

sugar level	Diabetic?
0	Yes → 1
1	No → 0
2	Yes
3	No
4	No
5	No
6	Yes
7	Yes → 1

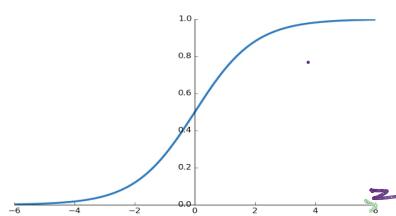
In logistic regression, we fit 'S' like curve to make classification.

### Requirements →

- ① Want output to be  $0 \leq g(z) \leq 1$ .
- ② Not much affected by the outliers.

We use 'sigmoid function' to fulfill the above requirements →

$$g(z) = \frac{1}{1 + e^{-z}}, \quad 0 \leq g(z) \leq 1$$



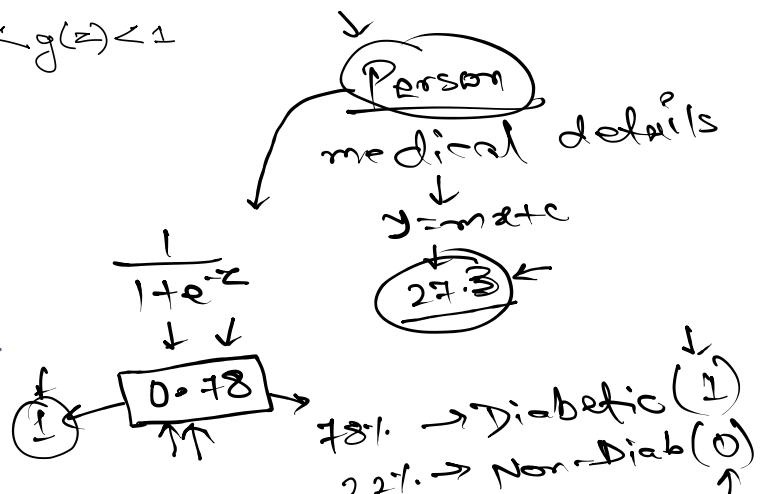
so!

$$180 \rightarrow 1.65$$

$$y = mx + c$$

$\uparrow \uparrow \downarrow \downarrow$

$-\infty \rightarrow +\infty$



Linear Regression → Equation of Best Fit Line

$$\hat{y} = mx + c$$

gives us the output b/w  $-0$  to  $+\infty$

Logit

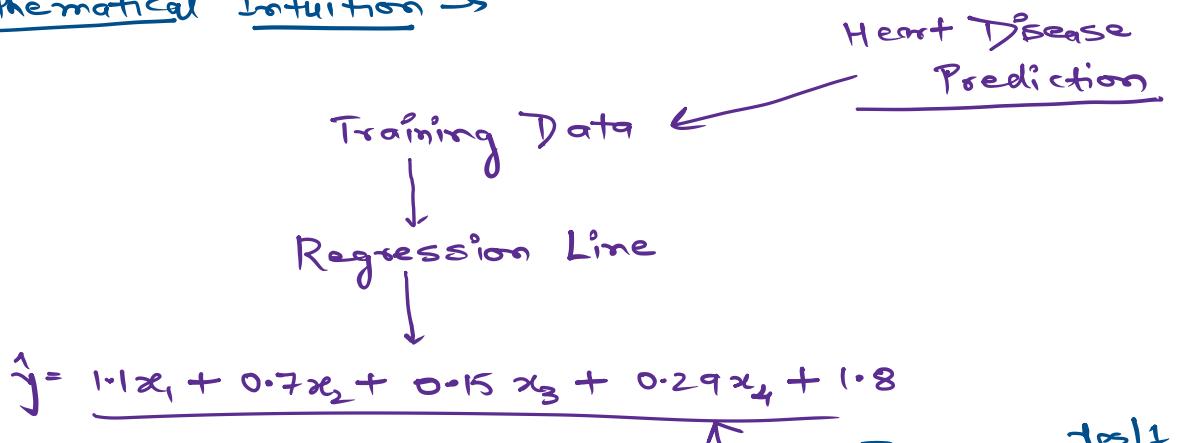
because of this it is not suitable for classification

Logistic Regression  $\rightarrow$  Sigmoid Function

$$g(z) = \frac{1}{1+e^{-z}}$$

gives an output b/w  $\frac{0 \text{ to } 1}{\downarrow \text{Probability}}$

Mathematical Intuition  $\rightarrow$



$$\hat{y} = 1.1x_1 + 0.7x_2 + 0.15x_3 + 0.29x_4 + 1.8$$

$$z = \hat{y} = 14.2 \text{ (suppose)}$$

$$g(z) = \frac{1}{1+e^{-z}}$$

$$= \frac{1}{1+e^{-14.2}}$$

$$g(z) = \underline{0.9999}$$

Always represent  
the probability  
that the predict-  
ed output is  
"Yes/1".

99.99% possibility  
that the person  
is a Heart Disease  
Patient.



Compose the output "g(z)" given by the sigmoid  
function with a pre-defined cut-off value  
of 0.5.

if  $g(z) > 0.5 \rightarrow$  output is Yes/1

— if  $g(z) \leq 0.5 \rightarrow$  output is No/0.

In our case,

$$\frac{0.9999}{g(z)} > 0.5$$

↓

Yes/1

if  $z \geq 0$   $\rightarrow g(z) = \frac{1}{1+e^{-z}} \rightarrow$  will always be  $\geq 0.5$ .

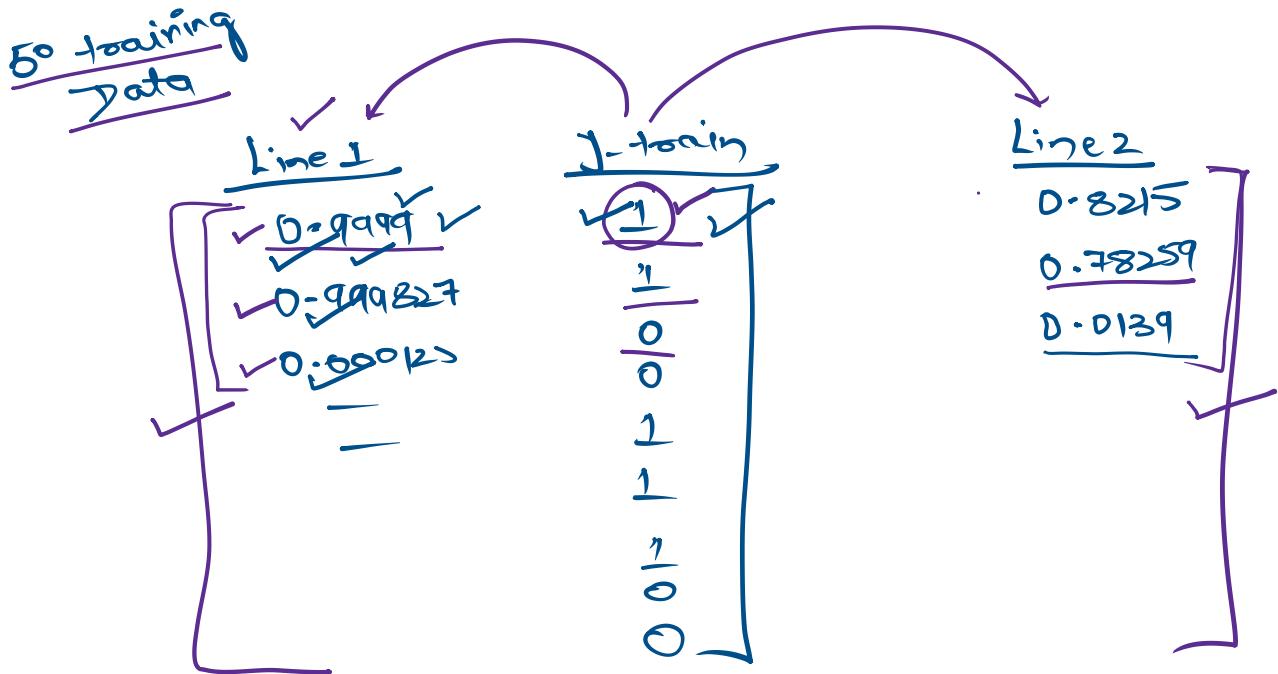
if  $z < 0$   $\rightarrow g(z) = \frac{1}{1+e^{-z}} \rightarrow$  will always be  $< 0.5$ .

Final Form of Logistic Regression equation:

$$z = \hat{y} = m_1x_1 + m_2x_2 + m_3x_3 + m_4x_4 + c$$

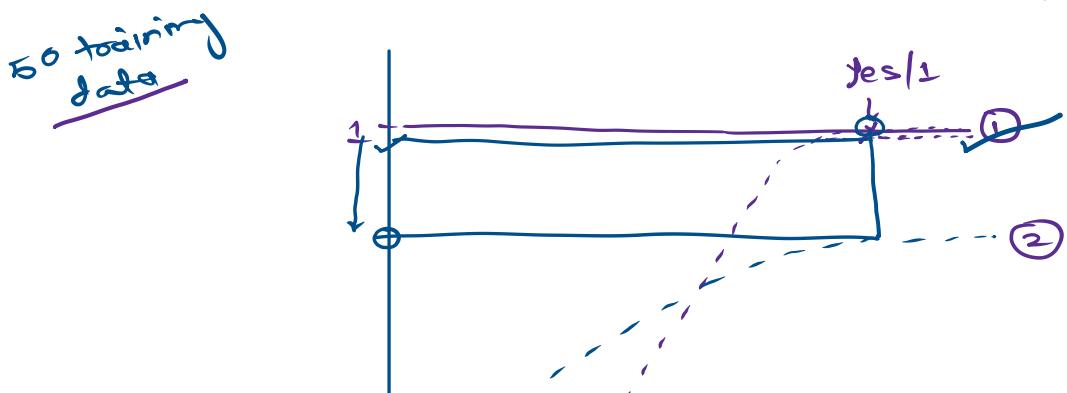
$$g(z) = \frac{1}{1+e^{-z}}$$

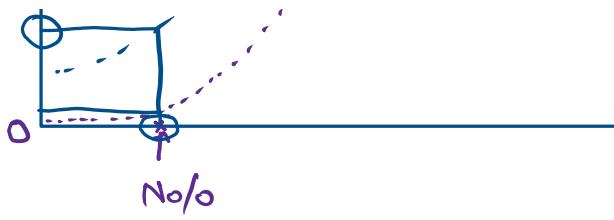
$$g(z) = \frac{1}{1 + e^{-(m_1x_1 + m_2x_2 + m_3x_3 + m_4x_4 + c)}}$$



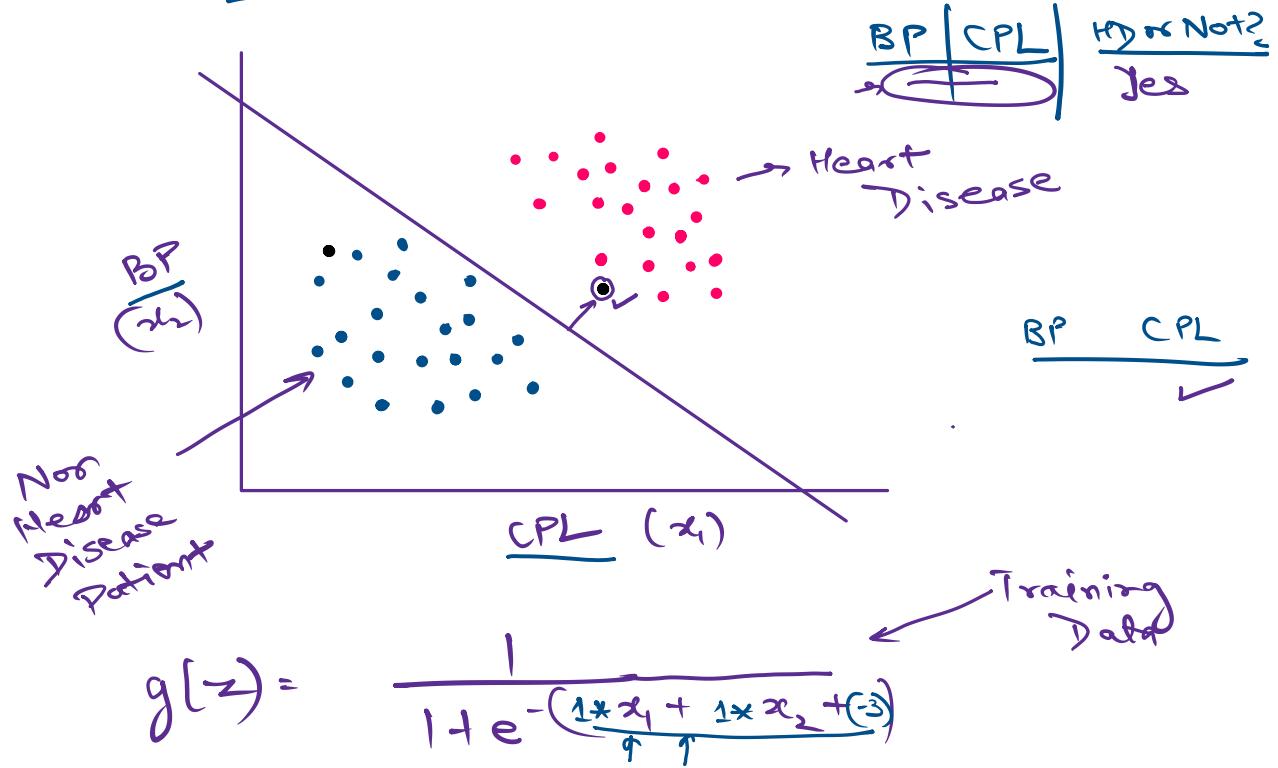
Line 1:  $1.1x_1 + 0.7x_2 + 0.15x_3 + 0.29x_4 + 1.8$  ✓

Line 2:  $0.91x_1 + 0.42x_2 + 1.13x_3 + 0.89x_4 + 1.35$





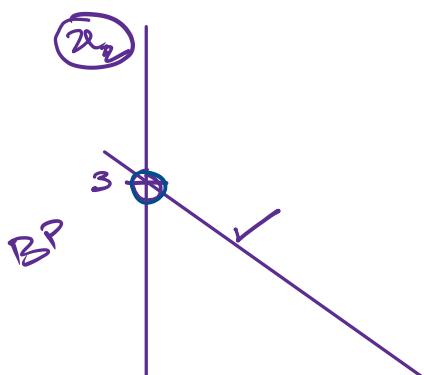
Decision Boundary :



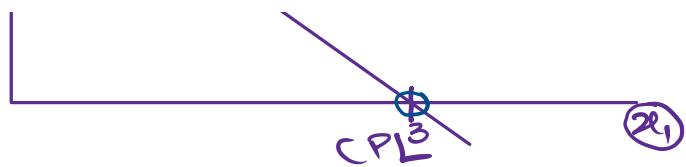
$$m_1 = 1, m_2 = 1, C = -3 \checkmark$$

$$m_1 x_1 + m_2 x_2 + C = 0$$

$$\begin{aligned} x_1 + x_2 - 3 &= 0 \checkmark \\ x_1 + x_2 &= 3 \square \end{aligned}$$



$$2x_1 + \left(\frac{5}{4}\right)x_2 = 19.7$$



$$g(z) = \frac{1}{1 + e^{-(1.1x_1 + 0.7x_2 + 0.15x_3 + 0.29x_4 + 1.8)}}$$

or

$$g(z) = \frac{1}{1 + e^{-(0.41x_1 + 0.42x_2 + 1.13x_3 + 0.89x_4 + 1.35)}}$$

