephemeris**Propagator

GMAT is designed with the ability to evolve a state vector using analytic methods, either from a set of analytic equations or by interpolating from a data file. The latter case works from interfaces defined in the EphemerisPropagator class. The first case of an ephemeris propagator in GMAT is the SPK propagator.

#### PhysicalModel

PhysicalModel is the base class for objects that provide differential equation data to the Integrator classes. The PhysicalModel class is subclassed to implement a specific set of differential equations that are then called by the numerical integrators. There is one special PhysicalModel class, the ODEModel, which is used to accumulate derivative data for the Integrators. Figure 2 shows the PhysicalModels in GMAT at this writing.

#### **ODEModel**

The ODEModel class implements the accumulation of derivative information required when performing numerical integration. ODEModel objects are containers for collections of PhysicalModels that together define the physics used to evolve a state vector. They apply superposition to the data generated by each member PhysicalModel, add the results together, and report the results to the numerical integrators. They can also optionally generate the A-matrix and the derivative of the state transition matrix for use in other calculations.

## PropagationStateManager

The PropagationStateManager is a helper class that manages the state vector that is propagated in the propagation subsystem. The PropagationStateManager tracks the state members element by element, associations between the elements, and constructs the state vector for use by Propagator and ODEModel objects.

The classes described, and classes derived from them, above comprise the propagation subsystem. The subsystem can be extended on either the Propagator side of the class hierarchy or on the PhysicalModel

side. New integrators and propagators are added to the system to implement new techniques for evolving a propagation state vector. New forces or other derivative models are added by adding subclasses of the PhysicalModel class. The remainder of this document describes the latter operation: extending the derivative models by implementing new PhysicalModel classes.

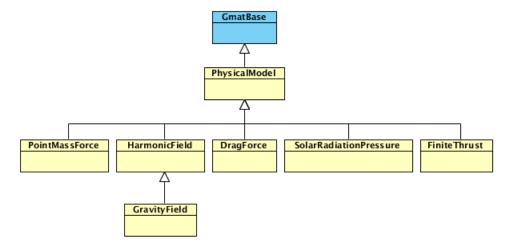


Figure 2: Physical Model Classes

Figure 2 shows the core PhysicalModel classes in GMAT that provide data for specific portions of the physics modeled by Integrators. The next section describes the interfaces that are required in order for a PhysicalModel object to interact with an ODEModel object. Following that section you will find specific instructions for adding the model to GMAT's factory subsystem, and then instructions for adding ancillary objects that are used by a PhysicalModel, using an atmosphere model for the DragForce as an example.

# 2 Creating the Model

The basic approach to adding a force or other derivative model to GMAT starts with designing and coding the class implementing the new model. The steps involved are basically these:

- Create a C++ class for the new model.
- Derive the new class from PhysicalModel (or a class derived from PhysicalModel).
- Implement at a minimum the following methods:
  - The usual four methods: Constructor, Destructor, Copy Constructor and Assignment operator (aka operator=). All GMAT classes that are derived from GmatBase need these methods to work correctly with GMAT's Configuration/Sandbox cloning design.
  - Clone: GmatBase defines this method as an abstract method to be implemented in all leaf classes.
     You'll need to implement it to call your class's copy constructor.
  - Initialize: Use this method to perform the final setup of your model prior to use by an integrator. This method is not strictly required, but is nearly always needed so that the model can adapt to changing state vector sizes and other dynamic propertied that may affect the derivative calculations.
  - SupportsDerivative: This method identifies the supported derivative types for the model. By default, the Gmat::CARTESIAN\_STATE type is supported. Other options include MASS\_FLOW,

ORBIT\_STATE\_TRANSITION\_MATRIX, and the ORBIT\_A\_MATRIX (all defined in the Gmat namespace).

- SetStart: The ODEModel uses this method to set the index for the start and size of supported derivative types.
- IsUserForce: (Optional) This method identifies PhysicalModels incorporated though the plugin interface, or through other means outside of the standard forces managed in GMAT's Interpreter code.
- GetDerivatives: The GetDerivatives method is the method accessed by an ODEModel to build the total state derivative.

The following paragraphs provide additional information about the last four of these methods, and include some stripped down sample code for each.

# 2.1 The SupportsDerivative Method

The SupportsDerivative method has the signature

```
virtual bool SupportsDerivative(Gmat::StateElementId id);
```

The purpose of this method is to identify support for specific derivative components inside of a PhysicalModel. It returns true if the input derivative type is supported, and false if not. Thus the code for the FiniteThrust PhysicalModel, which currently supports derivatives of the Cartesian state and mass depletion but no other derivative data, looks like this:

```
bool FiniteThrust::SupportsDerivative(Gmat::StateElementId id)
{
   if (id == Gmat::CARTESIAN_STATE)
     return true;

if (id == Gmat::MASS_FLOW)
     return true;

return PhysicalModel::SupportsDerivative(id);
}
```

If support is added for the A-matrix, another if test will be added to this method. Otherwise, the ODEModel will simply ignore this model when accumulating A-matrix data for an Integrator.

## 2.2 The SetStart Method

The SetStart method sets the index values for specific derivative data into the propagation state vector. It provides data used by the GetDerivatives method to fill in the data needed for the derivative calculations. The method has the signature

One example of this method is that found in the SolarRadiationPressure model:

```
bool retval = false;
switch (id)
   case Gmat::CARTESIAN_STATE:
                                      // Deprecated!
      satCount = quantity;
      cartesianCount = quantity;
      cartesianStart = index;
      fillCartesian = true;
      retval = true;
      break;
   case Gmat::ORBIT_STATE_TRANSITION_MATRIX:
      stmCount = quantity;
      stmStart = index;
      fillSTM = true;
      retval = true;
      break;
   case Gmat::ORBIT_A_MATRIX:
      aMatrixCount = quantity;
      aMatrixStart = index;
      fillAMatrix = true;
      retval = true;
      break;
   default:
      break;
}
return retval;
```

The propagation state vector is arranged by data type; all of the Cartesian state data is grouped together in one section, mass flow data in another, and so forth. The PhysicalModel class includes data structures to track the size and location of each known type in internal protected variables named typenameCount, typenameStart, and fill Typename, where typename identifies the type of state element in the vector. These data elements are populated in the SetStart method; this method provides the basic starting points for populating the derivative data in the propagation state vector.

## 2.3 The IsUserForce Method

}

Scripting for the ODEModel in GMAT is currently coded so that the core forces are managed in the Interpreter code on a case-by-case basis. The addition of new forces allows for new capabilities in GMAT, but these new cases have to handled differently from the scripting side of the system. Users identify these new, not yet fully interpreted cases by setting the IsUserForce method to return true. The signature for this method is

```
virtual bool IsUserForce();
```

When the implementation returns true – as in the solar sail code from the Plugin repository at SourceForge:

```
bool SolarSailForce::IsUserForce()
{
   return true;
}
```

then the Interpreter identifies the new derivative model from scripting calling out the force from a list of user defined forces:

```
Create ForceModel Prop_ForceModel;
...
GMAT Prop_ForceModel.UserDefined = {SailForce};
```

## 2.4 The GetDerivatives Method

The heart of GMAT's PhysicalModel system is the GetDerivatives method. This method is called repeatedly during propagation – as often as sixteen times per propagation step with the current suite of numerical integrators – so the method must be coded with efficiency in mind in order to enhance GMAT's performance. The method has the signature

where state is a vector of state data managed in the propagator, dt is a time offset from a base epoch, measured in seconds, order determines if the order of the derivative is first or second based on the needs of the Integrator, and id is a flag for the specific type of derivative requested. The last parameter, id, is not used in the current GMAT code.

When the GetDerivatives model is called on a Physical Model, the algorithm for the Physical Model takes the input state and fills in derivative information in an internal data structure named derivs, defined in the Physical Model base class. An overview of this process can be seen in a stripped down version of the Point Mass Force code:

```
// Then fill in the Cartesian state derivatives;
            // left intact for clarity
           if (order == 1)
              // Do dv/dt first, in case deriv = state
              deriv[3 + i6] = relativePosition[0] * mu_r - a_indirect[0];
              deriv[4 + i6] = relativePosition[1] * mu_r - a_indirect[1];
              deriv[5 + i6] = relativePosition[2] * mu_r - a_indirect[2];
               // dr/dt = v, but only fill this piece for the central body
              if (rbb3 == 0.0)
                  deriv[i6]
                               = state[3 + i6];
                  deriv[1 + i6] = state[4 + i6];
                  deriv[2 + i6] = state[5 + i6];
              }
              else
                  deriv[i6] = deriv[1 + i6] = deriv[2 + i6] = 0.0;
            else // Handle 2nd order derivative request
              deriv[ i6 ] = relativePosition[0] * mu_r - a_indirect[0];
              deriv[i6+1] = relativePosition[1] * mu_r - a_indirect[1];
               deriv[i6+2] = relativePosition[2] * mu_r - a_indirect[2];
               deriv[i6+3] = 0.0;
               deriv[i6+4] = 0.0;
              deriv[i6+5] = 0.0;
     }
     if (fillSTM || fillAMatrix)
        Real aTilde[36];
        Integer associate, element;
        Integer aiCount = (fillSTM ? stmCount : aMatrixCount);
        // This part work basically the same, so it's stripped down
        for (Integer i = 0; i < aiCount; ++i)</pre>
           i6 = stmStart + i * 36;
           a6 = aMatrixStart + i * 36;
           if (!fillSTM)
               i6 = a6;
            associate = theState->GetAssociateIndex(i6);
           relativePosition[0] = rv[0] - state[ associate ];
. . .
           // Calculate A-tilde
            // A = D = 0
```

```
aTilde[0] = aTilde[1] = aTilde[2] =
            aTilde[6] = aTilde[7] = aTilde[8] =
            aTilde[12] = aTilde[13] = aTilde[14] =
            aTilde[21] = aTilde[22] = aTilde[23] =
            aTilde[27] = aTilde[28] = aTilde[29] =
            aTilde[33] = aTilde[34] = aTilde[35] = 0.0;
            // B = I is set in the ODE Model
            aTilde[3] = aTilde[10] = aTilde[17] =
            aTilde[4] = aTilde[5] = aTilde[9] =
            aTilde[11] = aTilde[15] = aTilde[16] = 0.0;
            // Math spec, equ 6.69, broken into separate pieces
            aTilde[18] = - mu_r + 3.0 * mu_r / (radius*radius) *
                             relativePosition[0] * relativePosition[0];
            // etc for the other components
            for (Integer j = 0; j < 6; ++j)
               for (Integer k = 0; k < 6; ++k)
                  element = j * 6 + k;
                  if (fillSTM)
                     deriv[i6+element] = aTilde[element];
                  if (fillAMatrix)
                     deriv[a6 + element] = aTilde[element];
               }
            }
         }
      }
   }
   return true;
}
```

(Please refer to the SourceForge trunk code for the full implementation.) There are several pieces worth noting here. The derivative data is filled in type by type in this code: Cartesian state data, followed by the STM and A-matrix data. The base epoch is accessed from the base State vector in the PhysicalModel, and the time offset added to it for places where an epoch is needed (for the PointMassForce, the epoch is used when finding the location of the point mass with respect to the central body of the force). Indexing into the propagation state vector is performed based on the values of the typenameStart variable, and filled in for the typenameCount number of instances of the specified type. Finally, note that the A-matrix and STM portions of the code access the mapping to the associated Cartesian state data. This is performed through a call to GetAssociateIndex:

```
associate = theState->GetAssociateIndex(i6);
```

This call ensures that the A-matrix or STM contribution being references uses the correct Cartesian state data for the model.

Once the code is ready for incorporation into GMAT, the class is added to the appropriate factory for the model and built into the system. The next section describes this process.

- 3 Adding the Model to GMAT
- 3.1 Adding to an existing Factory system

3.2 Adding as a Plugin

4 Helper Classes: Adding an AtmosphereModel