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QHack

Quantum Coding Challenges

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Ctrl-Z

100 points

Backstory

Zenda and Reece work at Trine's Designs, a startup run by the eccentric inventor Doc Trine. Trine promises to tell Zenda and Reece about a revolutionary new type of quantum resource she has invented called "*timbits*". Before explaining timbits, she insists on demonstrating [Bennett's Laws of Infodynamics](#), governing the behaviour of quantum information. "*Only then,*" she says, "*will the power of timbits be revealed in their full glory.*"

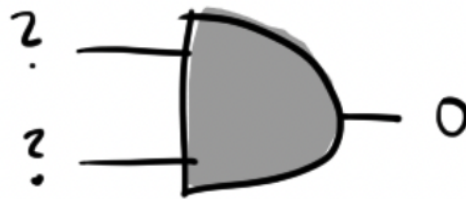
Reversible computation

► Laws of Infodynamics Part I: The First Law

Some classical logical operations are *irreversible*. For instance,

$$\text{AND}(0, 0) = \text{AND}(0, 1) = \text{AND}(1, 0) = 0,$$

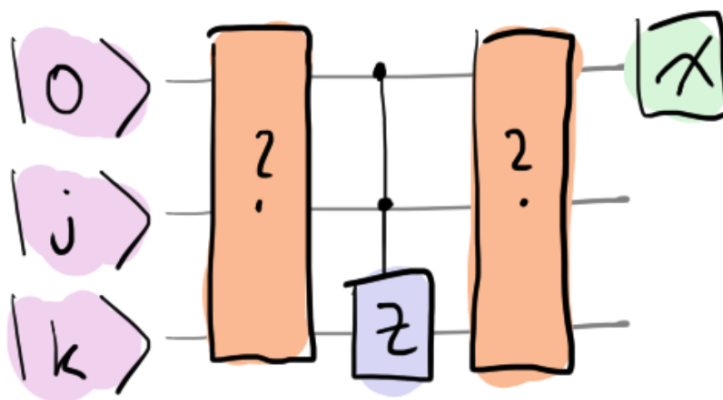
so given that $\text{AND}(j, k) = 0$, we can't tell the values of j and k .



Put differently, there is no way to press `ctrl-Z` and learn what went in! In contrast, quantum circuits are built out of unitary gates, which are always reversible. We can always press `ctrl-Z`! How can we encode something irreversible, like an AND gate, into a quantum circuit? Aptly, the answer is a controlled Z gate! It encodes the classical operation into a *phase*:

$$CZ|j, k\rangle \mapsto (-1)^{\text{AND}(j,k)}|j, k\rangle.$$

A phase by itself is unobservable, so we need to interfere this state with some others to detect it. A simple way to do this is to use a *controlled* controlled Z gate, with some extra operations on either side:



Your job: figure out which operations to apply so that measurement on the first qubit is guaranteed to be in state $|\text{AND}(j, k)\rangle$.

Challenge code

In the code below, you are given a function called `AND(j, k)`. **You must complete this circuit** and provide gates which implement a classical AND gate. More precisely, if the second and third qubits are in states $|j\rangle$ and $|k\rangle$, the circuit should place the first qubit in state $|\text{AND}(j, k)\rangle$.

Inputs

As input to this problem, you are given two bits `j (int)` and `k (int)`, encoded onto the second and third qubits for you.

Output

Your circuit must place the first qubit in basis state `AND(j, k)`. This will be checked using `qml.probs(wires = 0)`, which gives `[1, 0]` for $|0\rangle$ and `[0, 1]` for $|1\rangle$.

If your solution matches the correct one within the given tolerance specified in `check` (in this case it's a `1e-4` relative error tolerance), the output will be `"Correct!"` Otherwise, you will receive a `"Wrong answer"` prompt.

Code

? Help

```
1 import json
2 import pennylane as qml
3 import pennylane.numpy as np

4 dev = qml.device("default.qubit", wires=3)
5
6 @qml.qnode(dev)
7 def AND(j, k):
8     """Implements the AND gate using quantum gates and computes
9
10     Args:
11         j (int): A classical bit, either 0 or 1.
12         k (int): A classical bit, either 0 or 1.
13
14     Returns:
15         float: The probabilities of measurement on wire 0.
16     """
17
18     if j == 1:
19         qml.PauliX(wires=1)
20     if k == 1:
21         qml.PauliX(wires=2)
22
```

```
23     # Put your code here #
```

```
24
```

```
25     qml.ctrl(qml.PauliZ, control=[0, 1])(wires = [2])
```

```
26
```

```
27
```

```
28     # Your code here #
```

```
29
```

```
30     return qml.probs(wires=0)
```

```
31
```

```
32     # These functions are responsible for testing the solution.
```

```
33     def run(test_case_input: str) -> str:
```

```
34         j, k = json.loads(test_case_input)
```

```
35         output = AND(j, k).tolist()
```

```
36
```

```
37         return str(output)
```

```
38
```

```
39     def check(solution_output: str, expected_output: str) -> None:
```

```
40         solution_output = json.loads(solution_output)
```

```
41         expected_output = json.loads(expected_output)
```

```
42         assert np.allclose(solution_output, expected_output, rtol=1e
```

```
43
```

```
44     test_cases = [['[0, 0]', '[1, 0]'], ['[1, 1]', '[0, 1]']]
```

```
45     for i, (input_, expected_output) in enumerate(test_cases):
```

```
46         print(f"Running test case {i} with input '{input_}'...")
```

```
47
```

```
48     try:
```

```
49         output = run(input_)
```

```
50
```

```
51     except Exception as exc:
```

```
52         print(f"Runtime Error. {exc}")
```

```
53
```

```
54     else:
```

```
55         if message := check(output, expected_output):
```

```
56             print(f"Wrong Answer. Have: '{output}'. Want: '{expe
```

```
57
```

```
58         else:
```

```
59             print("Correct!")
```

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