

# final\_code

February 15, 2019

## 1 Workflow

1. Objective - Define Problem and Metrics
2. Import and Store Data
3. Data Exploration and Data Cleaning
4. Feature Engineering from Raw Data
5. Classification (Modelling)
6. Communicating Results (visualizations included)

### 1.1 1. Objective

Implement a “Hand Geometry based Person Identification” system using supervised learning. Training & Testing data with labels is provided. The classification system will be measured by accuracy.

```
In [635]: #Libraries
import numpy as np
import pandas as pd
import seaborn as sns
import matplotlib.pyplot as plt
plt.rcParams['figure.figsize'] = [24, 10]
sns.set(style="darkgrid")
plt.rcParams['figure.figsize'] = [24, 10]
```

## 2 2. Import & Store Data

```
In [72]: def getxLabel(x):
        return "{:02d}x".format(x)

        def getyLabel(y):
            return "{:02d}y".format(y)

In [706]: NPOINTS = 23
data_cols = ['label']
for p in range(1,NPOINTS+1):
    data_cols.append(getxLabel(p))
    data_cols.append(getyLabel(p))
```

```

df_train = pd.read_csv('Assignment2-handtrainfile.txt',delimiter=' ',header=None,names=
df_test = pd.read_csv('Assignment2-handtestfile.txt',delimiter=' ',header=None,names=

print("TRAIN DATA:", df_train.shape, "#ofUniqIDs:",len(df_train.label.unique()))
print("TEST DATA:", df_test.shape)

```

```

TRAIN DATA: (100, 47) #ofUniqIDs: 20
TEST DATA: (100, 47)

```

```

In [707]: #Convert labels to integer codes
df_train['label'], mapping_index = pd.Series(df_train['label']).factorize()

```

### 3 3. Data Exploration and Cleaning

- what kind of data do we have? => Numerical only
- Is there any missing Data? => No.
- Are there outliers, should I care? => No.

```

In [843]: #Plot highlevel view of data to confirm it is what we expect
sns.set_style("white")
def plotHexBins(df):
    x = df['01x'].values
    y = df['01y'].values

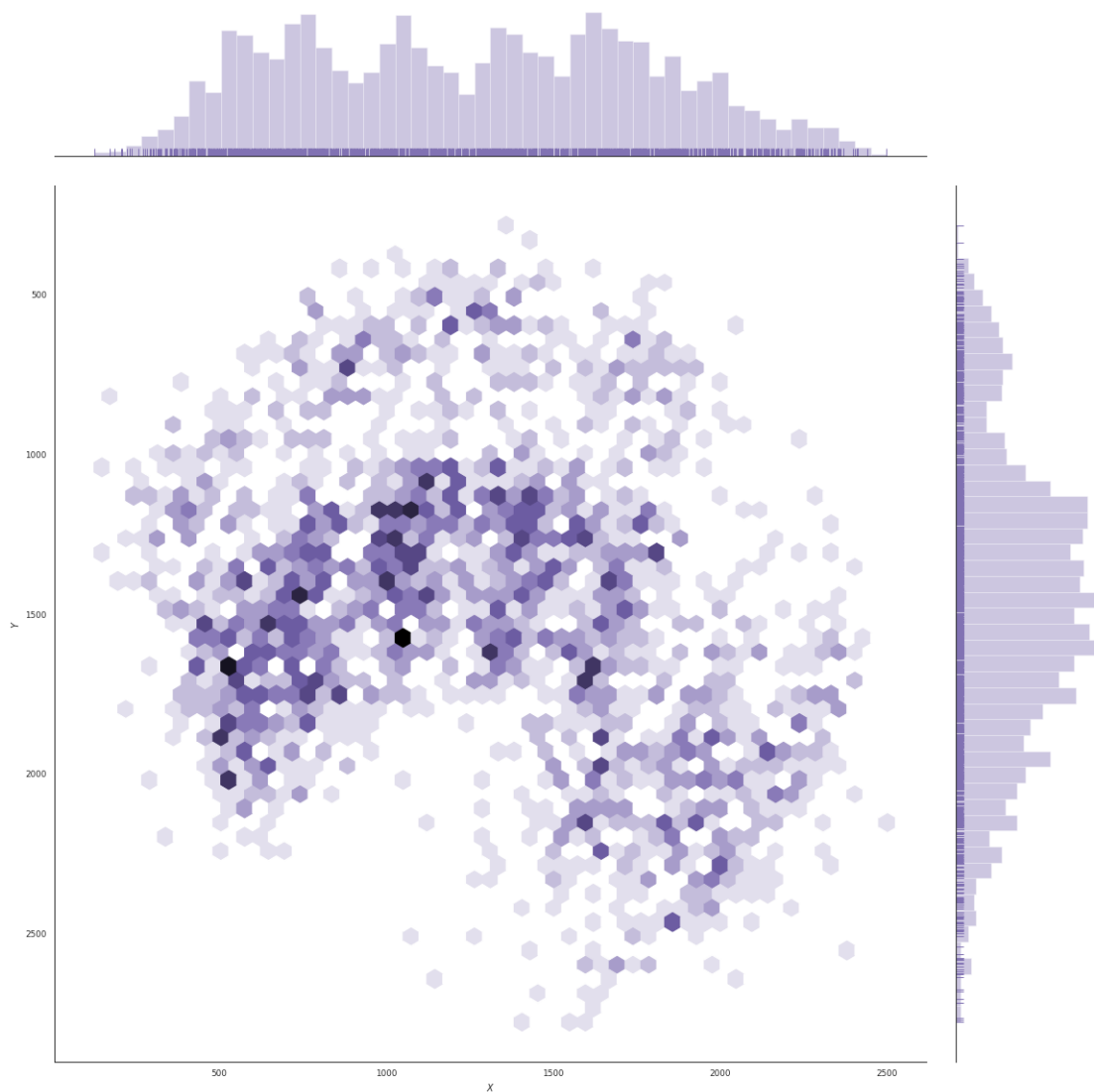
    for p in range(2,NPOINTS+1):
        x = np.append(x,df[getXLabel(p)].values)
        y = np.append(y,df[getYLabel(p)].values)

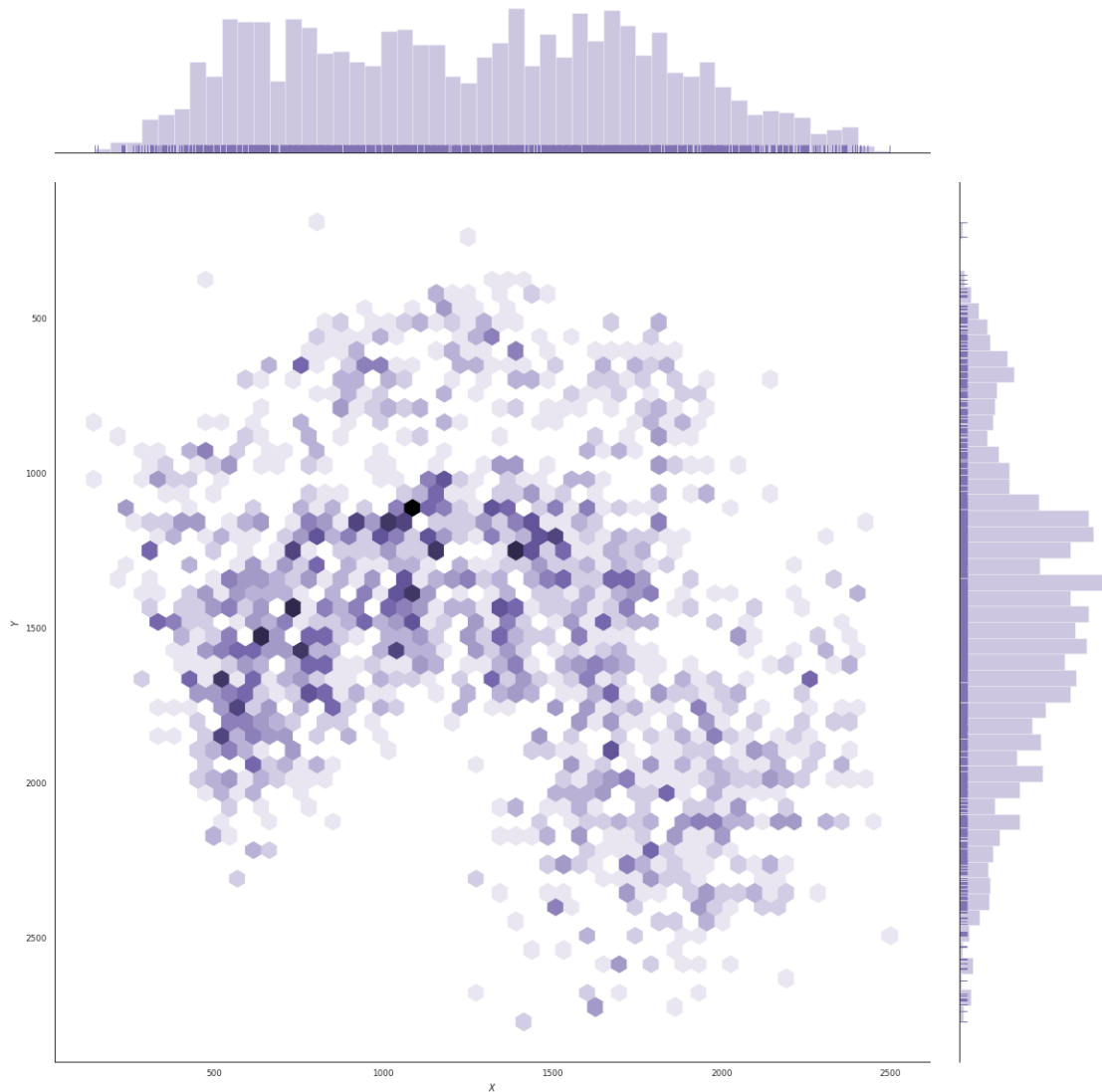
    g = sns.jointplot(x=x, y=y, kind="hex", color="m", height=16, marginal_kws=dict(
        gridsize=50)
    # g.plot_joint(plt.scatter, c="w", s=30, linewidth=1, marker="+")
    # g.ax_joint.collections[0].set_alpha(0)
    g.set_axis_labels("$X$", "$Y$")
    g.fig.axes[0].invert_yaxis()
    # g.fig.axes[0].invert_xaxis()
    plt.show()

sns.despine()
plotHexBins(df_train)
plotHexBins(df_test)

```

<Figure size 1152x864 with 0 Axes>





## 4 4. Feature Engineering

- Distance between each point?
- triangulation of all pairs? area of triangle?
- Removing highly correlated?

```
In [856]: %%time
          from sklearn.metrics.pairwise import paired_distances

          def getListofPoints(df, p):
              return df[[getXLabel(p), getyLabel(p)]].values.tolist()

          def getEdColname(p1,p2):
```

```

        return "{:02d}_e_{:02d}".format(p1,p2)

def getMdColname(p1,p2):
    return "{:02d}_m_{:02d}".format(p1,p2)

def getDistances(df):
    """
    Calculates euclidean and manhattan distances between all possible pairs
    and stores the distances in the data frame.
    RETURNS:
        - DataFrame
    """

    for p1 in range(1,NPOINTS+1):
        p1s = getListofPoints(df, p1)
        for p2 in range(p1+1,NPOINTS+1):
            if p1==p2:
                continue
            p2s = getListofPoints(df, p2)
            colname = getEdColname(p1,p2)
            df[colname] = paired_distances(p1s,p2s,'euclidean')
            colname = getMdColname(p1,p2)
            df[colname] = paired_distances(p1s,p2s,'manhattan')
    return df

df_trainf = getDistances(df_train.copy())
df_testf = getDistances(df_test.copy())

```

CPU times: user 850 ms, sys: 0 ns, total: 850 ms  
Wall time: 858 ms

```

In [857]: %%time
import itertools

def getPerimeterColname(comb):
    return "P_{:02d}_{:02d}_{:02d}".format(comb[0],comb[1],comb[2])

def getTAreaColname(comb):
    return "TA_{:02d}_{:02d}_{:02d}".format(comb[0],comb[1],comb[2])

def getSideLength(df,p1,p2):
    try:
        s1 = df[getEdColname(p1,p2)]
    except:
        s1 = df[getEdColname(p2,p1)]
    return s1

```

```

def getTriangleFeatures(df):
    """
    Calculates Triangle perimeter and area between all possible triplets of points
    and stores the values in the data frame.
    RETURNS:
        - DataFrame
    """
    for comb in itertools.combinations(range(1,NPOINTS+1), 3):
        a = getSideLength(df,comb[0],comb[1])
        b = getSideLength(df,comb[0],comb[2])
        c = getSideLength(df,comb[1],comb[2])
        df[getPerimeterColname(comb)] = (a + b + c)

        s = df[getPerimeterColname(comb)] / 2
        df[getTAreaColname(comb)] = np.sqrt((s*(s-a)*(s-b)*(s-c)))

    return df

df_trainf = getTriangleFeatures(df_trainf)
df_testf = getTriangleFeatures(df_testf)

```

CPU times: user 6.51 s, sys: 0 ns, total: 6.51 s

Wall time: 6.51 s

In [858]: %%time

```

def getRidOfPointVars(df):
    """
    Drops the raw location points (they are not valuable features, we do not need them)
    RETURNS:
        - DataFrame
    """
    to_drop = []
    for p in range(1,NPOINTS+1):
        to_drop.append(getxLabel(p))
        to_drop.append(getyLabel(p))
    return df.drop(columns=to_drop)

df_trainf = getRidOfPointVars(df_trainf)
df_testf = getRidOfPointVars(df_testf)

print('TOTAL FEATURE COLUMNS:', len(df_trainf.columns))

#drop highly correlated features

# Compute the correlation matrix
corr = df_trainf.drop(columns=['label']).corr()

```

```

# Select upper triangle of correlation matrix
upper = corr.where(np.triu(np.ones(corr.shape), k=1).astype(np.bool))

# Find index of feature columns with correlation greater than 0.90 and drop them from
to_drop = [column for column in upper.columns if any(upper[column] > 0.90)]

df_trainf = df_trainf.drop(columns=to_drop)
df_testf = df_testf.drop(columns=to_drop)

feature_columns = df_trainf.drop(columns=['label']).columns
print('FEAT COLUMNS REMAINING:', len(feature_columns))

#Convert data to Numpy Arrays
y = df_trainf.label.values
X = df_trainf.drop(columns=['label']).values

y_test = df_testf.label.values
X_test = df_testf.drop(columns=['label']).values

```

```

TOTAL FEATURE COLUMNS: 4049
FEAT COLUMNS REMAINING: 460
CPU times: user 4.02 s, sys: 160 ms, total: 4.18 s
Wall time: 4.06 s

```

## 5 5. Classification (Modelling)

- Feature Scaling
- Feature selection / reduction
- Stratified Cross Validation
- Testing Classifiers / hyper parameter tuning

```

In [859]: #Copy training data into other variables
X_train, y_train = X, y

```

```

In [860]: %%time

```

```

#Import all classification and pre processing libraries we need
from sklearn import preprocessing
from sklearn.model_selection import GridSearchCV
from sklearn.pipeline import make_pipeline, Pipeline

from sklearn.svm import SVC, LinearSVC
from sklearn.utils.testing import ignore_warnings
from sklearn.exceptions import ConvergenceWarning

```

```

from sklearn.ensemble import RandomForestClassifier

from sklearn.cluster import KMeans
from sklearn.mixture import GaussianMixture
from sklearn.gaussian_process import GaussianProcessClassifier

from sklearn.metrics import make_scorer
from sklearn.metrics import accuracy_score, precision_score, recall_score

from sklearn.decomposition import PCA
from sklearn.feature_selection import SelectKBest, f_classif
from sklearn.gaussian_process.kernels import RBF

def get_name(estimator):
    name = estimator.__class__.__name__
    if name == 'Pipeline':
        name = [get_name(est[1]) for est in estimator.steps]
        name = ' + '.join(name)
    return name

```

CPU times: user 0 ns, sys: 0 ns, total: 0 ns

Wall time: 66.8  $\mu$ s

In [864]: %%time

```

#Define pipeline consisting of scaling, reduction, and classification
pipe = Pipeline([
    ('scaler', preprocessing.MinMaxScaler()),
    ('reduce_dim', PCA()),
    ('classify', LinearSVC())
])

#Create arrays of possible options for pipeline
scalers = [preprocessing.MinMaxScaler(), preprocessing.StandardScaler()]
classifiers = [LinearSVC(), SVC(gamma='scale'), RandomForestClassifier(), GaussianProcessClassifier()]
MAX_ITER_OPT = range(100, 1000, 100)
N_FEATURES_OPTIONS = [15, 20, 25, 30]
C_OPTIONS = np.logspace(-2, 7, 10)
n_estimators_opt = range(25, 75, 25)
max_depth_opt = range(2, 4, 1)
RANDOM_STATES = [0, 5, 42]

#Define the parameter grid for experimentation
#Joins together all appropriate combination of scaling, reduction/selection, and classification
param_grid = [
    #SVC Classifier options
    {

```



```

        'scaler': scalers,
        'reduce_dim': [PCA(iterated_power=7)],
        'reduce_dim__n_components': N_FEATURES_OPTIONS,
        'classify': classifiers[:2],
        'classify__C': C_OPTIONS
    },
    {
        'scaler': scalers,
        'reduce_dim': [SelectKBest(f_classif)],
        'reduce_dim__k': N_FEATURES_OPTIONS,
        'classify': classifiers[:2],
        'classify__C': C_OPTIONS
    },
    #Gaussian Process Classifier Option
    {
        'scaler': scalers,
        'reduce_dim': [PCA(iterated_power=7)],
        'reduce_dim__n_components': N_FEATURES_OPTIONS,
        'classify': classifiers[3:],
        'classify__random_state': RANDOM_STATES
    },
    {
        'scaler': scalers,
        'reduce_dim': [SelectKBest(f_classif)],
        'reduce_dim__k': N_FEATURES_OPTIONS,
        'classify': classifiers[3:],
        'classify__random_state': RANDOM_STATES
    },
    #Random Forest Classifier Options
    {
        'scaler': scalers,
        'reduce_dim': [PCA(iterated_power=7)],
        'reduce_dim__n_components': N_FEATURES_OPTIONS,
        'classify': classifiers[2:3],
        'classify__n_estimators': n_estimators_opt,
        'classify__max_depth': max_depth_opt,
    },
    {
        'scaler': scalers,
        'reduce_dim': [SelectKBest(f_classif)],
        'reduce_dim__k': N_FEATURES_OPTIONS,
        'classify': classifiers[2:3],
        'classify__n_estimators': n_estimators_opt,
        'classify__max_depth': max_depth_opt,
    },
]

#Define scoring metric

```

```

scoring = {'Accuracy': make_scorer(accuracy_score)}

#Create 5-fold classification cross validation grid
grid = GridSearchCV(pipe, cv=5, param_grid=param_grid,
                    scoring=scoring, refit='Accuracy',
                    return_train_score=True)

with ignore_warnings(category=ConvergenceWarning):
    grid.fit(X_train, y_train)

print("BEST CV SCORE:", grid.best_score_)
print("BEST CONFIGURATION:")
print(grid.best_params_)

#Save results into a dataframe locally
results_df = pd.DataFrame(grid.cv_results_)
results_df.to_pickle('results_df.pkl')

```

BEST CV SCORE: 0.98

BEST CONFIGURATION:

```

{'classify': SVC(C=10.0, cache_size=200, class_weight=None, coef0=0.0,
  decision_function_shape='ovr', degree=3, gamma='scale', kernel='rbf',
  max_iter=-1, probability=False, random_state=None, shrinking=True,
  tol=0.001, verbose=False), 'classify__C': 10.0, 'reduce_dim': SelectKBest(k=15, score_func=<
CPU times: user 2min 40s, sys: 3min 19s, total: 5min 59s
Wall time: 1min 13s

```

In [1040]: *#Outputting final results for train and test*

```

print("FINAL TRAIN SCORE:", grid.best_estimator_.score(X,y))
y_pred = grid.best_estimator_.predict(X)
df_train['label'] = y_pred

final_train_results = df_train.copy()
final_train_results['label'] = final_train_results['label'].map(lambda x: mapping_in
final_train_results.to_csv('trainfile_output.txt',sep=' ',index=False,header=False)
final_train_results.groupby('label').size().plot(kind='bar')
plt.show()

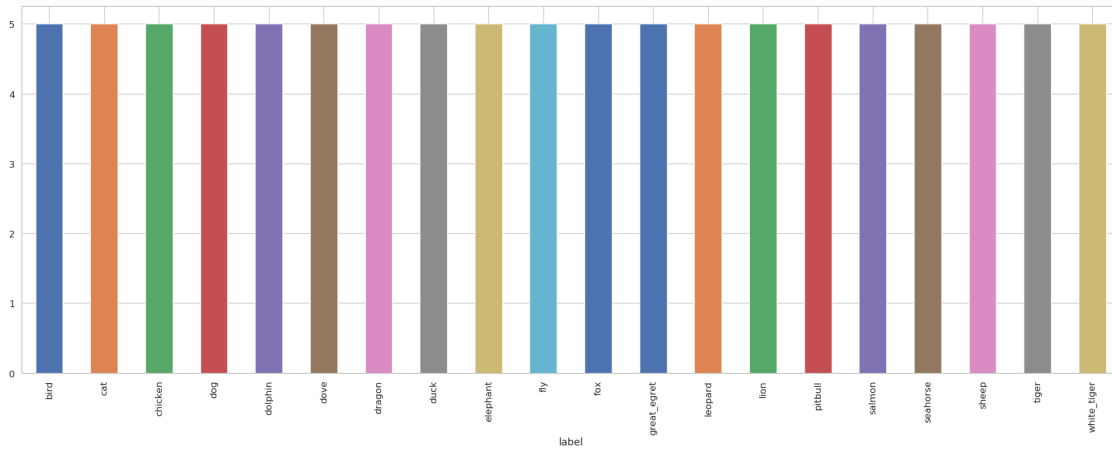
print("FINAL TRAIN CLASSIFICATION:")
y_test = grid.best_estimator_.predict(X_test)
df_test['label'] = y_test
df_testf['label'] = y_test

final_test_results = df_test.copy()
final_test_results['label'] = final_test_results['label'].map(lambda x: mapping_ind

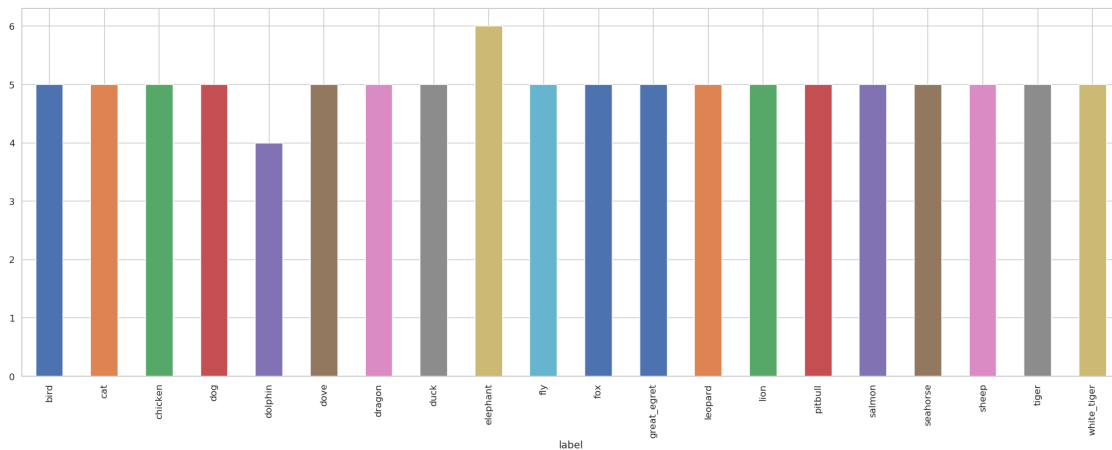
```

```
final_test_results.to_csv('testfile_output.txt',sep=' ',index=False,header=False)
final_test_results.groupby('label').size().plot(kind='bar')
plt.show()
```

FINAL TRAIN SCORE: 1.0



FINAL TRAIN CLASSIFICATION:



## 6. Communicating Results

- Discriminative Feature Correlation Plot
- 2D Representation of Classification Results for training and test
- plots to show model metrics across various classifiers

```

In [866]: results_df = pd.read_pickle('results_df.pkl')

In [867]: #Getting names of various components of the pipeline
results_df['param_classify_name'] = results_df['param_classify'].map(lambda x: get_name(x))
results_df['param_reduce_dim_name'] = results_df['param_reduce_dim'].map(lambda x: get_name(x))
results_df['param_scaler_name'] = results_df['param_scaler'].map(lambda x: get_name(x))
results_df['param_reduce_dim_n_components'] = results_df['param_reduce_dim_n_components'].fillna(results_df['param_reduce_dim_k'])
results_df['param_preprocess_name'] = results_df[['param_scaler_name', 'param_reduce_dim_name']].apply(lambda x: '+'.join(x), axis=1)

In [971]: #Printing top results for each combination of scaler, reducer, and classifier
results_df.groupby(['param_scaler_name',
                    'param_reduce_dim_name',
                    'param_classify_name'])['mean_test_Accuracy'].max().reset_index().sort_values(ascending=False)

Out[971]:
   param_scaler_name param_reduce_dim_name param_classify_name \
7      MinMaxScaler      SelectKBest      SVC
15     StandardScaler      SelectKBest      SVC
4      MinMaxScaler      SelectKBest  GaussianProcessClassifier
5      MinMaxScaler      SelectKBest      LinearSVC
12     StandardScaler      SelectKBest  GaussianProcessClassifier
13     StandardScaler      SelectKBest      LinearSVC
1      MinMaxScaler              PCA      LinearSVC
3      MinMaxScaler              PCA      SVC
9      StandardScaler              PCA      LinearSVC
0      MinMaxScaler              PCA  GaussianProcessClassifier
11     StandardScaler              PCA      SVC
6      MinMaxScaler      SelectKBest  RandomForestClassifier
14     StandardScaler      SelectKBest  RandomForestClassifier
10     StandardScaler              PCA  RandomForestClassifier
2      MinMaxScaler              PCA  RandomForestClassifier
8      StandardScaler              PCA  GaussianProcessClassifier

   mean_test_Accuracy
7                    0.98
15                   0.98
4                    0.97
5                    0.96
12                   0.96
13                   0.95
1                    0.92
3                    0.92
9                    0.92
0                    0.91
11                   0.89
6                    0.88
14                   0.84

```

10	0.82
2	0.76
8	0.47

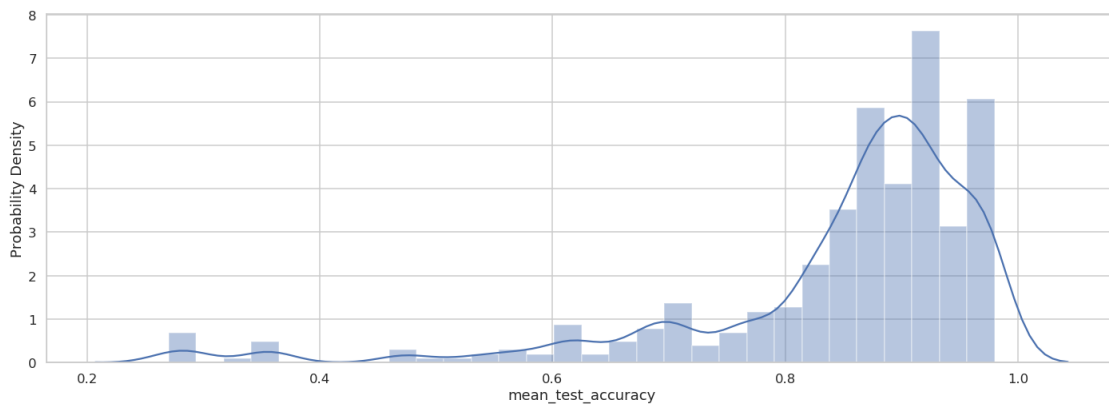
```
In [884]: #Accuracy Distribution
sns.set_style('whitegrid')
sns.despine(left=True)
sns.set_context("talk")

fig, ax = plt.subplots((1), figsize=(24,8))
for metric in ['mean_test_Accuracy']:
    sns.distplot(results_df[metric],label=metric, ax=ax)

ax.set_xlabel('mean_test_accuracy')
ax.set_ylabel('Probability Density')

plt.show()
```

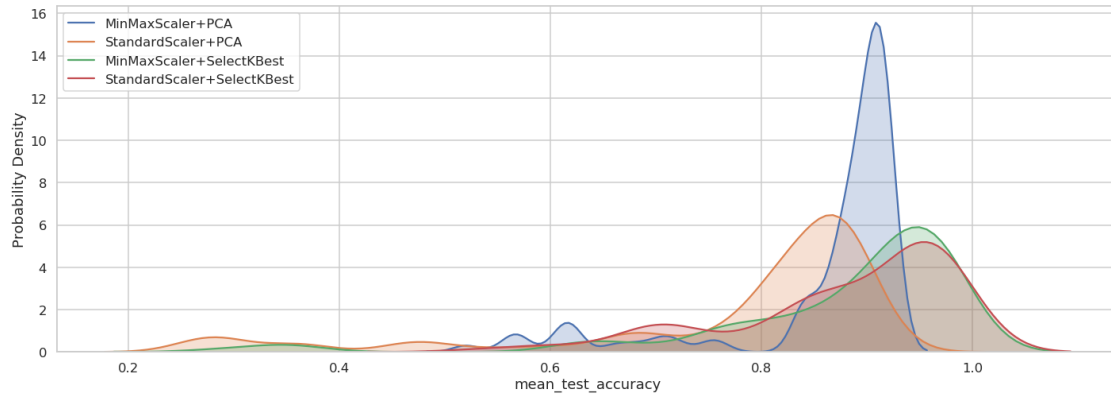
<Figure size 1152x864 with 0 Axes>



```
In [883]: #Accuracy Distribution for each PreProcessor
fig, ax = plt.subplots((1), figsize=(24,8))
for label in results_df['param_preprocess_name'].unique():
    print(label)
    mask = results_df['param_preprocess_name']==label
    # sns.distplot(results_df[mask]['mean_test_Precision'], bins=5,
    #               kde=True, rug=False, norm_hist=True,label=label, ax=ax)
    sns.kdeplot(results_df[mask]['mean_test_Accuracy'],shade=True,label=label, ax=ax)

ax.set_xlabel('mean_test_accuracy')
ax.set_ylabel('Probability Density')
plt.show()
```

MinMaxScaler+PCA  
StandardScaler+PCA  
MinMaxScaler+SelectKBest  
StandardScaler+SelectKBest

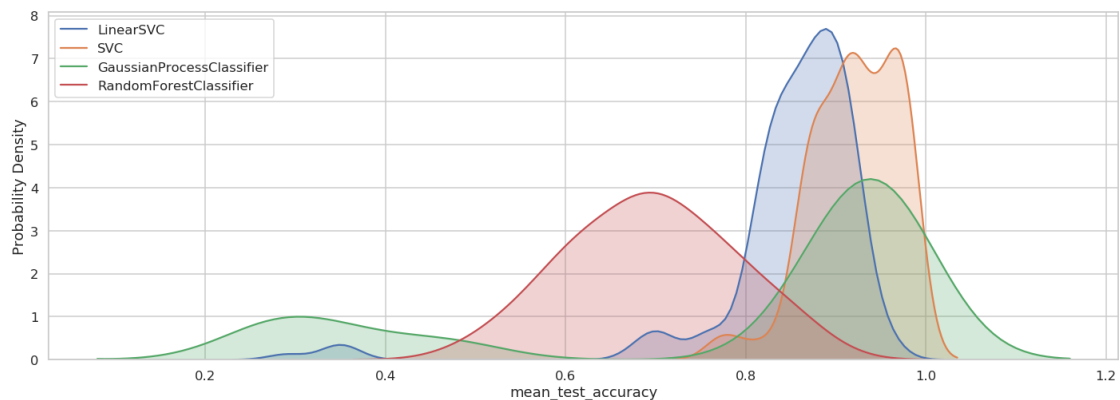


```
In [882]: #Accuracy Distributions for each classifier
fig, ax = plt.subplots((1), figsize=(24,8))
for label in results_df['param_classify_name'].unique():
    print(label)
    mask = results_df['param_classify_name']==label

    sns.kdeplot(results_df[mask]['mean_test_Accuracy'],shade=True,label=label, ax=ax)

    ax.set_xlabel('mean_test_accuracy')
    ax.set_ylabel('Probability Density')
plt.show()
```

LinearSVC  
SVC  
GaussianProcessClassifier  
RandomForestClassifier



```

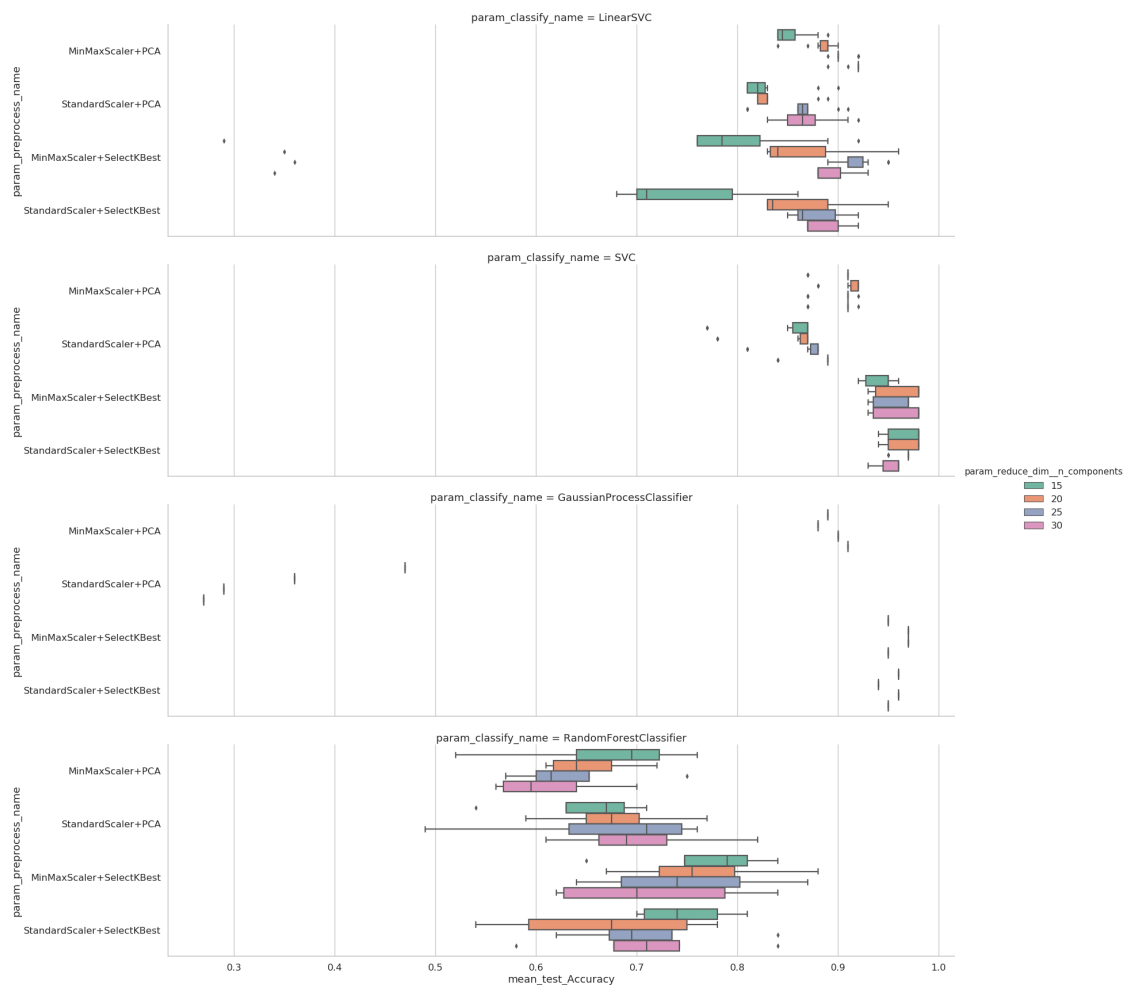
In [881]: #Detailed Box Chart
plt.rcParams['figure.figsize'] = [16,12]
sns.set_style('whitegrid')
sns.despine(left=True)
sns.set_context("talk")

g = sns.catplot(x="mean_test_Accuracy", y="param_preprocess_name", row="param_classify_name",
#               col='param_scaler_name',param_preprocess_name
               hue="param_reduce_dim_n_components",
               kind="box", orient="h", height=6.0, aspect=4,
               data=results_df,
               palette="Set2",dodge=True)

plt.show()

```

<Figure size 1152x864 with 0 Axes>



```

In [986]: #Finding top discriminative features by the best classifier
          scaler = grid.best_estimator_.named_steps.scaler
          reduce_dim = grid.best_estimator_.named_steps.reduce_dim
          X_train, y_train = X, y
          X_val, y_val = X, y

          X_train = scaler.transform(X_train)
          X_train = reduce_dim.transform(X_train)

          X_test = scaler.transform(X_test)
          X_test = reduce_dim.transform(X_test)

          print(X_train.shape,X_val.shape,X_test.shape)

          print("COLUMNS SELECTED:")
          final_feature_list = df_trainf.drop(columns=['label']).loc[:,reduce_dim.get_support()]
          final_feature_list

(100, 15) (100, 460) (100, 15)
COLUMNS SELECTED:

```

```

Out[986]: ['01_e_19',
           '01_e_20',
           '04_e_06',
           '06_e_08',
           '08_e_10',
           '12_e_14',
           '14_e_16',
           '16_e_19',
           'TA_01_08_09',
           'TA_01_12_13',
           'TA_01_16_17',
           'TA_01_21_22',
           'TA_04_06_10',
           'TA_08_10_14',
           'TA_08_19_21']

```

```

In [904]: #Displaying correlation matrix of top features

          sns.set(style="white")

          # Compute the correlation matrix
          # corr = df_trainf.drop(columns=['label']).loc[:,model.get_support()].corr()
          corr = df_trainf[final_feature_list].corr()

```



```

# Generate a mask for the upper triangle
mask = np.zeros_like(corr, dtype=np.bool)
mask[np.triu_indices_from(mask)] = True

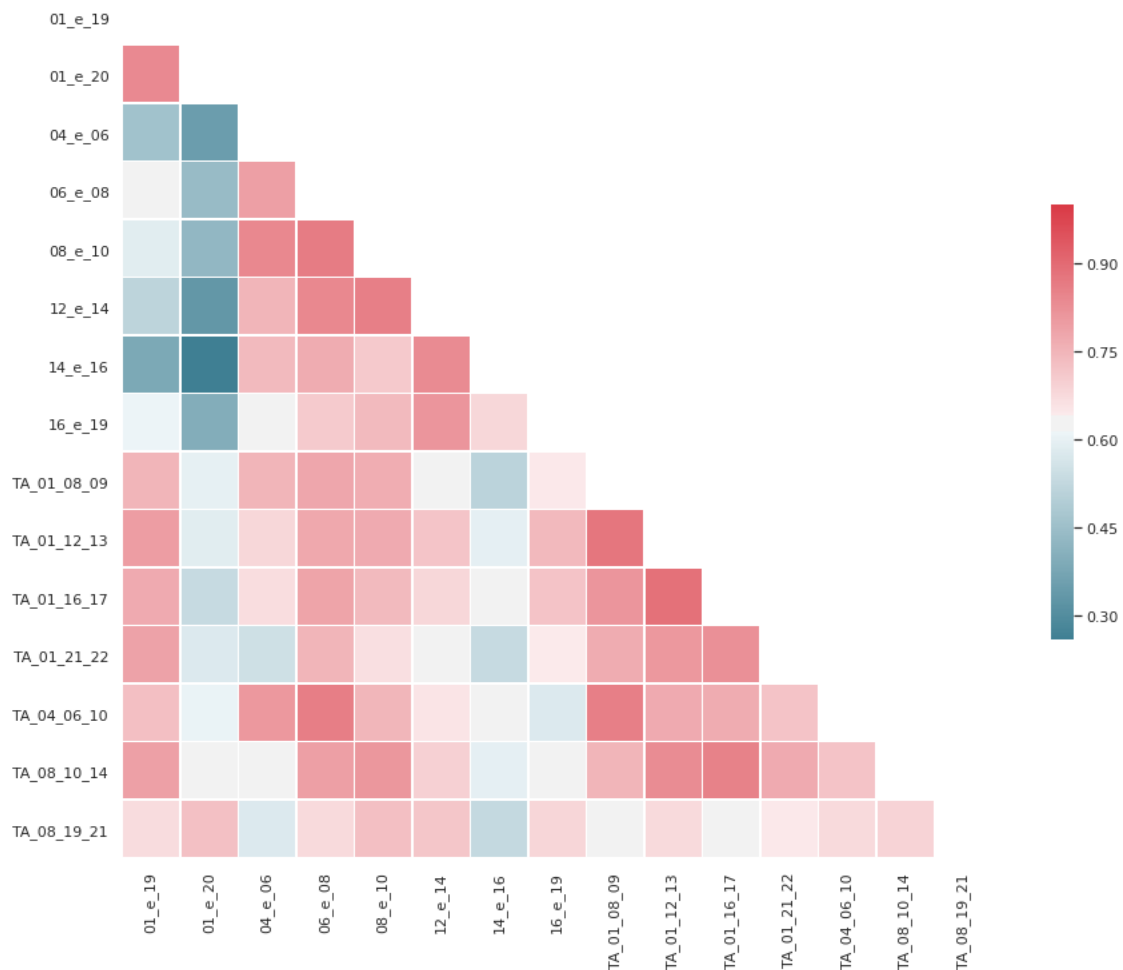
# Set up the matplotlib figure
f, ax = plt.subplots(figsize=(16, 12))

# Generate a custom diverging colormap
cmap = sns.diverging_palette(220, 10, as_cmap=True)

# Draw the heatmap with the mask and correct aspect ratio
sns.heatmap(corr, mask=mask, cmap=cmap, vmax=1.0, vmin=corr.min().min(),
            square=True, linewidths=.5, cbar_kws={"shrink": .5})

```

Out[904]: <matplotlib.axes.\_subplots.AxesSubplot at 0x7fa5eb02e0f0>



```

In [825]: # bokeh basics library load
from bokeh.plotting import figure, output_notebook, show

```

```

from bokeh.models import ColumnDataSource, LabelSet, Label, LinearColorMapper, LogCo
from bokeh.models.tools import HoverTool
from bokeh.transform import dodge, factor_cmap, transform
from bokeh.palettes import PuBu,Spectral, Paired, Oranges, Greens, GnBu3, OrRd3, Pur
output_notebook()

```

In [1004]: *#Display clustered results*

```

from sklearn.manifold import Isomap

def dt_scatter(source,title='Cluster Topic Plot',labelsFlag=False,csize=8):
    # Create a blank figure with labels
    p = figure(plot_width = 950, plot_height = 600,
               title = title,
               x_axis_label = 'X', y_axis_label = 'Y',
    #               y_axis_type="log", x_axis_type="log",
               tools=('pan, box_zoom, reset,save, wheel_zoom,hover')
               )

    colours = list((Category20c[source['label'].astype(int).max()+1]))
    source['color'] = source['label'].apply(lambda x: colours[int(x)])

    p.circle(x='x', y='y',
             source=source[source['type']=='TRAIN'],
             size=csize,
             color='color',
             legend='labelName',
             alpha=0.8)

    p.square(x='x', y='y',
             source=source[source['type']=='TEST'],
             size=csize,
             color='color',
    #             legend='labelName',
             alpha=0.8)

    if labelsFlag:
        labels = LabelSet(x='x', y='y', text='labelName',
                          x_offset=2, y_offset=2, source=ColumnDataSource(source),
                          text_font_size='7pt')

        p.add_layout(labels)

    p.hover.tooltips = [(c,'@'+c) for c in source.columns]

```

```

    # configure visual elements of the plot
    p.title.text_font_size = '10pt'
    p.xaxis.visible = False
    p.yaxis.visible = False
    p.legend.label_text_font_size = "5pt"
    p.legend.location = "top_right"
    p.legend.background_fill_alpha = 0.8

    p.legend.spacing = 0
    p.legend.padding = 0
    p.legend.margin = 0
    #     p.grid.grid_line_color = None
    #     p.outline_line_color = None

    #     # Show the plot
    show(p)
    return

df_trainf['labelName'] = df_trainf['label'].map(lambda x: mapping_index[x])
df_testf['labelName'] = df_testf['label'].map(lambda x: mapping_index[x])
df_trainf['color'] = Paired[4][0]
df_testf['color'] = Paired[4][-1]

df_trainf['type'] = 'TRAIN'
df_testf['type'] = 'TEST'

displaydf = pd.concat([df_trainf, df_testf], ignore_index=True).reset_index()

displaydf.loc[:df_trainf.shape[0]-1,final_feature_list] = X_train
displaydf.loc[df_trainf.shape[0]:,final_feature_list] = X_test

#Reduce feature set into 2D
n_iter=1000
red_model = TSNE(n_components=2, n_iter=n_iter, learning_rate=20)

r_matrix = red_model.fit_transform(displaydf[final_feature_list].values)
displaydf['x'] = r_matrix[:,0]
displaydf['y'] = r_matrix[:,1]

#Plot scatter plot
dt_scatter(displaydf[['label','labelName','x','y','type','color'] + final_feature_list],
            csize=15,
            labelsFlag=True)

```

/opt/conda/lib/python3.6/site-packages/ipykernel\_launcher.py:13: SettingWithCopyWarning:  
A value is trying to be set on a copy of a slice from a DataFrame.  
Try using .loc[row\_indexer,col\_indexer] = value instead

See the caveats in the documentation: <http://pandas.pydata.org/pandas-docs/stable/indexing.html>  
del sys.path[0]

```
In [1031]: # Display each variables profile across classes
df_scaled_train = pd.DataFrame(X_train, columns=final_feature_list)

df_scaled_train['labelName'] = df_trainf['labelName']

plotdf = pd.melt(df_scaled_train, id_vars=['labelName'], value_vars=final_feature_list)

plt.rcParams['figure.figsize'] = [35,12]
sns.set_style('whitegrid')
sns.despine(left=True)
sns.set_context("poster")

clr_pal = sns.color_palette("muted", n_colors=10) + sns.color_palette("colorblind",

g = sns.catplot(x="variable", y="value", hue="labelName",
#             col='param_scaler_name',param_preprocess_name
#             hue="variable",
            row='labelName',
            kind="point", orient="v", height=5.0, aspect=3,
            data=plotdf,
            palette=clr_pal,dodge=False,
            ci='sd',join=True,errwidth=1.0,
#             cut=0
            )

plt.show()
```

<Figure size 2520x864 with 0 Axes>

