Paper Title: Joint Transmit Waveform and Reflection Design for RIS-Assisted MIMO Radar Systems

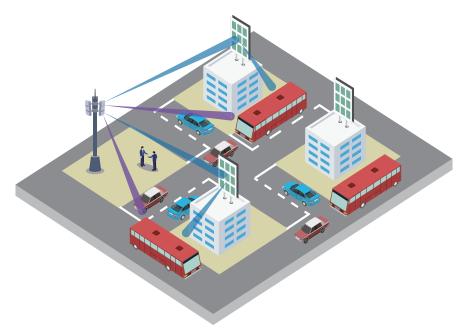


Fig. R1: An application scenario of RIS-assisted MIMO radar.

The expressions of $\mathbf{D}_{t,p}$, $\mathbf{d}_{t,p}$, and $c_{t,p}$ in (11b) can be easily calculated based on (7) and (10).

$$\mathbf{D}_{t,p} = \sum_{i=1,i\neq t}^{T} \sigma^{2} \widetilde{\mathcal{F}}_{i}^{H}(\boldsymbol{\phi}_{i}) \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^{H} \mathbf{M}_{t,p}^{-1} \widetilde{\mathcal{F}}_{i}(\boldsymbol{\phi}_{i}) + \sum_{t=1}^{T} \sum_{q=1}^{Q} \varsigma^{2} \widetilde{\mathcal{F}}_{t,q}^{H}(\boldsymbol{\phi}_{t}) \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^{H} \mathbf{M}_{t,p}^{-1} \widetilde{\mathcal{F}}_{t,q}(\boldsymbol{\phi}_{t}),$$
(R1a)

$$\mathbf{d}_{t,p}^{H} = -2\mathbf{s}_{t,p}^{H}\mathbf{M}_{t,p}^{-1}\widetilde{\mathcal{F}}_{t}(\boldsymbol{\phi}_{t}),\tag{R1b}$$

$$c_{t,p} = \sigma_z^2 \mathbf{s}_{t,p}^H \mathbf{M}_{t,p}^{-1} \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p}. \tag{R1c}$$

Substituting (15) into (10), the expressions of $\mathbf{F}_{t,p}$, $\mathbf{G}_{t,p}$, $\mathbf{L}_{t,p}$, $\mathbf{f}_{t,p}$, $\mathbf{g}_{t,p}$, and $\widehat{c}_{t,p}$ can be calculated as

$$\mathbf{F}_{t,p} = \sum_{i=1, i \neq t}^{T} \sigma^2 \mathbf{C}_i^H \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^H \mathbf{M}_{t,p}^{-1} \mathbf{C}_i + \sum_{t=1}^{T} \sum_{q=1}^{Q} \varsigma^2 \mathbf{C}_{t,q}^H \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^H \mathbf{M}_{t,p}^{-1} \mathbf{C}_{t,q},$$
(R2a)

$$\mathbf{G}_{t,p} = \sum_{i=1,i\neq t}^{T} \sigma^2 \mathbf{E}_i^H \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^H \mathbf{M}_{t,p}^{-1} \mathbf{E}_i + \sum_{t=1}^{T} \sum_{q=1}^{Q} \varsigma^2 \mathbf{E}_{t,q}^H \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^H \mathbf{M}_{t,p}^{-1} \mathbf{E}_{t,q},$$
(R2b)

$$\mathbf{L}_{t,p} = 2 \sum_{i=1, i \neq t}^{T} \sigma^{2} \mathbf{E}_{i}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{C}_{i} + 2 \sum_{t=1}^{T} \sum_{q=1}^{Q} \varsigma^{2} \mathbf{E}_{t,q}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{C}_{t,q},$$
(R2c)

$$\mathbf{f}_{t,p}^{H} = 2\sum_{i=1,i\neq t}^{T} \sigma^{2} \mathbf{a}_{i}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{C}_{i} + 2\sum_{t=1}^{T} \sum_{q=1}^{Q} \varsigma^{2} \mathbf{a}_{t,q}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{C}_{t,q} - 2\mathbf{s}_{t,p}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{C}_{t},$$
(R2d)
$$\mathbf{g}_{t,p}^{H} = 2\sum_{i=1,i\neq t}^{T} \sigma^{2} \mathbf{a}_{i}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{E}_{i} + 2\sum_{t=1}^{T} \sum_{q=1}^{Q} \varsigma^{2} \mathbf{a}_{t,q}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{E}_{t,q} - 2\mathbf{s}_{t,p}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{E}_{t},$$
(R2e)
$$\widehat{c}_{t,p} = \sum_{i=1,i\neq t}^{T} \sigma^{2} \mathbf{a}_{i}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{a}_{i} + \sum_{t=1}^{T} \sum_{q=1}^{Q} \varsigma^{2} \mathbf{a}_{t,q}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{s}_{t,p} \mathbf{s}_{t,p}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{a}_{t,q} - 2\Re{\{\mathbf{s}_{t,p}^{H} \mathbf{M}_{t,p}^{-1} \mathbf{a}_{t}\}} + c_{t,p}.$$