Issues for the Next Generation of Galaxy Surveys
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Issues for the next generation of galaxy surveys

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The weight of the evidence is that the mean mass density (excluding a cosmological constant or its equivalent) is less than the critical Einstein–de Sitter value. This result, if confirmed, is notable because so many of us believed the Einstein–de Sitter model is the elegant and sensible choice. It may offer a cautionary lesson: perhaps our search for a theory of structure formation should broaden the range of models under discussion, in case our first guesses disagree with Nature's choice. To that end I describe an isocurvature model that offers a viable and arguably attractive picture for the early assembly of galaxies that trace mass. Surveys in progress will be capable of distinguishing between this model and the commonly studied adiabatic cold dark matter theory, and may convincingly establish the nature of the initial conditions out of which the galaxies grew.

**Keywords: cosmological tests; biasing; galaxy formation;
thermal background radiation**

1. Standard models and paradigms

In cosmology we attempt to draw large conclusions from limited and often ambiguous data. I am impressed at how well the enterprise is succeeding, to the point that we have an established standard model for the hot, expanding universe (Peebles *et al.* 1991). Which elements to include in the standard model is a matter for ongoing debate, of course. I am inclined to take a conservative line if only to avoid giving misleading impressions to our colleagues with deconstructionist tendencies. For example, the adiabatic cold dark matter model for structure formation has been more successful than I expected, and as a result is rightly the model most commonly used in studies of how structure might have formed. Simon White calls this model a paradigm, which I take to mean a pattern many find useful and convenient in their research. I like this use of the term, provided we agree to distinguish it from a well-established standard model.† I think we cannot count the adiabatic cold mark matter paradigm as part of the standard model for cosmology because, as argued here, there is a viable and perhaps even more attractive alternative.

I organize this discussion around the issues of the weight of the evidence on whether galaxies are good tracers of mass, what we are learning from the cosmological tests, and what one might look for in a model for structure formation on the scale of galaxies and larger. I begin with another question, whether Einstein's introduction of the cosmological principle set a good example for research in our field. The hurried reader will find the main points summarized in § 6.

† In Kuhn's (1970) picture 'normal science' is done within the framework of a paradigm. I hope we can agree that those of us who study models for structure formation outside the set of ideas in the adiabatic cold dark matter paradigm are not necessarily doing abnormal science.

2. The cosmological and biasing principles

The tension between caution and adventure in the advance of science is well illustrated by the histories of these two principles.

Einstein (1917) introduced modern cosmology with his application of general relativity theory to a universe that is spatially homogeneous on average (that is, a stationary random process). Milne gave the homogeneity assumption its name, Einstein's cosmological principle. It is difficult to find in the published literature evidence that Einstein was aware of the observational situation on the distribution of matter. Astronomers had established that we live in a bounded island universe of stars, and some had speculated that the spiral nebulae are other island universes. de Sitter (1917) was willing to consider the possibility that the nebulae are uniformly distributed in the large-scale mean, and that their mass constitutes Einstein's near-homogeneous world matter.† On the other hand, de Sitter was well aware that the distribution of the nearby nebulae is decidedly clumpy; indeed, Charlier (1922) pointed out that it resembles a clustering hierarchy (what we would now call a fractal). That is, the conservative advice from the astronomical community would have been that the observations do not support Einstein's world picture, that he would do well to consider a fractal model instead. But now Einstein's cosmological principle is well established and part of the standard model: fluctuations from homogeneity on the scale of the Hubble length are less than one part in 10^3 (from the isotropy of the X-ray background, and about one part in 10^4 in the standard relativistic model (Peebles 1993)). This is a magnificent triumph of pure thought!

Just as the cosmological principle was introduced by hand to solve a theoretical problem, the violation of Mach's principle in asymptotically flat spacetime, the biasing principle was introduced to reconcile the low relative peculiar velocities of the galaxies with the high mass density of the theoretically preferred Einstein–de Sitter world model (Davis *et al.* 1985). There never has been any serious observational evidence for biasing, but the idea was rightly taken seriously because it is elegant and plausible.‡ But I do not include biasing in the standard model; we have no very strong evidence for it and the following three arguments against it.

First, there is no identification of a population of void irregular galaxies, remnants of the assumed suppression of galaxy formation in the voids (Peebles 1989). The first systematic redshift survey showed that the distributions of low and high luminosity galaxies are strikingly similar (Davis *et al.* 1982). I know of no survey since then, in 21 cm, infrared, ultraviolet, or low surface brightness optical, that reveals a void population. There is a straightforward interpretation: the voids are nearly empty because they contain little mass.

Second, the improving suite of cosmological tests listed in the next section suggests the mean mass density is well below the Einstein–de Sitter value. If the density is

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† Published comments suggest de Sitter considered Einstein's ideas on this point somewhat speculative, while Einstein felt that de Sitter's conservative attitude was a little defeatist. It will be fascinating to see whether the de Sitter archives yield any letters exchanging views on the cosmological principle.

‡ The different distributions of early-type galaxies, of spirals, and of starburst galaxies cannot all trace the mass, and it has been very correctly noted that in this sense the biasing manifestly obtains (e.g. Guzzo *et al.* 1997). But the spheroid components of the galaxies seem to be the most robust against environment-dependent effects such as mass loss—biasing through evolution rather than birth—and my impression is that within the uncertainties all dynamical analyses are consistent with the assumption that the spheroid light traces the mass on the scale of inter-galaxy distances. And optical samples are reasonable tracers of the spheroid component.

low, it means galaxies move slowly because there is not much mass to gravitationally pull them, not because they are biased tracers of the mass.

Third, the galaxy autocorrelation function at low redshift has a simple form, quite close to the power law $\xi_{gg} \propto r^{-\gamma}$, with $\gamma = 1.77 \pm 0.04$, over three orders of magnitude in separation, $10 \text{ kpc} \lesssim hr \lesssim 10 \text{ Mpc}$. Carlberg (this issue) shows that the index γ is quite close to constant back to redshifts near unity. On the theoretical side, Simon White describes elegant numerical simulations of the adiabatic cold dark matter (CDM) model. In these simulations the mass autocorrelation function $\xi_{\rho\rho}(r)$ is not close to a power law, and the slope of $\xi_{\rho\rho}(r)$ increases with increasing time. The two functions allow the definition of a bias parameter,

$$b(r, t) = [\xi_{gg}(r, t)/\xi_{\rho\rho}(r, t)]^{1/2}. \tag{2.1}$$

In the adiabatic CDM model, this is a function of separation and time. One interpretation is galaxies are biased tracers of mass, the bias depending on scale and time. But why should the biased tracer exhibit a striking regularity, in $\xi_{gg}(r)$ and the three- and four-point functions, that is not a property of the mass that is driving evolution? The more straightforward reading is that the regularity in $\xi_{gg}(r)$ reflects a like regularity in the behaviour of the mass, and that there is a slight flaw in the model. Given the enormous step we are taking in analysing the growth of the structure of the universe, it surely would not be surprising to learn that we have not yet got it exactly right.

3. The cosmological tests

(a) The purpose of the tests

In the standard Friedmann–Lemaître cosmological model, coordinates can be assigned so the mean line element (ignoring departures from homogeneity) is

$$ds^2 = dt^2 - a(t)^2 \left[\frac{dr^2}{1 \pm r^2/R^2} + r^2(d\theta^2 + \sin^2\theta \, d\phi^2) \right]. \tag{3.1}$$

The mean expansion rate satisfies the equation

$$H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \tfrac{8}{3}\pi G\rho \pm \frac{1}{a^2 R^2} + \tfrac{1}{3}\Lambda, \tag{3.2}$$

which can be approximated as

$$H^2 = H_0^2[\Omega(1+z)^3 + \kappa(1+z)^2 + \lambda]. \tag{3.3}$$

This defines the fractional contributions to the square of the expansion rate by matter, space curvature, and the cosmological constant (or a term in the stress-energy tensor that acts like one). The time dependence assumes pressureless matter and constant Λ. Other notations are in the literature; one that reflects the equal roles of the three parameters in equation (3.2) is

$$\Omega_M = \Omega, \qquad \Omega_R = \kappa, \qquad \Omega_\Lambda = \lambda. \tag{3.4}$$

Another that adds the matter and Λ terms appears in Michael Turner's contribution (this issue). To avoid confusion with the definitions in equations (3.3) and (3.4) we might express Turner's convention as

$$\Omega' = \Omega + \lambda = 1 - \kappa. \tag{3.5}$$

Table 1. *The cosmological tests*

(EdS is Einstein–de Sitter, $\Omega = 0.25 \pm 0.1$, $\sqrt{}$ is a conditional pass and X is a conditional fail.)

	test	EdS	Ω flat	Ω open
1a	world time $t(z)$: ages of stars and elements	X??	$\sqrt{}$	$\sqrt{}$
1b	SneIa redshift–magnitude relation	X	$\sqrt{}$	$\sqrt{}$
1c	counts: $\mathrm{d}N = f(m,z)\,\mathrm{d}m\,\mathrm{d}z$	?	?	?
1d	lensing of quasars by galaxies	$\sqrt{}$	X??	$\sqrt{}$
2a	dynamics on scales $\lesssim 10$ Mpc	X	$\sqrt{}$	$\sqrt{}$
2b	dynamics on larger scales	X?	$\sqrt{}$	$\sqrt{}$
3a	CBR and galaxy distributions	X?	$\sqrt{}$?	$\sqrt{}$?
3b	cluster evolution	X?	$\sqrt{}$	$\sqrt{}$
3c	baryon mass fraction in clusters	X?	$\sqrt{}$	$\sqrt{}$
3d	galaxy formation	?	?	?
4	fundamental physics	?	?	?

This isolates the curvature term, which is useful. And since the evidence is that Ω is small it certainly helps rescue our theoretical preference for a density parameter equal to unity. I find it unsatisfying, however; what became of the intense debates we had on biasing and the other systematic errors in the measurement of Ω?

I can get more excited about the Full Monty: let

$$\Omega'' = \Omega + \kappa + \lambda. \tag{3.6}$$

Each of the terms on the right-hand side of this equation is measurable in principle, and if the applications of the cosmological tests continue to improve at the present rate it may not be many more years before we have 10% measurements of each of the three numbers. If they add to unity, we will have a test of general relativity theory applied on large scales in the strong curvature limit.

The point is illustrated another way in table 1. The entries represent different ways to probe the standard relativistic model, and the columns are grades for how well three sets of parameter choices fit the results. As the observations improve we may find that only one narrow range of parameters is consistent with all the constraints. If so we will have settled two issues.

First, it surely will continue to be difficult to use internal evidence to rule out systematic errors in astronomical observations. For example, can astronomers unambiguously demonstrate that supernovae of type Ia and in a given class of light curve shape really are drawn from the identical population at redshifts $z \sim 0$ and $z \sim 1$? A consistent story from independent tests is strong evidence that the measurements have not been corrupted by some subtle systematic error.

Second, a consistent story will be a strong positive test of the standard relativistic cosmological model, as in equation (3.6). The successful parameter set could be quite different from any of the choices in the table, of course; we may be driven to a dynamical Λ, for example (Peebles & Ratra 1988; Huey *et al.* 1998).

The classical cosmological tests based on measures of the spacetime geometry have been supplemented by a new class of tests based on the condition that the

cosmology admit a consistent and observationally acceptable model for structure formation (category 3 in table 1). I comment on aspects of structure formation in § 4 and § 5.

(b) The state of the tests

The constraint from the rate of lensing of quasars by foreground galaxies does not comfortably fit the curvature of the redshift–angular distance relation. The analysis of lensing by Falco *et al.* (1998), for a combined sample of lensing events detected in the optical and radio, indicates that if the universe is cosmologically flat then $0.64 < \Omega < 1.66$ at one standard deviation, and $\Omega > 0.38$ at 2σ. The SNeIa redshift magnitude relation, from the magnificent work of Perlmutter *et al.* (1998) and Reiss *et al.* (1998), seems best fit by $\Omega \sim 0.2$, $\lambda \sim 0.8$. The discrepancy is not far outside the error flags, but I think that if the lensing rate were the only available cosmological test, we would greet it as confirmation of the Einstein–de Sitter model and another success for pure thought.

The lensing constraint depends on the galaxy mass function. The predicted peak of the lensing rate at angular separation $\theta \sim 1$ arc sec is dominated by the high surface density branch of early-type galaxies at luminosities $L \sim L_*$. The number density of these objects is not well known, and an improved measurement is an important goal for the new generations of surveys of galaxies. If further tests of the lensing and redshift-magnitude constraints confirm an inconsistency for constant Λ, the lesson may be that the cosmological constant is dynamical, rolling to zero, as Ratra & Quillen (1992) point out.

The Einstein–de Sitter model is not yet ruled out, but I think most of us would agree that consideration of structure formation in low density cosmological models is well motivated.

4. The origin of large-scale structure

We have good reason to think galaxies grew by gravity out of small initial departures from homogeneity, but the nature of the initial conditions is open to discussion. To illustrate this I present some elements of an isocurvature model. Details are in Peebles (1999*a, b*).

(a) Adiabatic and isocurvature models

In the paradigm Simon White discussed at the Discussion Meeting, structure grows out of an adiabatic departure from homogeneity—as would be produced by local reversible expansion or contraction from exact homogeneity—that is a spatially stationary isotropic random Gaussian process. Another possibility is that the primeval mass distribution is exactly homogeneous—there is no perturbation to spacetime curvature—and structure formation is seeded by an inhomogeneous composition. In the isocurvature model presented here the initial entropy per baryon is homogeneous, to preserve the paradigm for element formation, and homogeneity is broken by the distribution of cold dark matter. In both the adiabatic and isocurvature models, the present mass of the universe is dominated by non-baryonic CDM; I shall call them ACDM and ICDM models.
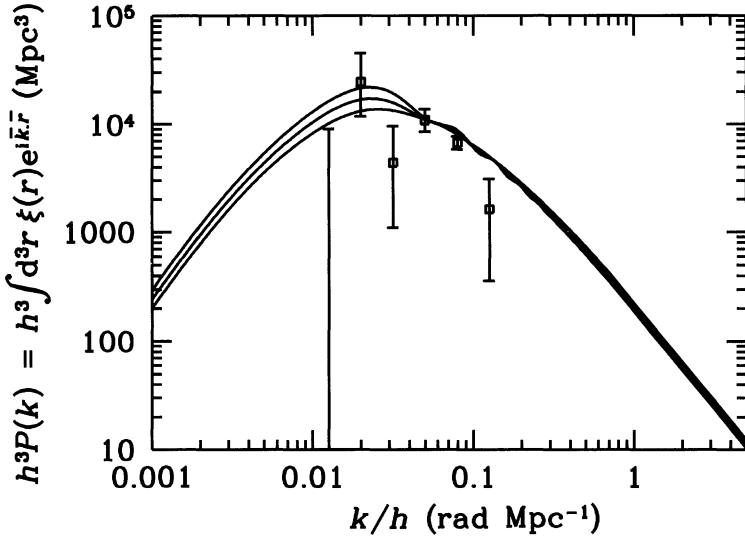
Figure 1. Power spectrum of the CDM space distribution in the ICDM model at the present epoch computed in linear perturbation theory for the parameters in equations (4.3) and (4.4). The density parameter in baryons is $\Omega_B = 0.05$ in the top curve at small k, 0.03 in the middle, and 0.01 in the bottom curve. The data are from the PSC-z survey (Saunders *et al.* 1998).

(b) *Power spectra*

In the ACDM model the primeval mass density fluctuation (defined as the most rapidly growing density perturbation mode in time-orthogonal coordinates) has a close to power law power spectrum, $P \propto k^n$. In the ICDM model the primeval distribution of the CDM is close to a power law, $P \propto k^m$, in a homogeneous net mass distribution. It is an interesting exercise to check that in linear perturbation theory the evolution from the initial radiation-dominated universe to the present CDM-dominated epoch bends the spectra to

$$\text{ACDM:} \quad P \propto k^{n-4}, \ k \gg k_{eq}, \qquad\qquad P \propto k^n, \ k \ll k_{eq}, \qquad (4.1)$$

$$\text{ICDM:} \quad P \propto k^m, \ k \gg k_{eq}, \qquad\qquad P \propto k^{m+4}, \ k \ll k_{eq}, \qquad (4.2)$$

where k_{eq} is the wavenumber appearing at the Hubble length at the redshift z_{eq} of equality of mass densities in matter and radiation.

The similarity of equations (4.1) and (4.2) for $m \sim n-4$ extends to roughly similar spectra of the angular distribution of the thermal cosmic background radiation (the CBR) in the adiabatic and isocurvature CDM models. The status of ACDM model fits to the fluctuation spectra of galaxies and the CBR is discussed in this issue by Bond. Figures 1 and 2 show the ICDM model predictions for the parameters

$$m = -1.8, \qquad \Omega = 0.2, \qquad \lambda = 0.8, \qquad h = 0.7, \qquad (4.3)$$

with the normalization

$$P(k) = 6300 h^{-3} \text{ Mpc}^3 \text{ at } k = 0.1 h \text{ Mpc}^{-1}, \qquad (4.4)$$

where Hubble's constant is $H_0 = 100 h \text{ km s}^{-1} \text{ Mpc}^{-1}$. The data in figure 1 are from the IRAS PSC-z (point source catalogue) redshift survey of Saunders *et al.* (1998). This is the real space spectrum after correction for peculiar velocity distortion
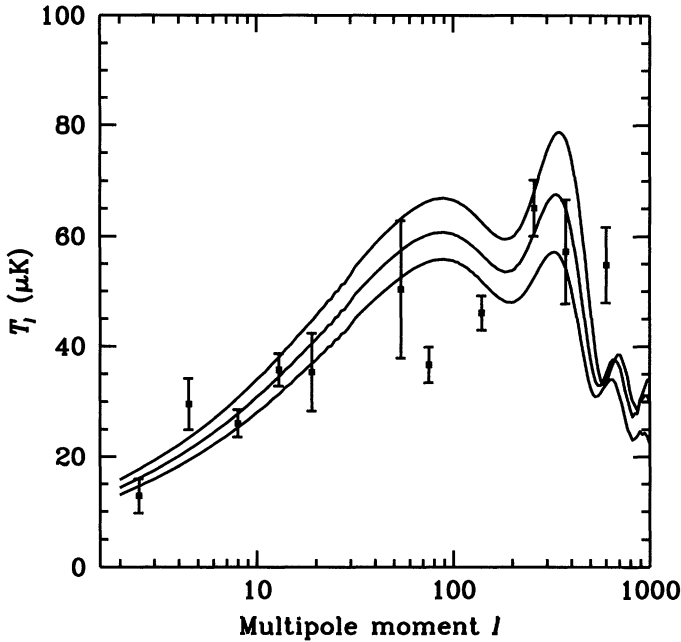
Figure 2. Angular fluctuation spectrum of the CBR in the ICDM model with the parameters in equations (4.3) and (4.4). The density parameter in baryons is $\Omega_B = 0.05$ in the top curve, 0.03 in the middle, and 0.01 in the bottom curve. The ionization history is computed under the assumption that there is no source of ionizing radiation apart from the CBR.

represented by the density-bias parameter $\beta = 0.6$. There are good measurements of the spectrum of the galaxy distribution on smaller scales, $k > 0.1h$ Mpc^{-1}, but this approaches the nonlinear sector, and it seems appropriate to postpone discussion of the small-scale mass distribution until we have analyses of nonlinear evolution from the non-Gaussian initial conditions of the model in equation (4.6). Since the PSC-z catalogue is deep, with good sky coverage, it promises to be an excellent probe of the large-scale galaxy distribution, and it offers a very useful normalization for the structure formation models.

Figure 2 shows second moments of the angular distribution of the CBR, where

$$T(\theta, \phi) = \sum a_l^m Y_l^m(\theta, \phi), \qquad T_l = \left[\frac{l(2l+1)}{4\pi}\right]^{1/2} \langle|a_l^m|^2\rangle^{1/2}. \qquad (4.5)$$

In the approximation of the sum over l as an integral, the variance of the CBR temperature per logarithmic interval of l is $(T_l)^2$.† The measured T_l are from the compilation of Ratra (personal communication).

The data point in figure 2 at $l \sim 80$ is well below the ICDM model, but I am told the measurements could be more uncertain than the formal error flags. Perhaps more serious is the slope of the model spectrum at $l \lesssim 20$, at three standard deviations from the COBE measurement (Hinshaw *et al.* 1996), but again I gather this is not

† There are good historical reasons, dating from the introduction of the ACDM model, for writing $2l(l+1)$ in place of $l(2l+1)$, as does Bond in his contribution to this issue, but since I am considering ICDM, the convention in equation (4.5), which I prefer because it reflects the $2l+1$ components for each value of l, may not be unreasonable.

a definitive inconsistency with an exceedingly difficult measurement. That is, the second moments of the large-scale distributions of mass and radiation in the ICDM model agree with the data as well about as might be expected. The same is true of the ACDM models considered by Bond. At most one will pass the tests expected from work in progress, but that is for the future.

(c) Inflation-based model for isocurvature initial conditions

Simple and arguably natural realizations of the inflation concept lead to adiabatic initial conditions; others to isocurvature initial conditions. In the example of the latter in Peebles (1999a), the CDM is a scalar field ϕ that ends up after inflation in a squeezed state as a Gaussian random process with mass density

$$\rho(\boldsymbol{x}) = M^2 \phi(\boldsymbol{x})^2/2, \tag{4.6}$$

for field mass M. In a simple case the field satisfies

$$\langle \phi \rangle = 0, \qquad \langle \phi(\boldsymbol{x}_1)\phi(\boldsymbol{x}_2) \rangle \propto x_{12}^{-\epsilon}, \tag{4.7}$$

and the power spectrum of the mass distribution in equation (4.6) is a power law with index $m = 2\epsilon - 3$. The model requires $m = -1.8$, or $\epsilon = 0.6$. The 'tilt' from the scale-invariant case $\epsilon \simeq 0$ is not difficult to arrange; whether it might be considered natural has yet to be debated.

The primeval density fluctuations in the model in equations (4.6) and (4.7) are non-Gaussian and scale-invariant: the frequency distribution of the density contrast δ averaged through a window and scaled by the standard deviation $\langle \delta^2 \rangle^{1/2}$ is independent of the window size. The evidence discussed in Peebles (1999b) indicates the model with these initial conditions is viable but subject to serious tests from improvements from observational work in progress. The same is true of the ACDM models, of course. I turn now to one of the tests, the redshift of assembly of the galaxies.

5. The epoch of galaxy assembly

(a) Scaling galaxies from clusters of galaxies

The power law model for the primeval CDM fluctuation spectrum (equations (4.2) and (4.3)) is a good approximation for the residual CDM mass distribution at redshifts less than the epoch z_{eq} of equality of mass densities in matter and radiation and on scales small compared to the Hubble length at z_{eq} and large compared to the scale of nonlinear clustering. Within these bounds the spectrum varies as

$$P_\rho(k, t) \propto k^m D(t)^2, \tag{5.1}$$

where $D(t)$ is the solution to the linear equation for the evolution of the density contrast from an initially isothermal perturbation of the CDM. The RMS contrast through a window of co-moving radius x varies as

$$\delta \propto x^{-(3+m)/2} D(t). \tag{5.2}$$

Gravitational structure formation is triggered by passage of upward fluctuations of δ through unity, and the threshold is not sensitive to Ω in a cosmologically flat model. This means the characteristic physical length (r_{nl} is the characteristic radius

of the nonlinear mass concentrations), mass, and internal velocity of newly forming structures scale with time as

$$r_{\mathrm{nl}} \propto (1+z)^{-1} D^{2/(3+m)}, \quad M \propto D^{6/(3+m)}, \quad \sigma \propto (1+z)^{1/2} D^{2/(3+m)}. \tag{5.3}$$

These relations neglect non-gravitational interactions; they may be expected to be useful approximations on scales much larger than the half-light radii in galaxies, where the CDM halo dominates the mass in the standard model.

We can normalize to the great clusters of galaxies, with

$$\left.\begin{array}{ll} r_{\mathrm{A}} = 1.5h^{-1}\ \mathrm{Mpc}, & \sigma_{\mathrm{cl}} = 750\ \mathrm{km\ s}^{-1}, \\ m_{\mathrm{cl}} = 4 \times 10^{14} h^{-1} M_{\odot}, & n_{\mathrm{cl}} = (2 \pm 1) \times 10^{-6} h^{-3}\ \mathrm{Mpc}^{-3}. \end{array}\right\} \tag{5.4}$$

The Abell radius is r_{A}, σ_{cl} is the RMS mean line of sight dispersion of velocities of galaxies in $R \geqslant 1$ clusters, m_{cl} is the mean mass within the Abell radius, and n_{cl} is the present number density of clusters with mass $m > m_{\mathrm{cl}}$ (Bahcall & Cen 1993). Clusters are relaxing at the Abell radius, and the merging rate is significant, but it is generally agreed that that internal velocities typically are close to what is needed for support against gravity at $r \sim r_{\mathrm{A}}$. In the power law model in equation (5.1), these quantities scaled back in time characterize objects in a like state of development in the past.

With the parameters used in figures 1 and 2 (equation (4.3)) the scaling relations applied at expansion factor $1 + z = 7$ give

$$r_{\mathrm{g}} = 15h^{-1}\ \mathrm{kpc}, \qquad \sigma_{\mathrm{g}} = 140\ \mathrm{km\ s}^{-1}, \qquad M_{\mathrm{g}} = 1.3 \times 10^{11} h^{-1} M_{\odot}. \tag{5.5}$$

The present characteristic separation of clusters and the scaled value of the co-moving separation at $1 + z = 7$ are

$$d_{\mathrm{cl}} = n_{\mathrm{cl}}^{-1/3} = 80h^{-1}\ \mathrm{Mpc}, \qquad d_{\mathrm{g}} = 5h^{-1}\ \mathrm{Mpc}. \tag{5.6}$$

In this model an astronomer sent back in time to $1 + z = 7$ would see objects with the somewhat disordered appearance of present-day clusters, merging at a significant rate, but with internal motions typically close to what is needed for virial support. The characteristic size, mass, and co-moving distance between objects would be seen to be characteristic of the luminous parts of present-day L_* galaxies. Our time traveller might well be inclined to call these objects young galaxies, already assembled at $z = 6$.

At expansion factor $1 + z = 20$ the scaling relations give

$$r \sim 1\ \mathrm{kpc}, \qquad \sigma \sim 40\ \mathrm{km\ s}^{-1}, \qquad m \sim 1 \times 10^9 M_{\odot}, \tag{5.7}$$

numbers characteristic of dwarf galaxies. I have to assume many merge to form the L_* giants, and that the merging rate eases off at $1 + z \sim 7$, perhaps because the dissipative settling of the baryons has progressed far enough to lower the cross-section for merging, so later structure formation can build the present-day galaxy clustering hierarchy.

If galaxies were assembled as mass concentrations at $1 + z = 7$, as this model suggests, how would they appear at $1 + z \simeq 4$? Internal velocities ought to be characteristic of present-day galaxies. That is not inconsistent with the properties of the damped Lyman-α absorbers studied by Wolfe & Prochaska (1998), though Haehnelt *et al.* (1998) show other interpretations are possible. The expected optical appearance depends on how feedback affects the rate of conversion of gas to stars, a delicate
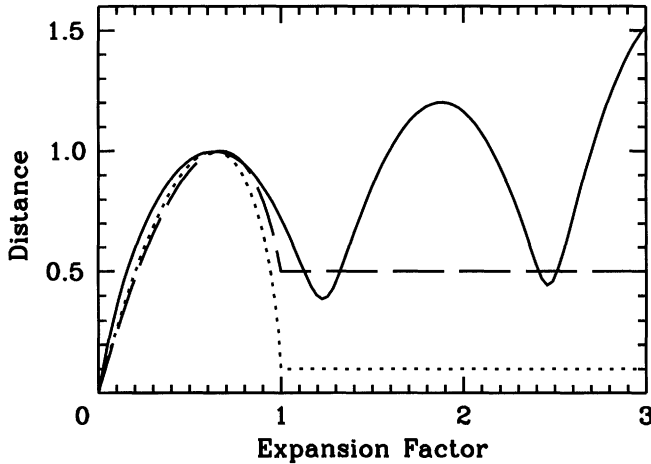
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Figure 3. Models for gravitational assembly of galaxies and systems of galaxies. The solid line is the distance between the Andromeda Nebula and the Milky Way in a solution for the interaction with neighbouring mass concentrations. For this curve the present epoch is at expansion parameter $a = 1$ and the distance unit is 0.97 Mpc. The dashed line is a commonly discussed spherical model. The dotted line models late assembly of the mass in the central parts of a normal giant galaxy.

issue I am informed. Steidel (this issue) presents elegant optical observations of high redshift galaxies that reveal strong spatial clustering. Steidel points out this could signify strong biasing at formation. The interpretation could be slightly different in the non-Gaussian ICDM model, where high density fluctuations tend to appear in concentrations (Peebles 1999c).

Structure formation happens later in ACDM than ICDM. I have expressed doubts that late assembly could produce the high density contrasts of normal present-day L_* galaxies, but the numerical simulations White describes seem not to find this a problem. If dense galaxies can be assembled at low redshift, when the mean mass density is low, one might have thought that protogalaxies assembled at high redshift and high mean mass density would be unacceptably dense. But Nature was able to form clusters of galaxies that are close to virial equilibrium at modest density contrast at the Abell radius, and well enough isolated that they seem likely to remain part of the clustering hierarchy rather than merging into larger monolithic superclusters. Under the scaling argument the same would be true of protogalaxies assembled at $1 + z \sim 7$ in the ICDM model.

(b) Collapse models

I arrived at the isocurvature model in § 4 (and Peebles 1999a, b) through a search for a model for galaxy formation at high redshift, when the cosmic mean density is comparable to that of the luminous parts of a normal large galaxy. The argument traces back to Partridge & Peebles (1967), a recent version is in Peebles (1998), and elements are reviewed here.

The solid line in figure 3 is the distance between the Andromeda Nebula M31 and our Milky Way galaxy in a numerical solution for the motions of the galaxies in and near the Local Group (Peebles 1996). The orbits are constrained to arrive

at the present positions at expansion parameter $a = 1$ from initial motions at $a \to 0$ consistent with the homogeneous background cosmological model. This uses the Einstein–de Sitter model, so the solution may be scaled with time.

The dashed line in the figure assumes spherical symmetry with no orbit crossing, expansion from cosmological initial conditions, and collapse to half the maximum radius, at which point the kinetic energy in the spherical model has reached half the magnitude of the gravitational potential energy. The solid line for the motion of M31 relative to the Milky Way has a similar shape but with significant differences. In the numerical solution neighbouring galaxies are close to the Milky Way and M31 at $a \lesssim 0.25$, so the solid line is more strongly curved than a spherical solution with fixed mass. The solid line is less strongly curved at larger expansion factor because the interaction with neighbouring mass concentrations has given the Milky Way and M31 substantial relative angular momentum. In this solution the present transverse velocity of M31 relative to the Milky Way is comparable to the radial velocity of approach, the minimum separation is about half the present value, and the mean separation in the future is larger than the present value. As we all know, non-radial motions tend to suppress collapse.

Now let us consider the spherically symmetric solution as a model for young galaxies. Let $r(t)$ be the proper radius of a sphere that is centred on the young galaxy and contains the mass M_g in equation (5.5). In the spherical solution, which ignores non-radial motion and the motion of mass across the surface of the sphere, the radius varies with time as $r = A(1 - \cos\eta)$, where $t = B(\eta - \sin\eta)$ and $A^3 = GM_gB^2$. This ignores the cosmological constant Λ, which has little effect on the orbit. If spherical collapse stops at radius r_g at redshift z_g, then in the spherical model the collapse factor from maximum expansion is

$$r_g/r_{max} = (1 - \cos\eta_g)/2, \tag{5.8}$$

and an adequate approximation to η_g is

$$\frac{(\eta_g - \sin\eta_g)^2}{(1 - \cos\eta_g)^3} = \frac{8}{9\Omega}\left(\frac{\sigma_g}{H_0 r_g}\right)^2 (1 + z_g)^{-3} = \frac{4 \times 10^4}{(1 + z_g)^3}, \tag{5.9}$$

for the numbers in equation (5.5).

For the collapse factor $r_{max}/r_g = 2$ in the dashed line in figure 3, equation (5.9) says $1 + z_g \sim 10$, not far from the value $1 + z_g = 7$ in equation (5.5).

In a model for late galaxy assembly, at $z_g = 1$, equations (5.8) and (5.9) say $r_{rmax}/r_g \sim 10$. This is the dotted line in figure 3. The pronounced collapse could result from exchange of energy among lumps settling out of a more extended system, as happens in numerical simulations (Navarro *et al.* 1996), but I think there are two reasons to doubt it happens in galaxy formation. First, in a hierarchical model for structure formation collapse to $r_g \sim 20\,\mathrm{kpc}$ at $z_g = 1$ traces back to a cloud of subgalaxy fragments—star clusters—at radius $\sim r_{max} \sim 200\,\mathrm{kpc}$. I know of no evidence of such clustering (apart from the usual power law correlation functions) in deep samples. Second, the scaled process of formation of rich clusters of galaxies shows no evidence of pronounced collapse: clusters seem to be close to stable at the Abell radius and present in significant numbers at redshift $z = 0.5$.

These are arguments, of course, not demonstrations. I consider them persuasive enough to lend support to the isocurvature model that leads from the fit to measures of large-scale structure in figures 1 and 2 to the scaling model for early galaxy

assembly in equation (5.5), but this depends on whether galaxies really were assembled early. The observational programmes Steidel describes in this issue may well be capable of telling us when the galaxies formed.

6. Discussion

It is inevitable that the exciting rush of advances in this subject has left ideas unexplored. I have attempted to identify some roads not taken, less popular lines of thought that seem worth considering. The main points are summarized in the following questions.

(i) *Did Einstein set a good example?*

Einstein's brilliant success in establishing key elements of the standard cosmological model is an example of why we pay serious attention to elegant ideas, sometimes even in the face of contrary empirical indications. But I think this is not an entirely edifying example: Einstein's intuition was not always so successful, and most of us are not Einsteins. In the present still crude state of cosmology it is better to be led by the phenomenology from astronomy and from particle physics (that may teach us the identity of the dark matter, for example).

Most of us agree that the Einstein–de Sitter model is the elegant case; it makes sense that the community has given it special attention despite the long-standing indication from galaxy peculiar velocities that the Einstein–de Sitter density is too high. Now other lines of evidence are pointing in the same direction, as summarized in table 1, and I think there is general agreement in the community that we must give serious consideration to the possibility that Nature has other ideas about elegance. I count this as a cautionary example for the exploration of ideas on how the galaxies formed.

(ii) *Why are galaxies thought to be biased tracers of mass?*

The galaxy two-point correlation function is quite close to a power law, $\xi_{gg}(r) \propto r^{-\gamma}$, over three orders of magnitude of separation r at low redshift, and the index γ is quite close to constant back to redshifts approaching unity. This is not true of the mass autocorrelation function $\xi_{\rho\rho}(r)$ in the adiabatic cold dark matter (ACDM) model. Thus we have a measure of bias, $b(r,t) = [\xi_{gg}(r,t)/\xi_{\rho\rho}(r,t)]^{1/2}$ (equation (2.1)), that depends on position and time. Should we take this as evidence that galaxies are biased mass tracers? Since the regularity is in the galaxies surely the first possibility to consider is that $\xi_{gg}(r)$ is revealing a like regularity in the behaviour of the mass, that the bias is in the model. This reading is heavily influenced by a related issue: if much of the CDM is in the voids defined by normal galaxies where are the remnants of the void galaxies? Surely they are not entirely invisible?

I was impressed by the elegant simulations of the ACDM models Simon White presented at the Discussion Meeting, and have to believe they reflect aspects of reality, but as I have explained I also have to suspect there is more to the story. Would the isocurvature variant do better? That awaits searching tests by numerical simulations of the kind that that have been applied to the adiabatic case.

(iii) *What is the purpose of the cosmological tests?*

One often reads that it is to determine how the world ends. But should we trust an extrapolation into the indefinitely remote future of a theory that we know can only be a good approximation to reality? For a trivial example, suppose the universe has zero space curvature and the present value of the density parameter in matter capable of clustering is $\Omega = 0.2$, with the rest of the contribution to H_0^2 in a term that acts like a cosmological 'constant' Λ that is rolling toward zero (Peebles & Ratra 1988; Huey *et al.* 1998). If the final value of Λ is identically zero, then the world ends as Minkowksi spacetime (after all the black holes have evaporated). If Λ ends up at a fixed negative value, no matter how close to zero, the world ends in a Big Crunch. Should we care which it is? I would consider a bare answer an empty advance, because the excitement of physical science is in discovering the interconnections among phenomena. Perhaps the excitement of knowing how the world ends will lie in what it teaches us about how the world began.

The classical cosmological tests, that probe spacetime geometry, have been greatly enriched by tests based on the condition that the cosmology admit a consistent and observationally acceptable theory for structure formation. The structure formation theory in turn tests ideas about what the universe was like before it was well described by the classical Friedmann–Lemaître model, and may eventually allow us to enlarge the standard model to include the story of how the world begins and ends.

(iv) *What is the standard model for structure formation?*

Generally accepted elements are the gravitational growth of small primeval departures from homogeneity, that may be described as a stationary isotropic random process, in a universe with present mass that is dominated by CDM and maybe a term that acts like a cosmological constant.

The most striking piece of evidence for the gravitational instability picture is the agreement between the primeval density fluctuations needed to produce the CBR anisotropy and the present distribution and motion of the galaxies. Precision measurements in progress should allow us to fix many of the details of this gravitational instability picture, but within present constraints we cannot say that the primeval density fluctuations are Gaussian, or adiabatic, because we have a viable alternative, the non-Gaussian isocurvature model mentioned in § 4.

The main piece of evidence for the CDM is the mismatch between the baryon mass density in the standard model for the origin of the light elements and the mass density indicated by dynamical analyses of relative motions of the galaxies. Our reliance on hypothetical mass is embarrassing; a laboratory demonstration of its existence would be an exceedingly valuable advance.

(v) *Should we expect surprises from the next generation of surveys?*

It is a sign of the growing maturity of our field that we can pose questions that are motivated by specific theoretical issues and can be addressed by feasible observations. But I think our subject still is immature enough that we should be quite prepared for surprises. My favourite example is Shaver's (1991) demonstration that the radio galaxies within $50h^{-1}$ Mpc distance are close to the plane of the Local Supercluster, even though the plane is not apparent in the general distribution of galaxies at this

depth. If the clusters and radio sources were produced by a pancake collapse, why do we not see it in the general galaxy distribution? Maybe a better picture is that in the early universe a nearly straight cosmic string passed by, piling mass in its wake into a sheet that fragmented into the seeds of engines of active galaxies.

I think the most surprising outcome of the new surveys would be that there are no major corrections to what we think we know.

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