

① H_0 There is NO significant difference in the variance of the Population and Sample

H_1 There is a significant difference in the variance of Population and Sample

V_1	V_1^2	V_2	V_2^2	V_3	V_3^2
27	729	63	3969	52	2704
43	1849	43	1849	60	3600
64	4096	52	2704	37	1369
62	3844	58	3364	40	1600
34	1156	54	2916	23	529
54	2916	50	2500	39	1521
57	3249	65	4225	55	3025
49	2401	53	2809	52	2704
31	961	43	1849	43	1849
69	4761	49	2401	49	2401
500	250000	530	280900	440	193600

$$\text{Correction Term } C_2 = \frac{\sum (V_i)^2}{N} = \frac{(500 + 530 + 440)^2}{30}$$

$$C_2 = 72030$$

Sum of Squares of Total

$$SST = \sum x^2 - C_2 = 26742 + 28586 + 20420 - 72030$$

$$SST = 3720$$

Sum of Squares among groups

$$SS_A = \frac{(\sum x^2)}{N} - Cx$$

$$= \frac{500^2}{10} + \frac{(530)^2}{10} + \frac{(440)^2}{10} - 72030$$

$$= 25000 + 28090 + 19360 - 72030$$

$$SS_A = 420$$

Sum of Squares within groups

$$SS_W = SS_T - SS_A$$

$$= 3720 - 420$$

$$SS_W = 3300$$

mean Sum of Squares among groups

$$MSS_A = \frac{SS_A}{K-1} = \frac{420}{10-1} = \frac{420}{9}$$

$$MSS_A = 46.667$$

Mean Sum of Squares within group

$$MSS_W = \frac{SS_W}{N-K} = \frac{3300}{30-3}$$

$$= \frac{3300}{27} = \frac{1100}{9}$$

$$MSS_W = 122.22$$

$$F_{calc} = \frac{MSS_W}{MSS_A} = \frac{122.22}{46.667}$$

$$F_{calc} = 2.619$$

Source of Variation	df	SS	MSS	F-value
Among groups	3-1=2	420	46.67	2.619
Within group	30-3=27	3300	122.22	

$$df (27, 2) = 5.49 \text{ (table)}$$

$F_{calc} > F_{crit}$ H_0 is accepted -

2)

H_0 - There is no difference in Rate of Return

H_1 - There is a significant difference in rate of Return

Finance	
x	x^2
10.76	115.7
5.05	226.50
7.01	289.34
5.07	25.7
19.5	380.25
8.16	66.58
10.38	107.74
6.75	45.56
72.62	1257.47

Energy	
x	x^2
12.72	161.79
13.91	193.48
6.43	41.34
11.19	125.21
18.79	353.06
20.73	429.73
9.6	92.16
17.4	302.7
110.77	1699.56

Chemical	
x	x^2
11.88	141.13
5.86	34.33
13.46	181.17
9.9	98.01
3.95	15.60
3.44	11.83
7.11	50.55
15.7	246.49
71.3	779.13

Correction Term

$$C_x = \frac{(\sum x)^2}{N} = \frac{(92.68 + 110.77 + 71.3)^2}{24} = 3145.31$$

Sum of Square of Total SST:

$$\sum x^2 - C_x = 1257.46 + 1699.56 + 779.13 - 3145.31$$

$$SST = 590.85$$

Sum of Square among group SSA:

$$= \frac{(\sum x^2)}{N} - C_x$$

$$= \frac{92.68^2}{10} + \frac{110.77^2}{10} + \frac{71.3^2}{10} - 3145.31$$

$$SSA = 7452.6$$

Sum of square within group: SSW

$$= SS_T - SSA$$

$$= 7452.69 - 590.85$$

$$SSW = 6861.83$$

mean of square among the group MSA

$$MSA = \frac{SSA}{N-1} = \frac{590.85}{8-1} = 84.4$$

$$MSW = \frac{SSW}{Total - K} = \frac{7452.69}{24-3} = 354.9$$

$$F_{ratio} = \frac{MSW}{MSA} = \frac{354.9}{84.4}$$

$$F_{ratio} = 4.204$$

Sum of Variance	df	SS	MS	F-ratio
Among group	8-1=7	7452.7	84.40	4.204
within group	24-3=21	6861.83	354.89	F _{crit}

$$df(21, 7) = 3.64 (F_{tab})$$

H_0 is Rejected and H_1 is accepted

3) H_0 = population variance = sample variance
 H_1 = POP. variance \neq Sample variance

$$F = \frac{s_1^2}{s_2^2}$$

$$F = \frac{0.718}{0.6198} = 1.1588$$

$$df_1 = 10 - 1 = 9$$

$$df_2 = 10 - 1 = 9$$

$$F_{tab} = 5.35 \quad F_{cal} = 1.1588$$

$$F_{tab} > F_{cal}$$

So, H_0 is accepted

X — X

$$4) \quad H_0: \mu = 100 \quad H_1: \mu \neq 100$$

$$\text{mean } \bar{x} = 100.83$$

$$s \text{ (S.D.)} = 1.7573, \quad n = 10, \quad v = 10 - 1 = 9$$

$$\text{At Level } 95\%, \quad \alpha = 0.05, \quad \frac{\alpha}{2} = 0.025$$

$$\bar{x} - t_{n-1, \alpha/2} \frac{s}{\sqrt{n}} \leq \mu \leq \bar{x} + t_{n-1, \alpha/2} \frac{s}{\sqrt{n}}$$

$$100.83 - 2.262 \times \frac{1.7573}{\sqrt{10}} \leq \mu \leq 100.83 + 2.262 \times \frac{1.7573}{\sqrt{10}}$$

$$100.83 - 1.279 \leq \mu \leq 100.83 + 1.279$$

$$99.5 \leq \mu \leq 102.1$$

The mean is 100 and 90% of confident average speed batch of cars b/w 99.5 and 102.1 mph.

$$H_0 = \mu = 105$$

$$H_1 = \mu \neq 105$$

$$\bar{x} = 125$$

$$s = 14$$

$$n = 25$$

$$d.f = 24 - 1 = 24$$

$$\alpha = 95\%$$

$$t = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}} \Rightarrow \frac{125 - 105}{14/\sqrt{25}}$$

$$t = \frac{20}{2.8} = 7.14$$

$$t_{tab} = 9.064, t_{cal} = 7.14$$

$$t_{cal} > t_{tab}$$

b) Null hypothesis $H_0: \mu = 13$
Alternate hypothesis $H_1: \mu \neq 13$

DATA'S

$$\bar{x} = 15.5$$

$$\mu_0 = 13$$

$$n = 169$$

$$\sigma = 13$$

$$Z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$$

$$Z = \frac{15.5 - 13}{13 / \sqrt{169}} = 2.15$$

$Z > 1.96$ Null Hypothesis Rejected