

Prime Number of Set Bits in Binary Representation

Given two integers L and R , find the count of numbers in the range $[L, R]$ (inclusive) having a prime number of set bits in their binary representation.

(Recall that the number of set bits an integer has is the number of 1s present when written in binary. For example, 21 written in binary is 10101 which has 3 set bits. Also, 1 is not a prime.)

Example 1:

Input: $L = 6, R = 10$

Output: 4

Explanation:

6 \rightarrow 110 (2 set bits, 2 is prime)

7 \rightarrow 111 (3 set bits, 3 is prime)

9 \rightarrow 1001 (2 set bits, 2 is prime)

10 \rightarrow 1010 (2 set bits, 2 is prime)

Example 2:

Input: $L = 10, R = 15$

Output: 5

Explanation:

10 \rightarrow 1010 (2 set bits, 2 is prime)

11 \rightarrow 1011 (3 set bits, 3 is prime)

12 \rightarrow 1100 (2 set bits, 2 is prime)

13 \rightarrow 1101 (3 set bits, 3 is prime)

14 \rightarrow 1110 (3 set bits, 3 is prime)

15 \rightarrow 1111 (4 set bits, 4 is not prime)

Note:

1. L, R will be integers $L \leq R$ in the range $[1, 10^6]$.
2. $R - L$ will be at most 10000.

Solution 1

Java

```
class Solution {
    public int countPrimeSetBits(int l, int r) {
        Set<Integer> primes = new HashSet<>(Arrays.asList(2, 3, 5, 7, 11, 13, 17, 19, 23, 29));
        int cnt = 0;
        for (int i = l; i <= r; i++) {
            int bits = 0;
            for (int n = i; n > 0; n >>= 1)
                bits += n & 1;
            cnt += primes.contains(bits) ? 1 : 0;
        }
        return cnt;
    }
}
```

C++

```
class Solution {
public:
    int countPrimeSetBits(int l, int r) {
        set<int> primes = { 2, 3, 5, 7, 11, 13, 17, 19, 23, 29 };
        int cnt = 0;
        for (int i = l; i <= r; i++) {
            int bits = 0;
            for (int n = i; n; n >>= 1)
                bits += n & 1;
            cnt += primes.count(bits);
        }
        return cnt;
    }
};
```

written by [alexander](#) original link [here](#)

Solution 2

```
class Solution {
    public int countPrimeSetBits(int L, int R) {
        int cnt = 0;
        Set<Integer> listPrimes = new HashSet<>(Arrays.asList(2, 3, 5, 7, 11, 13, 17, 19, 23, 29));
        int[] res = countBits(R);
        for(int i=L; i<=R; i++){
            if(listPrimes.contains(res[i])){
                cnt++;
            }
        }
        return cnt;
    }

    public int[] countBits(int num) {
        if(num == 0)
            return new int[1];
        int[] dp = new int[num+1];

        dp[0] = 0;
        dp[1] = 1;

        for(int i=2; i<=num; i++){
            dp[i] = dp[i >> 1] + dp[i & 1]; // i >> 1 is i / 2 and i & 1 is i % 2
        }
        return dp;
    }
}
```

written by [ashish53v](#) original link [here](#)

Solution 3

Ruby:

```
def count_prime_set_bits(l, r)
  (l..r).sum { |i| 665772 >> i.digits(2).sum & 1 }
end
```

Python:

```
def countPrimeSetBits(self, L, R):
    return sum(665772 >> bin(i).count('1') & 1 for i in range(L, R+1))
```

Java stream:

```
public int countPrimeSetBits(int L, int R) {
    return IntStream.range(L, R+1).map(i -> 665772 >> Integer.bitCount(i) & 1).sum()
;
}
```

Java:

```
public int countPrimeSetBits(int L, int R) {
    int count = 0;
    while (L <= R)
        count += 665772 >> Integer.bitCount(L++) & 1;
    return count;
}
```

C++:

```
int countPrimeSetBits(int L, int R) {
    int count = 0;
    while (L <= R)
        count += 665772 >> __builtin_popcount(L++) & 1;
    return count;
}
```

written by [StefanPochmann](#) original link [here](#)

From [Leetcode](#).