

Ende

$$\int_1^2 \frac{\Delta x}{2} \left[(4 - (1)^2) + 2(4 - (1.125)^2) + 2(4 - (1.25)^2) + 2(4 - (1.375)^2) + 2(4 - (1.5)^2) + 2(4 - (1.625)^2) + 2(4 - (1.75)^2) + (4 - (1.875)^2) \right]$$

$$\frac{1}{16} [21.664]$$

Simpson

$$\frac{1}{24} \left[(4 - (1)^2) \cdot 4(4 - (1.125)^2) + 2(4 - (1.25)^2) + 4(4 - (1.375)^2) + 2(4 - (1.5)^2) + 4(4 - (1.625)^2) + 2(4 - (1.75)^2) + (4 - (1.875)^2) \right] = 1.653$$

2)

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \left[\left(\frac{4i}{n} - 1 \right)^2 + 2 \left(\frac{4i}{n} - 1 \right) + 3 \right] \frac{4}{n}$$

$$\frac{16i^2}{n^2} - \frac{8i}{n} + 14\frac{8i}{n} - 2 + 3$$

$$\lim_{n \rightarrow \infty} \left[\frac{4}{n} \sum_{i=1}^n \left(\frac{16i^2}{n^2} + 2 \right) \right]$$

$$\lim_{n \rightarrow \infty} \frac{4}{n} \left[\sum_{i=1}^n \frac{16i^2}{n^2} + \sum_{i=1}^n 2 \right] = \lim_{n \rightarrow \infty} \frac{4}{n} \cdot \left[\frac{16}{n^2} \sum_{i=1}^n i^2 + 2n \right]$$