

⇒ write an algorithm and a program
to solve 8-puzzle game.

→ Algorithm to find manhattan distance.

Step 1: A 2D array to represent the current state of the puzzle. (3×3)

A 2D array to represent the goal state of the puzzle (3×3).

goal state =

| | | |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | |

$$= [(1, 2, 3), (4, 5, 6), (7, 8, -)]$$

$$\text{possible moves} = [(-1, 0), (1, 0), (0, -1), (0, 1)].$$

Step 2:

```

def manhattan(state):
    for i in range(3):
        for j in range(3):
            if (state[i][j] != '-'):
                goal_i, goal_j = divmod(
                    state[i][j] - 1, 3)
                distance += abs(i - goal_i) +
                           abs(j - goal_j)
    end if
end for
end for.
return distance.

```

step 3: checking for the goal state in current state (if `current state == goal state`)
def check(state):
 return `goal state == current state`.

⇒ DFS Algorithm.

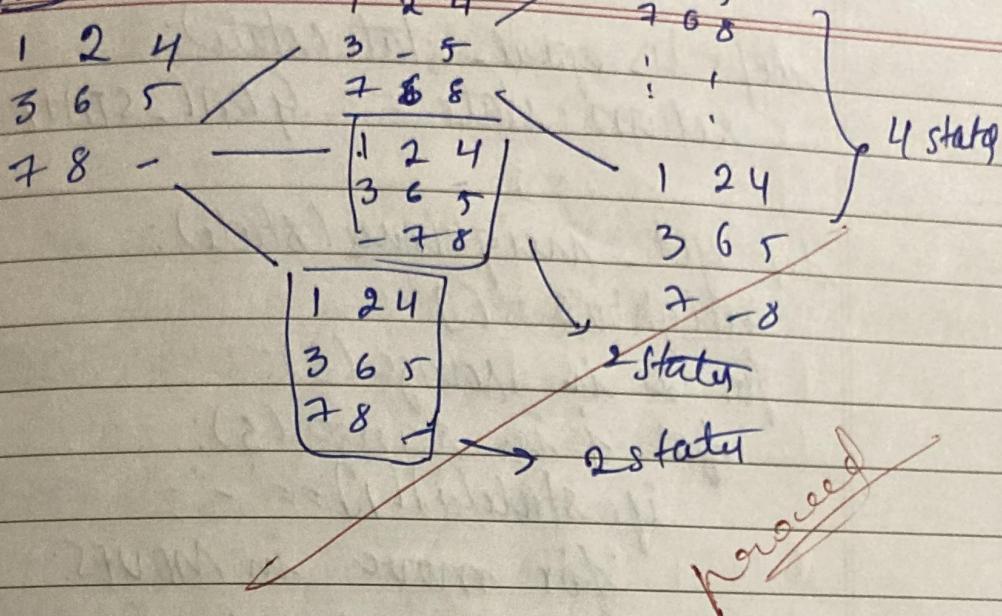
Step 4:

def neighbours(state):
 → Loop over the matrix from i to 3 + j to s
 → where if `state[i][j] = '-'` →
 then check all the four directions
 → using the move matrix, we can do this
 → add those to a new array.
 → Return the neighbours array.

Step 5: DFS.

→ declare a queue
→ visited array to mark visited positions
→ loop it until the queue is empty
→ check if the current state is the goal state.
→ skip already visited state using visited array.
→ if not visited - add to the visited array
→ Again, get the neighbours
→ if no neighbours → none.
→ end.

Trace:



→ code implementation:

from collections import deque

GOAL-STATE = [[1, 2, 3],
[4, 5, 6],
[7, 8, '-']]

MOVES = [(-1, 0), # UP
(1, 0), # down
(0, -1), # Left
(0, 1)] # Right .

def manhattan_distance(state):

distance = 0

for i in range(3):

for j in range(3):

if state[i][j] != '-':

goal_i, goal_j = divmod(state[i][j]) - 1, 3

distance += abs(i - goal_i) + abs(j - goal_j)

return distance .

```
def is_goal_state(state):
    return state == GOAL_STATE
```

```
def get_neighbours(state):
```

```
    neighbors = []
```

```
    for i in range(3):
```

```
        for j in range(3):
```

```
            if state[i][j] == '-':
```

```
                for move in MOVES:
```

```
                    new_i, new_j = i + move[0], j + move[1]
```

```
                    if 0 <= new_i < 3 and 0 <= new_j < 3:
```

```
                        new_state = [row[:] for row in state]
```

```
                        new_state[i][j], new_state
```

```
[new_i][new_j] = new_state[new_i][new_j],
```

```
new_state[i][j]]
```

```
return neighbors.append(new_state)
```

```
def dfs(state):
```

```
    queue = deque([(state, [])])
```

```
    visited = set()
```

```
while queue:
```

```
    current_state, path = queue.popleft()
```

```
    if is_goal_state(current_state):
```

```
        return path
```

```
    if tuple(map(tuple, current_state)) in visited:
```

```
        continue
```

visited.add(tuple(map(tuple, current_state)))

for neighbor in get_neighbors(current_state):
 queue.append((neighbor, path + [neighbor]))
 return None.

initial_state = [[4, 1, 3],
 [7, 2, 6],
 [5, 8, '-']]

path = dfs(initial_state)

if path:

print("solution found: ")

for state in path:

for row in state:

print(row)

print()

else:

print("No solution found.")

output:

Solution found:

[4, 1, 3]

[7, 2, 6]

[5, 8, '-']

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P.K.J.

$[4, 1, 3]$ $[7, 2, 6]$ $[5, \downarrow, 8]$ \downarrow $[4, 1, 3]$ $[7, 2, 6]$ $[\downarrow, 5, 8]$ \downarrow $[4, 1, 3]$ $[\downarrow, 2, 6]$ $[7, 5, 8]$ \downarrow $[\downarrow, 1, 3]$ $[4, 2, 6]$ $[7, 5, 8]$ \downarrow $[1, \downarrow, 3]$ $[4, 2, 6]$ $[7, 5, 8]$ \downarrow $[1, 2, 3]$ $[4, \downarrow, 6]$ $[7, 5, 8]$ \downarrow $[1, 2, 3]$ $[4, 5, 6]$ $[7, \downarrow, 8]$  $[1, 2, 3]$ $[4, 5, 6]$ $[7, 8, \downarrow]$

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