

MATH 101 Midterm Exam 1

Date: 08 February, 2024

Duration: 45 minutes

- The test consists of 8 pages and 3 questions, worth a total of 18 marks.
- This is a closed-book examination. **None of the following are allowed:** documents, formula sheets, electronic devices of any kind (including calculators, cell phones, etc.).
- No work on this page will be marked.
- Fill in the information below before turning to the questions.

Student number								
Section								
Name							
Signature								

Rules governing UBC examinations:

1. Each candidate must be prepared to produce, upon request, a UBC card for identification.
2. No candidate shall be permitted to enter the examination room after the expiration of one-half hour from the scheduled starting time, or to leave during the first half hour of the examination.
3. Candidates suspected of any of the following, or similar, dishonest practices shall be immediately dismissed from the examination and shall be liable to disciplinary action:
 - (a) Having at the place of writing any books, papers or memoranda, calculators, computers, sound or image players/recorders/transmitters (including telephones), or other memory aid devices, other than those authorized by the examiners;
 - (b) Speaking or communicating with other candidates;
 - (c) Purposely exposing written papers to the view of other candidates or imaging devices. The plea of accident or forgetfulness shall not be received.
4. Candidates must not destroy or mutilate any examination material; must hand in all examination papers; and must not take any examination material from the examination room without permission of the invigilator.
5. Candidates must follow any additional examination rules or directions communicated by the instructor or invigilator.

Additional rules governing this examination:

1. This is a closed-book exam.
 - (a) Calculators and other calculating devices may not be used.
 - (b) Notes may not be used.
 - (c) Watches must be removed and taken off the table.
 - (d) Phones must be turned off and stored in an inaccessible location (like inside a backpack).
2. If an answer box is provided, you must write down your answer (but not its justification) in the box.
3. Simplification is an important skill to demonstrate. Answers must be simplified and calculator-ready. For example, write $\log(e^{\sqrt{2}}) = \sqrt{2}$, but do not write $\sqrt{2} \approx 1.414$. Any answer of the form “trig (arctrig)” (for example: $\sin(\arctan x)$) is incomplete and will not receive full marks.
4. You must justify your answers unless an explicit exception is made.
5. You may use any result proven in class or on assignments.
6. You may not discuss this exam with anyone who has not yet taken their version of it.

1. (6 points) ★★☆☆ Compute $\int_1^e \frac{1}{x(1 + (\log x)^2)} dx$. Remember to simplify your final answer.

Use this page to continue your work on Question 1.

2. (6 points) ★★★☆ Set $e^x = 3 \sec^2 \theta$ to evaluate

$$\int \sqrt{e^x - 3} \, dx .$$

Use this page to continue your work on Question 2.

3. (6 points) ★★★☆ Snow is accumulating on the ground at a rate of $s(x)$ centimetres per hour, at time x (where x is measured in hours), $0 \leq x \leq 14$.

Snow that has been on the ground for at least two hours is turned into ice.

- (a) Write down an integral whose value equals the depth of snow at time t , where $2 \leq t \leq 14$. Make sure to use proper notation, and *exclude* snow that has turned into ice.

- (b) For this part, suppose $s(x) = \log\left(1 + 2x - \frac{x^2}{7}\right)$.

You like to play in deep snow. At what time from $t = 2$ to $t = 14$ is the amount of non-ice snow on the ground maximum?

For this question you may assume, without proof, that the absolute maximum of the function in part (a) over the interval $[2, 14]$ occurs at an interior point (not an endpoint).

Use this page to continue your work on Question 3.