

# MATH 101 Midterm Exam 1

**Date: 12 February, 2024**

**Duration: 45 minutes**

- The test consists of 8 pages and 3 questions, worth a total of 18 marks.
- This is a closed-book examination. **None of the following are allowed:** documents, formula sheets, electronic devices of any kind (including calculators, cell phones, etc.).
- No work on this page will be marked.
- Fill in the information below before turning to the questions.

Student number								
Section								
Name	.....							
Signature								

## Rules governing UBC examinations:

1. Each candidate must be prepared to produce, upon request, a UBC card for identification.
2. No candidate shall be permitted to enter the examination room after the expiration of one-half hour from the scheduled starting time, or to leave during the first half hour of the examination.
3. Candidates suspected of any of the following, or similar, dishonest practices shall be immediately dismissed from the examination and shall be liable to disciplinary action:
  - (a) Having at the place of writing any books, papers or memoranda, calculators, computers, sound or image players/recorders/transmitters (including telephones), or other memory aid devices, other than those authorized by the examiners;
  - (b) Speaking or communicating with other candidates;
  - (c) Purposely exposing written papers to the view of other candidates or imaging devices. The plea of accident or forgetfulness shall not be received.
4. Candidates must not destroy or mutilate any examination material; must hand in all examination papers; and must not take any examination material from the examination room without permission of the invigilator.
5. Candidates must follow any additional examination rules or directions communicated by the instructor or invigilator.

## Additional rules governing this examination:

1. This is a closed-book exam.
  - (a) Calculators and other calculating devices may not be used.
  - (b) Notes may not be used.
  - (c) Watches must be removed and taken off the table.
  - (d) Phones must be turned off and stored in an inaccessible location (like inside a backpack).
2. If an answer box is provided, you must write down your answer (but not its justification) in the box.
3. Simplification is an important skill to demonstrate. Answers must be simplified and calculator-ready. For example, write  $\log(e^{\sqrt{2}}) = \sqrt{2}$ , but do not write  $\sqrt{2} \approx 1.414$ . Any answer of the form “trig (arctrig)” (for example:  $\sin(\arctan x)$ ) is incomplete and will not receive full marks.
4. You must justify your answers unless an explicit exception is made.
5. You may use any result proven in class or on assignments.
6. You may not discuss this exam with anyone who has not yet taken their version of it.

1. (6 points) ★★☆☆ Compute

$$\int \frac{e^{-x} \log(e^{-x} + 1)}{e^{-x} + 1} dx.$$

*Use this page to continue your work on Question 1.*

2. (6 points) ★★★☆ Evaluate  $\int \frac{e^{2x} + 5}{e^{2x} + e^{-2x}} dx$ .

*Use this page to continue your work on Question 2.*

3. (6 points) ★★★☆ On a busy shopping day, the global financial network handles millions of transactions. Let  $t$  denote time in hours, starting at midnight, so that  $0 \leq t \leq 24$  covers the whole day. Suppose the rate at which money passes through one node in the network, in units of M\$/hr, is  $f(t) = 6 + \pi(\cos(\pi t/12))^3$ . (Here M stands for “mega” as usual, so 1 M\$ equals  $10^6$ \$.)
- (a) Write an integral expression for the total amount of money processed at the node of interest over the full 24-hour day. (Just write the integral: don’t evaluate it.)
- (b) Calculate the total amount of money processed over the 6-hour period from 12:00–18:00.

*Use this page to continue your work on Question 3.*