

Smallest Rotation with Highest Score

Given an array A , we may rotate it by a non-negative integer K so that the array becomes $A[K], A[K+1], A[K+2], \dots, A[A.length - 1], A[0], A[1], \dots, A[K-1]$. Afterward, any entries that are less than or equal to their index are worth 1 point.

For example, if we have $[2, 4, 1, 3, 0]$, and we rotate by $K = 2$, it becomes $[1, 3, 0, 2, 4]$. This is worth 3 points because $1 > 0$ [no points], $3 > 1$ [no points], $0 \leq 2$ [one point], $2 \leq 3$ [one point], $4 \leq 4$ [one point].

Over all possible rotations, return the rotation index K that corresponds to the highest score we could receive. If there are multiple answers, return the smallest such index K .

Example 1:

Input: $[2, 3, 1, 4, 0]$

Output: 3

Explanation:

Scores for each K are listed below:

$K = 0$,	$A = [2, 3, 1, 4, 0]$,	score 1
$K = 1$,	$A = [3, 1, 4, 0, 2]$,	score 3
$K = 2$,	$A = [1, 4, 0, 2, 3]$,	score 3
$K = 3$,	$A = [4, 0, 2, 3, 1]$,	score 4
$K = 4$,	$A = [0, 2, 3, 1, 4]$,	score 3

So we should choose $K = 3$, which has the highest score.

Example 2:

Input: $[1, 3, 0, 2, 4]$

Output: 0

Explanation: A will always have 3 points no matter how it shifts. So we will choose the smallest K , which is 0.

Note:

- A will have length at most 20000.
- $A[i]$ will be in the range $[0, A.length]$.

Solution 1

F*ck the examples.

written by [xmeng525](#) original link [here](#)

Solution 2

Key point

Don't calculate the score for $K=0$, we don't need it at all.

(I see almost all other solutions did)

The key point is to find out how score changes when $K++$

Time complexity:

"A will have length at most 20000."

I think it means you should find a $O(N)$ solution.

Explanation:

1. Search the index where score changes and record the chngement to a list.
2. A simple for loop to calculate the score for every K value.
3. Find the index of best score.

What value of K changes score?

a) get point

Each time when we rotate, we make index 0 to index $N-1$, then we get one more point.

b) loss point

$(i - A[i] + N) \% N$ is the value of K making $A[i]$'s index just equal to $A[i]$.

For example, If $A[6] = 1$, then $K = (6 - A[6]) \% 6 = 5$ making $A[6]$ to index 1 of new array.

So when $K=5$, we get this point for $A[6]$

Then if K is bigger when $K = (i - A[i] + 1) \% N$, we start to lose this point, making our score $-- 1$

All I have done is record the value of K for all $A[i]$ where we will lose points.

c) $A[i]=0$

Rotation makes no change for it, because we always have $0 \leq \text{index}$.

However, it is covered in a) and b)

C++:

```
int bestRotation(vector<int>& A) {
    int N = A.size();
    int change[N] = {0};
    for (int i = 0; i < N; ++i) change[(i - A[i] + 1 + N) % N] -= 1;
    for (int i = 1; i < N; ++i) change[i] += change[i - 1] + 1;
    return distance(change, max_element(change, change + N));
}
```

Java

```

public int bestRotation(int[] A) {
    int N = A.length;
    int change[] = new int[N];
    for (int i = 0; i < N; ++i) change[(i - A[i] + 1 + N) % N] -= 1;
    int max_i = 0;
    for (int i = 1; i < N; ++i) {
        change[i] += change[i - 1] + 1;
        max_i = change[i] > change[max_i] ? i : max_i;
    }
    return max_i;
}

```

Python

```

def bestRotation(self, A):
    N = len(A)
    change = [1] * N
    for i in range(N): change[(i - A[i] + 1) % N] -= 1
    for i in range(1, N): change[i] += change[i - 1]
    return change.index(max(change))

```

written by [lee215](#) original link [here](#)

Solution 3

```
class Solution {
    public int bestRotation(int[] A) {
        int len = A.length;

        // Store scores for each K value
        int[] kScores = new int[len];

        for (int i = 0; i < len; i++) {
            int v = A[i];
            // Ideal K is the K that puts A[i] in location i.
            int idealK = (len - v + i) % len;
            // Increment kScores for all possible K's s.t. v in A rotated by K will
            // improve the score.
            for (int j = 0; j < len - v; j++) {
                kScores[idealK] = kScores[idealK] + 1;
                idealK--;
                if (idealK < 0) idealK = len - 1;
            }
        }

        // Get the best K
        int bestK = 0;
        int bestScore = -1;
        for (int k = 0; k < len; k++) {
            int score = kScores[k];
            if (score > bestScore) {
                bestK = k;
                bestScore = score;
            }
        }

        return bestK;
    }
}
```

written by [JLeperez2](#) original link [here](#)

From [Leetcode](#).