7

Problems on Numbers

In this chapter, questions involving a set of numbers are put in the form of a puzzle. You have to analyse the given conditions, assume the unknown numbers and form equations accordingly, which on solving yield the unknown numbers.

SOLVED EXAMPLES

- Ex. 1. A number is as much greater than 36 as is less than 86. Find the number.
- **Sol.** Let the number be x. Then, $x 36 = 86 x \Rightarrow 2x = 86 + 36 = 122 \Rightarrow x = 61$. Hence, the required number is 61.
- Ex. 2. Find a number such that when 15 is subtracted from 7 times the number, the result is 10 more than twice the number.

 (Hotel Management, 2002)
 - **Sol.** Let the number be x. Then, $7x 15 = 2x + 10 \Rightarrow 5x = 25 \Rightarrow x = 5$. Hence, the required number is 5.
- Ex. 3. The sum of a rational number and its reciprocal is $\frac{13}{6}$. Find the number.
- **Sol.** Let the number be x. Then,

$$x + \frac{1}{x} = \frac{13}{6} \implies \frac{x^2 + 1}{x} = \frac{13}{6} \implies 6x^2 - 13x + 6 = 0 \implies 6x^2 - 9x - 4x + 6 = 0$$
$$\implies (3x - 2)(2x - 3) = 0 \implies x = \frac{2}{3} \text{ or } x = \frac{3}{2}.$$

Hence, the required number is $\frac{2}{3}$ or $\frac{3}{2}$.

- Ex. 4. The sum of two numbers is 184. If one-third of the one exceeds one-seventh of the other by 8, find the smaller number.

 (Bank Recruitment, 2011)
 - **Sol.** Let the numbers be x and (184 x). Then,

$$\frac{x}{3} - \frac{(184 - x)}{7} = 8 \implies 7x - 3(184 - x) = 168 \implies 10x = 720 \implies x = 72.$$

So, the numbers are 72 and 112. Hence, smaller number = 72.

- Ex. 5. The difference of two numbers is 11 and one-fifth of their sum is 9. Find the numbers.
- **Sol.** Let the numbers be x and y. Then

$$x - y = 11 \tag{...(i)}$$

and
$$\frac{1}{5}(x+y) = 9 \implies x+y = 45$$
 ...(ii)

Adding (i) and (ii), we get : 2x = 56 or x = 28.

Putting x = 28 in (i), we get : y = 17.

Hence, the numbers are 28 and 17.

- Ex. 6. If the sum of two numbers is 42 and their product is 437, then find the absolute difference between the numbers.

 (S.S.C., 2003; B.Ed., 2010)
- **Sol.** Let the numbers be x and y. Then, x + y = 42 and xy = 437.

$$x - y = \sqrt{(x + y)^2 - 4xy} = \sqrt{(42)^2 - 4 \times 437} = \sqrt{1764 - 1748} = \sqrt{16} = 4.$$

 \therefore Required difference = 4.

Ex. 7. If the sum of two numbers is 10 and the sum of their reciprocals is $\frac{5}{12}$, find the numbers. (P.C.S., 2006)

Sol. Let the numbers be x and y.

Then,
$$x + y = 10$$
 ...(*i*)

And,
$$\frac{1}{x} + \frac{1}{y} = \frac{5}{12}$$
 $\Rightarrow \frac{x+y}{xy} = \frac{5}{12} \Rightarrow xy = \frac{10 \times 12}{5} = 24$...(ii)

$$\therefore x - y = \sqrt{(x+y)^2 - 4xy} = \sqrt{(10)^2 - 4 \times 24} = \sqrt{100 - 96} = \sqrt{4} = 2 \Rightarrow x - y = 2 \qquad \dots(iii)$$

Adding (i) and (iii), we get: 2x = 12 or x = 6.

Putting x = 6 in (i), we get: y = 4.

Hence, the required numbers are 6 and 4.

Ex. 8. Three numbers are in the ratio 3:2:5. The sum of their squares is 1862. Find the numbers. (R.R.B., 2007) Sol. Let the numbers be 3x, 2x and 5x.

Then,
$$(3x)^2 + (2x)^2 + (5x)^2 = 1862 \Rightarrow 9x^2 + 4x^2 + 25x^2 = 1862$$

 $\Rightarrow 38x^2 = 1862 \Rightarrow x^2 = \frac{1862}{38} = 49 \Rightarrow x = \sqrt{49} = 7.$

Hence, the numbers are 21, 14 and 35.

Ex. 9. The sum of seven consecutive natural numbers is 1617. How many of these numbers are prime? (S.S.C., 2006)

Sol. Let the seven consecutive numbers be x, (x + 1), (x + 2), (x + 3), (x + 4), (x + 5) and (x + 6).

Then,
$$x + (x + 1) + (x + 2) + (x + 3) + (x + 4) + (x + 5) + (x + 6) = 1617$$

 $\Rightarrow 7x + 21 = 1617 \Rightarrow 7x = 1596 \Rightarrow x = 228.$

Thus, the numbers are 228, 229, 230, 231, 232, 233 and 234.

Of these numbers, only two numbers i.e. 229 and 233, are prime.

Ex. 10. The product of two consecutive numbers is 4032. Find the numbers. (Bank P.O., 2008)

Sol. Let the numbers be x and (x + 1).

Then,
$$x(x + 1) = 4032 \Rightarrow x^2 + x - 4032 = 0 \Rightarrow x^2 + 64x - 63x - 4032 = 0$$

$$\Rightarrow x(x + 64) - 63(x + 64) = 0 \Rightarrow (x + 64) (x - 63) = 0$$

$$\Rightarrow x = 63.$$
 [:: $x \neq -64$]

Hence, the required numbers are 63 and 64.

Ex. 11. The sum of two numbers is 15 and the sum of their squares is 113. Find the numbers. (R.R.B., 2006) Sol. Let the numbers be x and (15 - x).

Then,
$$x^2 + (15 - x)^2 = 113 \Rightarrow x^2 + 225 + x^2 - 30x = 113$$

$$\Rightarrow 2x^2 - 30x + 112 = 0 \Rightarrow x^2 - 15x + 56 = 0$$

$$\Rightarrow (x - 7)(x - 8) = 0 \Rightarrow x = 7 \text{ or } x = 8.$$

So, the numbers are 7 and 8.

Ex. 12. The average of four consecutive even numbers is 27. Find the largest of these numbers.

Sol. Let the four consecutive even numbers be x, x + 2, x + 4 and x + 6.

Then, sum of these numbers = $(27 \times 4) = 108$.

So,
$$x + (x + 2) + (x + 4) + (x + 6) = 108$$
 or $4x = 96$ or $x = 24$.

 \therefore Largest number = (x + 6) = 30.

Ex. 13. The sum of the squares of three consecutive odd numbers is 2531. Find the numbers. (R.R.B., 2010)

Sol. Let the numbers be x, x + 2 and x + 4.

Then,
$$x^2 + (x + 2)^2 + (x + 4)^2 = 2531 \Rightarrow 3x^2 + 12x - 2511 = 0 \Rightarrow x^2 + 4x - 837 = 0$$

 $\Rightarrow (x - 27)(x + 31) = 0 \Rightarrow x = 27.$

Hence, the required numbers are 27, 29 and 31.

- Ex. 14. Of two numbers, 4 times the smaller one is less than 3 times the larger one by 5. If the sum of the numbers is larger than 6 times their difference by 6, find the two numbers.
 - **Sol.** Let the numbers be x and y, such that x > y.

Then,
$$3x - 4y = 5$$
 ...(*i*)

and
$$(x + y) - 6(x - y) = 6 \implies -5x + 7y = 6$$
 ...(ii)

Solving (i) and (ii), we get : x = 59 and y = 43.

Hence, the required numbers are 59 and 43.

- Ex. 15. The ratio between a two-digit number and the sum of the digits of that number is 4:1. If the digit in the unit's place is 3 more than the digit in the ten's place, what is the number? (S.B.I.P.O., 2005)
 - **Sol.** Let the ten's digit be x. Then, unit's digit = (x + 3).

Sum of the digits = x + (x + 3) = 2x + 3. Number = 10x + (x + 3) = 11x + 3.

$$\therefore \frac{11x+3}{2x+3} = \frac{4}{1} \Leftrightarrow 11x+3 = 4(2x+3) \Leftrightarrow 3x = 9 \Leftrightarrow x = 3.$$

Hence, required number = 11x + 3 = 36.

- Ex. 16. A number consists of two digits. The sum of the digits is 9. If 63 is subtracted from the number, its digits are interchanged. Find the number.
 - **Sol.** Let the ten's digit be x. Then, unit's digit = (9 x).

Number = 10x + (9 - x) = 9x + 9.

Number obtained by reversing the digits = 10 (9 - x) + x = 90 - 9x.

$$\therefore (9x+9)-63=90-9x \Leftrightarrow 18x=144 \Leftrightarrow x=8.$$

So, ten's digit = 8 and unit's digit = 1.

Hence, the required number is 81.

- Ex. 17. In a three-digit number, the digit in the units place is four times the digit in the hundreds place. If the digits in the units place and the tens place are interchanged, the new number so formed is 18 more than the original number. If the digit in the hundreds place is one-third of the digit in the tens place, what is the original number? (L.I.C., 2005)
 - **Sol.** Let the digit in the hundreds place be x.

Then, digit in the units place = 4x. And, digit in the tens place = 3x.

Original number = $100x + 10 \times 3x + 4x = 100x + 30x + 4x = 134x$.

Number formed on interchanging the unit's and ten's digits

$$= 100x + 10 \times 4x + 3x = 143x.$$

$$\therefore 143x - 134x = 18 \Leftrightarrow 9x = 18 \Leftrightarrow x = 2.$$

Hence, original number = $134x = (134 \times 2) = 268$.

- Ex. 18. If the digits of a two-digit number are interchanged, the number formed is greater than the original number by 45. If the difference between the digits is 5, what is the original number? (Bank P.O., 2009)
 - **Sol.** Since the number formed by interchanging the digits is greater so the ten's digit of the original number is smaller than the unit's digit.

Let the ten's digit be x. Then, unit's digit = x + 5.

Original number = 10x + (x + 5) = 11x + 5.

Number formed on interchanging the digits = 10(x + 5) + x = 11x + 50.

 $\therefore (11x + 50) - (11x + 5) = 45 \Rightarrow 45 = 45, \text{ which is independent of } x.$

Hence, the number cannot be determined from the given data.

Ex. 19. A fraction becomes $\frac{2}{3}$ when 1 is added to both its numerator and denominator. And, it becomes $\frac{1}{2}$ when

1 is subtracted from both the numerator and denominator. Find the fraction.

Sol. Let the required fraction be $\frac{x}{y}$. Then,

$$\frac{x+1}{y+1} = \frac{2}{3} \implies 3x - 2y = -1$$
 ...(i) and $\frac{x-1}{y-1} = \frac{1}{2} \implies 2x - y = 1$...(i)

Solving (i) and (ii), we get : x = 3, y = 5.

 $\therefore \text{ Required fraction} = \frac{3}{5}$

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Ex. 20. 50 is divided into two parts such that the sum of their reciprocals is $\frac{1}{12}$. Find the two parts.

Sol. Let the two parts be x and (50 - x).

Then,
$$\frac{1}{x} + \frac{1}{50 - x} = \frac{1}{12} \implies \frac{50 - x + x}{x(50 - x)} = \frac{1}{12} \implies x^2 - 50x + 600 = 0$$

 $\implies (x - 30) (x - 20) = 0 \implies x = 30 \text{ or } x = 20.$

So, the parts are 30 and 20.

Ex. 21. If three numbers are added in pairs, the sums equal 10, 19 and 21. Find the numbers.

Sol. Let the numbers be x, y and z. Then,

Adding (i), (ii) and (iii), we get: 2(x + y + z) = 50 or (x + y + z) = 25.

Thus,
$$x = (25 - 19) = 6$$
; $y = (25 - 21) = 4$; $z = (25 - 10) = 15$.

Hence, the required numbers are 6, 4 and 15.

EXERCISE

(OBJECTIVE TYPE QUESTIONS)

Directions: Mark (\checkmark) against the correct answer:

- **1.** By how much is $\frac{3}{4}$ th of 568 lesser than $\frac{7}{8}$ th of 1008?
 - (Bank P.O., 2008)

- (a) 444
- (b) 448
- (c) 452
- (d) 456
- (e) None of these
- 2. The difference between a number and its three-fifths is 50. What is the number?
 - (a) 75

- (b) 100
- (c) 125
- (d) None of these
- 3. If a number is added to two-fifths of itself, the value so obtained is 455. What is the number?

(Bank Recruitment, 2010)

- (a) 325
- (b) 350
- (c) 400
- (d) 420
- (e) None of these
- 4. If a number is multiplied by two-thirds of itself the value so obtained is 864. What is the number?

(Bank Recruitment, 2010)

(a) 34

- (b) 36
- (c) 38
- (d) 44
- (e) 46
- 5. If a number is decreased by 4 and divided by 6, the result is 8. What would be the result if 2 is subtracted from the number and then it is divided by 5?
- (c) $10\frac{1}{5}$
- (d) $11\frac{1}{5}$
- (e) None of these

- 6. A number when multiplied by 13 is increased by 180. The number is (P.C.S., 2004)
 - (a) 5

- (b) 12
- (c) 15

- (d) 45
- 7. The sum of twice a number and three times of 42 is 238. What is the sum of thrice the number and two times of 42? (Bank P.O., 2010)
 - (a) 245
- (b) 250
- (c) 252
- (d) 264
- (e) None of these
- 8. If one-third of one-fourth of a number is 15, then three-tenths of that number is
 - (a) 35

- (c) 45 (d) 54 9. The difference between $\frac{3}{5}$ th of $\frac{2}{3}$ rd of a number

and $\frac{2}{5}$ th of $\frac{1}{4}$ th of the same number is 288. What

- is the number?
- (Bank P.O., 2006)

- (a) 850
- (b) 895
- (c) 955
- (d) 96010. A number is doubled and 9 is added. If the resultant
- is trebled, it becomes 75. What is that number?
 - (c) 8

- (d) None of these
- 11. Three-fourth of a number is 60 more than its onethird. The number is
 - (a) 84
- (b) 108
- (c) 144
- (d) None of these
- 12. A number whose fifth part increased by 4 is equal to its fourth part diminished by 10, is (SNAP, 2010)
 - (a) 240
- (b) 260
- (c) 270
- (d) 280

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13.	When 24 is subtracted from	om a number, it reduces		(a) 240	((b) 288	
	to its four-seventh. What			(c) 384	((d) 480	
	of that number?		23.	One-third of a two	-digit nur	mber exceeds	one-fourth
	(a) 1	(b) 9		of its successive n	umber by	1. The num	ber is
	(c) 11	(d) Data inadequate		(a) 12	((b) 15	
	(e) None of these			(c) 18		(d) 21	
14.	Find the number which v increased by 196.	when multiplied by 15 is (L.I.C., 2003)	24.	If the sum of a nu is the number?	mber and	l its square i	s 182, what
	(a) 14	(b) 20		(a) 15	((b) 26	
	(c) 26	(d) 28		(c) 28	((d) 91	
15.	If a number, when divide the number is	d by 4, is reduced by 21,	25.	(e) None of these If (73) ² is subtracted	ed from t	he square of	a number,
	(a) 18	(b) 20		the answer so obtain	ined is 50	75. What is t	he number?
	(c) 28	(d) 38		() 06			.A.D.O., 2007)
16.	A number whose fifth par	t increased by 4 is equal		(a) 96		(b) 98	
	to its fourth part diminish	ed by 10, is	26	(c) 102		(d) 106	.,
	(a) 240	(b) 260	26.	Twenty times a pos by 96. What is the		ger is less tha	n its square
	(c) 270	(d) 280		(a) 20	mucger.		
17.	The difference of two num	bers is 20% of the larger		(b) 24			
	number. If the smaller number.	mber is 12, the larger one		(c) 30			
	is	(1) 1((d) Cannot be dete	ermined		
	(a) 15	(b) 16		(e) None of these			
40	(c) 18	(d) 20	27.	Thrice the square	of a nat	ural number	decreased
18.	If one-seventh of a number by 100, then the number is			by 4 times the num number. The num	nber is eq		
	(a) 770	(b) 1100		(a) 4		(b) 5	(5.5.6., 2000)
	(c) 1825	(d) 1925		(c) 6		(d) 10	
19.	If the sum of one-half an	d one-fifth of a number	28.	The sum of a numb		` ′	one-eighth
	exceeds one-third of that nu		of 34. What is the square root?				
	is			(a) 8	((b) 27	
	(a) 15	(b) 18		(c) 32	((d) None of	these
20.	(c) 20 If doubling a number and	(d) 30 Ladding 20 to the result	29.	Two-third of a po	ositive n	umber and	$\frac{25}{216}$ of its
	gives the same answer as n			reciprocal are equa			
	8 and taking away 4 from	the product, the number		5	,	12	
	is			(a) $\frac{5}{12}$	((b) $\frac{12}{5}$	
	(a) 2	(b) 3		(c) $\frac{25}{144}$,	(d) $\frac{144}{25}$	
	(c) 4	(d) 6		(c) $\overline{144}$	((a) $\overline{25}$	
21.	If 50 is subtracted from tw result is equal to sum of 4 number. What is the num	40 and one-fourth of that	30.	Find the whole nu 20 is equal to 69 times		eciprocal of t	
	(a) 174	(b) 216		(a) 2.5	((b) 3	
	(c) 246	(d) 336		(c) 5		(d) 7	
22.	A student was asked to di		31.	A positive number			is equal to
	number by 6 and the other			21 times the recipr		•	_
	the two quantities so obta the student divided the nu			is		(1) =	
	fell short by 4. The given			(a) 3		(b) 5	
	, 0			(c) 7	((d) 9	

(c) 7

(b) 5 (d) 9

PRO	BLEMS ON NUMBERS				245		
32.	The sum and product of 35 respectively. The sum of		40. Two numbers are such that the square of one i 224 less than 8 times the square of the other. If th numbers be in the ratio of 3 : 4, the numbers are				
	(a) $\frac{12}{35}$	(b) $\frac{1}{35}$		(a) 6, 8	(<i>b</i>) 9, 12		
				(c) 12, 16	(d) None of these		
	(c) $\frac{35}{8}$	(d) $\frac{7}{32}$	41.	is 4:7. If each is incre	that the ratio between them eased by 4, the ratio becomes		
33.	The sum of a positive nur			3 : 5. The larger numb			
	thrice the difference of the	number and its reciprocal.		(a) 36	(b) 48		
	The number is	1		(c) 56	(d) 64		
	(a) $\sqrt{2}$	$(b) \ \frac{1}{\sqrt{2}}$	42.	be twice the second an	pers is 264. If the first number and third number be one-third econd number is: (R.R.B., 2004)		
	(c) $\sqrt{3}$	(d) $\frac{1}{\sqrt{3}}$		(a) 48	(b) 54		
		V 3		(c) 72	(d) 84		
34.	The product of two whole		43	` '	nbers is 22. Five times one		
	root of the difference of the		10.		imes the other. The bigger of		
	(a) 4.5	(b) 6		the two numbers is			
25	(c) 7.5	(d) 8		(a) 10	(b) 12		
35.	The product of two natu the sum of the reciprocals			(c) 15	(d) 16		
		-			` ´ _		
	(a) $\frac{1}{289}$	(b) $\frac{289}{290}$	44.		r is equal to $\frac{5}{8}$ of another		
	(c) $\frac{290}{289}$	(d) 289			to the first number, it becomes I number. The second number		
36.	If $2\frac{1}{2}$ is added to a number	er and the sum multiplied		(a) 25	(b) 40		
	2	1		(c) 70	(d) 125		
	by $4\frac{1}{2}$ and 3 is added to	the product and the sum	45.	` '	ers is 25 and their difference		
	is divided by $1\frac{1}{5}$, the quo	tient becomes 25. What is		(a) 104	(b) 114		
	9			(c) 315	(d) 325		
	the number?	4	46.		bers is 33 and their difference		
	(a) $2\frac{1}{2}$	(b) $3\frac{1}{2}$		is 15, the smaller num			
	_	_		(a) 9	(b) 12		
	(c) $4\frac{1}{2}$	(d) $5\frac{1}{2}$		(c) 15	(d) 18		
37.	Three numbers are in the	ratio 4:5:6 and their	47.		ers is 40 and their difference		
	average is 25. The largest			(a) 11:9	(b) 11:18		
	(a) 30	(b) 32		(c) 21 : 19	(d) 22 : 9		
20	(c) 36	(d) 42	48.	, ,	numbers is 192 and the sum		
30.	Three numbers are in the product is 1944. The large				is 28. What is the smaller of		
	(a) 6	(b) 12		(a) 12	(b) 14		
	(c) 18	(d) None of these		(c) 16	(d) 18		
39.	The ratio between a two-d			(e) None of these			
	of the digits of that numb	per is 4:1. If the digit in	49.	There are two numbers	s such that the sum of twice		
	the unit's place is 3 more				rice the second number is 100		
	place, then the number is				he first number and twice the		
	(a) 24	(b) 36		second number is 120.	Which is the larger number?		
	(c) 63	(d) 96			(Bank P.O., 2010)		

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	(a) 12	(b) 14		(a) 12, 5	(b) 13, 4
	(c) 32	(d) 35		(c) 14, 3	(d) 24, 10
	(e) None of these		59.	If the sum and differen	ice of two numbers are 20 and
50.	What is the greater of to product is 1092 and the s	sum of the two numbers		8 respectively, then the	ne difference of their squares
	exceeds their difference by	42? (S.B.I.P.O., 2008)		(a) 12	(b) 28
	(a) 44	(b) 48		(c) 160	(d) 180
F-1	(c) 52 (e) None of these	(d) 54	60.	sum and their product	th that their difference, their t are to one another as 1:7: two numbers is (M.B.A., 2010)
51.	The difference between product is 500. Find the n			(a) 6	(b) 12
	product is ooo. This the h	(Hotel Management, 2003)		(c) 24	(d) 48
	(a) 15, 20	(b) 20, 25	61.	, ,	imbers is 120 and the sum of
	(c) 30, 25	(d) 21, 26			he sum of the numbers is
52.	Two numbers differ by 5	, ,			(R.R.B., 2004)
	then the sum of the two r			(a) 20	(b) 23
	(a) 21	(b) 28		(c) 169	(d) None of these
	(c) 37	(d) 51	62.	-	umbers is 45 and the sum of
53.	Two different natural nur	nbers are such that their		=	he numbers are (R.R.B., 2002)
	product is less than their s	sum. One of the numbers		(a) 3 and 5	(b) 5 and 9
	must be	(1) a		(c) 5 and 19	(d) 45 and 1
	(a) 1	(b) 2	63.	*	s of two numbers is 3341 and
	(c) 3	(d) None of these		are	squares is 891. The numbers (M.B.A., 2006)
54.	The product of two number			(a) 25, 36	(b) 25, 46
	when the larger one is div. The sum of the numbers i	•		(c) 35, 46	(d) None of these
	(a) 380	(b) 395	64.	• •	en two positive integers is 3.
55	(c) 400 The difference between tw	(d) 425	01.		uares is 369, then the sum of (S.S.C., 2003)
33.	the larger number is divide			(a) 25	(b) 27
	quotient is 6 and the rem			(c) 33	(d) 81
	number is		65.	If the sum of two numl	bers is 22 and the sum of their
	(a) 240	(b) 270		squares is 404, then th	ne product of the numbers is
	(c) 295	(d) 360		(a) 40	(b) 44
56.	The difference between tw			(c) 80	(d) 88
	third of the smaller num seventh of the larger num numbers are		66.		n the squares of two numbers of the numbers is 1000. The
	(a) 9 and 25	(b) 12 and 28		(a) 600, 400	(b) 628, 372
	(c) 33 and 49	(d) 56 and 72		(c) 640, 360	(d) None of these
57.	The sum of two numbers 375. What will be the sum		67.	The difference between	n two numbers is 3 and the eir squares is 63. Which is the
	(a) $\frac{1}{40}$	(b) $\frac{8}{75}$		larger number?	(Bank P.O., 2009)
	40			(a) 9	
	(c) $\frac{75}{4}$	(d) $\frac{75}{8}$		(b) 12	
	-	O		(c) 15	
58.	The sum of two positive is bigger number is 204, and t by the smaller number is	heir difference multiplied		(<i>d</i>) Cannot be determine(<i>e</i>) None of these	ned

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68.	A, B, C, D and E are five con			(a) 7	(b) 9	
	sum of A and C is 146. Wh			(c) 11	(d) Data inac	dequate
	() =a	(Bank P.O., 2009)		(e) None of these		
	(a) 71	(b) 75	76.	The product of three conse		
	(c) 79	(d) 81		divided by 8 is 720. Th		
	(e) None of these			roots is		agement, 2006)
69.	Out of six consecutive nati			(a) $12\sqrt{10}$	(b) $24\sqrt{10}$	
	first three is 27, what is the			(c) 120	(d) None of	these
	(a) 24	(S.S.C., 2010) (b) 25	77.	The sum of three consect What is the largest number 1.		s of 3 is 72
	(c) 35	(d) 36		(a) 21	(b) 24	
70.	The sum of seven consecu	tive numbers is 175. What		(c) 27	(d) 36	
	is the difference between and thrice the smallest nu		78.	What is the sum of two of the difference of whose s		
		(Bank Recruitment, 2010)		(a) 34	(b) 38	
	(a) 7	(<i>b</i>) 8		(c) 42	(d) 46	
	(c) 10	(d) 12	79.	The sum of the squares o	f three consecu	tive natural
	(e) None of these			numbers is 2030. What is		
71.	The sum of five consecu	tive odd numbers is 575.		(a) 25	(b) 26	
	What is the sum of the ne			(c) 27	(d) 28	
	odd numbers?	(NABARD, 2009)	80.	If the product of three c	onsecutive inte	gers is 120
	(a) 595			then the sum of the integ	gers is	(M.B.A., 2006)
	(b) 615			(a) 9	(b) 12	
	(c) 635			(c) 14	(d) 15	
	(d) Cannot be determined			(e) 18		
	(e) None of these		81.	There are two numbers s		
72.	The sum of three consec	cutive odd numbers and		the first and thrice the se		
	three consecutive even i			of thrice the first and tw	vice the second	t is 36. The
	Also, the smallest odd			larger of the two is	(1-) 0	
		er. What is the sum of		(a) 6	(b) 8	
	the largest odd numbe	_	0.0	(c) 9	(d) 12	••/ 1
	number?	(Bank P.O., 2010)	82.	In a two-digit number, the		
	(a) 74			is four times the digit in digits is equal to 10. Wh		
	(b) 82			(a) 14	(b) 41	
	(c) 83			(c) 82	(d) Data inac	dequate
	(d) Cannot be determined			(e) None of these	(11) 2 4 4 4 1 1 1 1 1 1	acquare
	(e) None of these	. 11	83.	A number of two digits	has 3 for its	unit's digit
73.	Three times the first of three is 2 more than twice the th			_ ,	1	_
	is 3 more than twice the th			and the sum of digits is	$\frac{1}{7}$ of the number	er itself. The
	(a) 0	(M.B.A., 1998)		number is		(L.I.C., 2003)
	(a) 9	(b) 11		(a) 43	(b) 53	
74	(c) 13	(d) 15		(c) 63	(d) 73	
/4.	The sum of four consecut The greatest of them is	ive even integers is 1284.	84.	If a number of two digit		sum of its
	(a) 320	(b) 322		digits, then the number		
	(c) 324	(d) 326		the digits is the sum of t		
75	The sum of three consec	, ,				(M.B.A., 2005)
, 3.	more than the first of the			(a) $k - 1$	(b) $11 - k$	
	middle number?			(c) 9 + k	(d) 10 - k	

85.	A two-digit number exceed of that number by 18. If the is double the digit in the number?	e digit at the unit's place	92.	number obtair its digits is 36	ned by intero . What is th	two-digit number changing the potential difference bet (Bank P.O., 2003)	sitions of
	(a) 24	(b) 42		(a) 3		(b) 4	
	(c) 48	(d) Data inadequate		(c) 9		(d) Cannot be de	etermined
86.	The sum of the digits of a	-		(e) None of th	ese		
	and the difference between the two-digit number? (a) 69 (b) 78		93.	number obtair	ned by interc	wo-digit number changing the two of the two numb (Bank	o digits is
	• •			(a) 29			
	(c) 96			(b) 70			
	(d) Cannot be determined			(c) 92			
	(e) None of these			(d) Cannot be	determined		
87.	A two-digit number is 7			(e) None of th	ese		
	digits. The number that is digits is 18 less than the o		0.4	The cum of th	o dicite of a	s trus disit num	hor is 1
	the number?	(R.R.B., 2006)	94.	. The sum of th	ie digits of a	a two-digit num	$\frac{1}{5}$
	(a) 42	(b) 52				e number and th	
	(c) 62	(d) 72				the positions of	
88	If the digit in the unit's pla	` '		of that numbe		erence between	tne aigits
00.	is halved and the digit in t			(a) 5	.1:	(b) 7	
	the number thus obtained			(c) 9		(d) Data inade	ruste
	obtained by interchanging	the digits. Which of the		(e) None of th	ese	(ii) Data Hade	quate
	following is definitely true	e? (NMAT, 2005)	95.			terchanging the	two digits
	(a) Sum of the digits is a t(b) Digit in the unit's place ten's place.	_	<i>30.</i>	of a two-digit number by 54	t number is . If the sum	lesser than the n of the two di s the original n	e original git of the
	(c) Digit in the unit's place	e and the ten's place are				(Bank	P.O., 2009)
	equal.			(a) 28			
	(d) Digit in the unit's place	e is twice the digit in the		(b) 39			
00	ten's place.	1		(c) 82			
89.	In a two-digit number, if i			(d) Cannot be			
	digit exceeds its ten's digit of the given number and		0.0	(e) None of th		1	1.1
	equal to 144, then the num		96.			wo-digit numbe	
	(a) 24	(b) 26				changing the di etween the sum	
	(c) 42	(d) 46				the number if	
90.	A number consists of two					number is 1 : 2	
,,,,	change places and the new			(a) 4	· ·	(b) 8	
	original number, then the			(c) 16		(d) None of the	ese
	divisible by	(S.S.C., 2003)	97		nositive num	ber, the digit in	
	(a) 3	(<i>b</i>) 5	57.		•	are of the digi	
	(c) 9	(d) 11				between the nu	
91.	The sum of the digits of a than the number. Which	of the following digits is		the number of	otained by in	nterchanging the iginal number?	
	at unit's place of the num	ber?				(Bank	P.O., 2008)
	(a) 1	(b) 2		(a) 15.6		(b) 24	
	(c) 4	(d) Data inadequate		(c) 37.2		(d) 39	
		-		(e) None of th	ese		

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PRO	BLEMS ON NUMBERS					249
98.	A number consists of 3 di middle digit is equal to and the number will be in are reversed. The number	the sum of the other two acreased by 99 if its digits	plac	42 number of three dig ce and in the hund:	red's place	are equal and
	(a) 145	(b) 253		sum of all the digits obers is	3 18 8. The r	number of such
	(c) 370	(d) 352	(a) 3		(b) 4	
99.	A two-digit number become its digits are reversed. The number is			5 three-digit number, 5% of the digit in the		
	(a) 45	(b) 54		s place is greater than		
	(c) 56	(d) 65		e by 1. If the sum of		
100.	If the square of a two-dig the square of the number digits of the number, the	formed by reversing the	(a) 6 (b) 7		15 15, What 1	s the number? (Bank P.O., 2006)
	(a) divisible by 11	(b) divisible by 9	(c) 7			
	(c) necessarily irrational	(<i>d</i>) Both (<i>a</i>) and (<i>b</i>)		Cannot be determine	ed	
101.	A number consists of two			None of these	14	
	in the ten's place is less l		108. The	product of two fraction	ons is $\frac{14}{15}$ an	d their quotient
	unit's place. Three times times the number obtained		is $\frac{3}{2}$	$\frac{35}{24}$. The greater fract	ion is	(S.S.C., 2005)
	equals 108. The sum of the		(a)	<u>4</u> 5	(b) $\frac{7}{6}$	
	(a) 6	(b) 7	(c) -	7	(d) $\frac{7}{3}$	
	(c) 8	(d) 9	(1)	$\overline{4}$	$(u) \overline{3}$	
102.	The digit in the unit's pl to the digit in the ten's pl and the digit in the ten's p than the digit in unit's pl by 1. If the sum of the c then what is the number?	ace of half of that number is less ace of half of the number ligits of the number is 7, (S.B.I.P.O., 2001)	Ва	pair of fractions, fraction of the product of two value of fraction A? $\frac{1}{5}$	vo fractions	2
	(a) 34	(b) 52		2	(1) D (. 1 .
	(c) 162	(d) Data inadequate	(c) -	5	(a) Data	inadequate
102	(e) None of these	a digit in the unit's place		ne difference between		
103.	In a two-digit number, the is more than twice the digits in the unit's pla	git in ten's place by 1. If	proj	per fraction and the	fraction itse	elf be $\frac{9}{20}$, then
	interchanged, difference b	etween the newly formed		fraction is	4	(C.P.O., 2006)
	number and the original		(a)	<u>3</u> 5	(b) $\frac{4}{5}$	
	original number by 1. What (a) 25	(b) 37				
	(c) 49	(d) 52	(c) ·	$\frac{3}{4}$	(d) $\frac{3}{10}$	
104.	(e) 73 A certain number of two sum of its digits and if 45		111. The	sum of the numeration is 11. If 1 is add	ator and de	
	are reversed. The number			ubtracted from the de	enominator,	it becomes $\frac{2}{3}$.
	(a) 23	(b) 27		fraction is 5	6	
105.	(c) 32 A two-digit number is su	(d) 72 ch that the product of the	(a)	6	(b) $\frac{6}{5}$	
	digits is 8. When 18 is ac					
	the digits are reversed. The		(c)	8	(d) $\frac{8}{3}$	
					•	

(Bank P.O., 2008)

112. The denominator of a fraction is 3 more than the numerator. If the numerator as well as the denominator is increased by 4, the fraction becomes What was the original fraction?

113. The difference between the numerator and the denominator of a fraction is 5. If 5 is added to its denominator, the fraction is decreased by $1\frac{1}{4}$. Find the value of the fraction.

(a) $\frac{1}{6}$

(c) $3\frac{1}{4}$

114. The numerator and denominator of a fraction are in the ratio of 2:3. If 6 is subtracted from the numerator, the result is a fraction that has a value $\frac{2}{3}$ of the original fraction. The numerator of the original fraction is

(a) 6

(b) 18

(c) 27

(d) 36

115. If 1 is added to the denominator of a fraction, the fraction becomes $\frac{1}{2}$. If 1 is added to the numerator of the fraction, the fraction becomes 1. The fraction

(a) $\frac{1}{3}$

116. If the numerator of a fraction is increased by 2 and the denominator is increased by 3, the fraction becomes $\frac{7}{9}$ and if both the numerator as well as the denominator are decreased by 1, the fraction becomes $\frac{4}{5}$. What is the original fraction?

(a) $\frac{5}{6}$

117. If the numerator of a fraction is increased by $\frac{1}{4}$ and the denominator is decreased by $\frac{1}{3}$, the new fraction obtained is $\frac{33}{64}$. What was the original fraction?

(d) Cannot be determined

(e) None of these

118. If the numerator of a fraction is increased by 200% and the denominator is increased by 300%, the resultant fraction is $\frac{15}{26}$. What was the original

fraction? (S.B.I.P.O., 2008)

(a) $\frac{8}{11}$

(e) None of these

When the numerator of a fraction increases by 4, the fraction increases by $\frac{2}{3}$. The denominator of the fraction is

(a) 2

(b) 3

(c) 4

(d) 6

120. A fraction is such that if the double of the numerator and the triple of the denominator is changed by + 10 percent and -30 percent respectively, then we get 11 percent of $\frac{16}{21}$. Find the fraction.

(A.T.M.A., 2004)

(d) None of these

121. 54 is to be divided into two parts such that the sum of 10 times the first and 22 times the second is 780. The bigger part is

(a) 24

(b) 34

(c) 30

(d) 32

122. 243 has been divided into three parts such that half of the first part, one-third of the second part and one-fourth of the third part are equal. The largest part is

(a) 74

(b) 86

(c) 92

(d) 108

123. The sum of four numbers is 64. If you add 3 to the first number, 3 is subtracted from the second number, the third is multiplied by 3 and the fourth is divided by 3, then all the results are equal. What PROBLEMS ON NUMBERS 251

is the difference between the largest and the smallest of the original numbers?

(a) 21

(b) 27

(c) 32

(d) Cannot be determined

(e) None of these

124. The sum of the squares of three numbers is 138, while the sum of their products taken two at a time is 131. Their sum is (Hotel Management, 1999)

(a) 20

(b) 30

(c) 40

(d) None of these

125. The sum of three numbers is 136. If the ratio between first and second be 2:3 and that between second and third is 5:3, then the second number is

(a) 40

(b) 48

(c) 60

(d) 72

126. Of the three numbers, the sum of the first two is 73; the sum of the second and the third is 77 and the sum of the third and thrice the first is 104. The third number is (NABARD, 2008)

(a) 25

(b) 39

(c) 48

(d) Cannot be determined

(e) None of these

127. If the product of two numbers is 5 and one of the number is $\frac{3}{2}$, then the sum of two numbers is

[Indian Railways—Gr. 'D' Exam, 2014] (b) $4\frac{2}{3}$

(a) $4\frac{1}{3}$

(c) $4\frac{5}{6}$

(d) $5\frac{1}{6}$

128. The sum of the squares of two positive integers is 100 and the difference of their squares is 28. The sum of the numbers is

[Indian Railways-Gr. 'D' Exam, 2014]

(a) 12

(b) 13

(c) 14

(d) 15

129. The sum of two number is 37 and the difference of their squares is 185, then the difference between the two numbers is: [SSC-CHSL (10 +2) Exam, 2015]

(a) 10

(b) 4

(c) 5

(d) 3

130. A man bought some eggs of which 10% are rotten. He gives 80% of the remainder to his neighbors. Now he is left out with 36 eggs. How many eggs he bought? [SSC—CHSL (10 +2) Exam, 2015]

(a) 40

(b) 100

(c) 200

(d) 72

131. The sum of two numbers is 75 and their difference is 25. The product of the two numbers is:

[SSC—CHSL (10 +2) Exam, 2015]

(a) 1350

(b) 1250

(c) 125

(d) 1000

132. In a Mathematics examination the number scored by 5 candidates are 5 successive odd integers. If their total marks are 185, the highest score is

[NICL—AAO Exam, 2015]

(a) 39

(b) 43

(c) 41

(d) 47

133. The difference between two numbers is 10 and one-fifth of their sum is equal to 8. Find the smaller [ESIC—UDC Exam, 2016] number

(a) 28

(b) 45

(c) 35

(d) 15

ANSWERS

1. (d)	2. (c)	3. (a)	4. (b)	5. (<i>b</i>)	6. (c)	7. (c)	8. (<i>d</i>)	9. (<i>d</i>)	10. (c)
11. (c)	12. (<i>d</i>)	13. (<i>c</i>)	14. (a)	15. (<i>c</i>)	16. (<i>d</i>)	17. (<i>a</i>)	18. (<i>d</i>)	19. (c)	20. (<i>c</i>)
21. (<i>b</i>)	22. (<i>d</i>)	23. (<i>b</i>)	24. (<i>e</i>)	25. (<i>c</i>)	26. (<i>b</i>)	27. (<i>b</i>)	28. (<i>a</i>)	29. (<i>a</i>)	30. (<i>b</i>)
31. (c)	32. (<i>a</i>)	33. (<i>a</i>)	34. (<i>b</i>)	35. (<i>c</i>)	36. (<i>b</i>)	37. (<i>a</i>)	38. (<i>c</i>)	39. (<i>b</i>)	40. (<i>a</i>)
41. (c)	42. (c)	43. (<i>b</i>)	44. (<i>b</i>)	45. (<i>b</i>)	46. (a)	47. (a)	48. (a)	49. (c)	50. (<i>c</i>)
51. (<i>b</i>)	52. (<i>c</i>)	53. (<i>a</i>)	54. (<i>c</i>)	55. (<i>b</i>)	56. (<i>c</i>)	57. (<i>b</i>)	58. (<i>a</i>)	59. (<i>c</i>)	60. (<i>d</i>)
61. (<i>b</i>)	62. (<i>b</i>)	63. (<i>c</i>)	64. (<i>b</i>)	65. (<i>a</i>)	66. (<i>b</i>)	67. (<i>b</i>)	68. (<i>c</i>)	69. (<i>d</i>)	70. (<i>e</i>)
71. (<i>e</i>)	72. (<i>e</i>)	73. (<i>d</i>)	74. (c)	75. (<i>b</i>)	76. (<i>b</i>)	77. (c)	78. (<i>c</i>)	79. (<i>b</i>)	80. (<i>d</i>)
81. (c)	82. (<i>e</i>)	83. (<i>c</i>)	84. (<i>b</i>)	85. (<i>a</i>)	86. (<i>d</i>)	87. (<i>a</i>)	88. (<i>d</i>)	89. (<i>a</i>)	90. (<i>d</i>)
91. (<i>d</i>)	92. (<i>b</i>)	93. (<i>d</i>)	94. (<i>d</i>)	95. (<i>e</i>)	96. (<i>b</i>)	97. (<i>a</i>)	98. (<i>b</i>)	99. (<i>b</i>)	100. (<i>d</i>)
101. (a)	102. (<i>b</i>)	103. (<i>b</i>)	104. (<i>b</i>)	105. (<i>b</i>)	106. (<i>b</i>)	107. (<i>b</i>)	108. (<i>b</i>)	109. (<i>c</i>)	110. (<i>b</i>)
111. (c)	112. (a)	113. (<i>b</i>)	114. (<i>b</i>)	115. (<i>b</i>)	116. (a)	117. (<i>d</i>)	118. (<i>d</i>)	119. (<i>d</i>)	120. (<i>a</i>)
121. (<i>b</i>)	122. (<i>d</i>)	123. (<i>c</i>)	124. (a)	125. (<i>c</i>)	126. (<i>e</i>)	127. (c)	128. (c)	129. (<i>c</i>)	130. (<i>c</i>)
131. (<i>b</i>)	132. (<i>c</i>)	133. (<i>d</i>)							

SOLUTIONS

1.
$$\frac{7}{8}$$
 of $1008 - \frac{3}{4}$ of $568 = \left(1008 \times \frac{7}{8}\right) - \left(568 \times \frac{3}{4}\right)$
= $882 - 426 = 456$.

2. Let the number be x.

Then,
$$x - \frac{3}{5} x = 50 \Leftrightarrow \frac{2}{5} x = 50$$

$$\Leftrightarrow x = \left(\frac{50 \times 5}{2}\right) = 125.$$

3. Let the number be x

Then,
$$x + \frac{2}{5}$$
 $x = 455 \Leftrightarrow \frac{7}{5}$ $x = 455 \Leftrightarrow x = \left(\frac{455 \times 5}{7}\right) = 325$.

4. Let the number be x. Then, $x \times \frac{2}{3}$ x = 864

$$\Leftrightarrow \frac{2}{3} x^2 = 864$$

$$\Leftrightarrow x^2 = \left(\frac{864 \times 3}{2}\right) = 1296 \Leftrightarrow x = \sqrt{1296} = 36.$$

5. Let the number be x. Then, $\frac{x-4}{6} = 8$

$$\Leftrightarrow x - 4 = 48$$

$$\Leftrightarrow x = 52$$

$$\Leftrightarrow x - 4 = 48$$

$$\Leftrightarrow x = 52.$$

$$\therefore \frac{x-2}{5} = \frac{52-2}{5} = \frac{50}{5} = 10.$$

6. Let the number be x.

Then, $13x = x + 180 \Leftrightarrow 12x = 180$

$$\Leftrightarrow x = \frac{180}{12} = 15.$$

7. Let the number be x.

Then,
$$2x + 3 \times 42 = 238 \Leftrightarrow 2x + 126 = 238$$

$$\Leftrightarrow 2x = 112 \Leftrightarrow x = 56.$$

$$\therefore$$
 Required sum = $3x + 2 \times 42 = 3 \times 56 + 2 \times 42$
= $168 + 84 = 252$.

8. Let the number be x. Then, $\frac{1}{3}$ of $\frac{1}{4}$ of x = 15

$$\Leftrightarrow x = 15 \times 12 = 180.$$

So, required number =
$$\left(\frac{3}{10} \times 180\right) = 54$$
.

9. Let the number be *x*

Then,
$$\frac{3}{5}$$
 of $\frac{2}{3}$ of $x - \frac{2}{5}$ of $\frac{1}{4}$ of $x = 288$

$$\Leftrightarrow$$
 $\left(x \times \frac{3}{5} \times \frac{2}{3}\right) - \left(x \times \frac{2}{5} \times \frac{1}{4}\right) = 288$

$$\Leftrightarrow \quad \frac{2}{5} x - \frac{1}{10} x = 288$$

$$\Leftrightarrow \frac{3x}{10} = 288 \Leftrightarrow x = \left(\frac{288 \times 10}{3}\right) = 960.$$

10. Let the number be x.

Then,
$$3(2x + 9) = 75 \Leftrightarrow 2x + 9 = 25$$

 $\Leftrightarrow 2x = 16 \Leftrightarrow x = 8$.

11. Let the number be
$$x$$
.

Then,
$$\frac{3}{4}x - \frac{1}{3}x = 60$$

$$\Leftrightarrow \frac{5x}{12} = 60$$

$$\Leftrightarrow x = \left(\frac{60 \times 12}{5}\right) = 144.$$

12. Let the number be

Then,
$$\frac{x}{5} + 4 = \frac{x}{4} - 10 \iff \frac{x}{4} - \frac{x}{5} = 14$$

$$\Leftrightarrow \frac{x}{20} = 14 \Leftrightarrow x = 14 \times 20 = 280.$$

13. Let the number be x

Then,
$$x - 24 = \frac{4}{7}x \iff x - \frac{4}{7}x = 24$$

$$\Leftrightarrow \frac{3}{7}x = 24 \Leftrightarrow x = \left(\frac{24 \times 7}{3}\right) = 56.$$

Sum of the digits = (5 + 6) = 11.

14. Let the number be x.

Then,
$$15x - x = 196$$

$$\Leftrightarrow 14x = 196$$

15. Let the number be x.

Then,
$$\frac{x}{4} = x - 21 \iff x = 4x - 84$$

$$\Leftrightarrow$$
 $3x = 84 \Leftrightarrow x = 28.$

16. Let the number be x.

Then,
$$\left(\frac{1}{5}x + 4\right) = \left(\frac{1}{4}x - 10\right)$$

$$\Leftrightarrow \frac{x}{20} = 14 \Leftrightarrow x = 14 \times 20 = 280.$$

17. Let the number be x.

Then,
$$x - 12 = 20\%$$
 of $x \iff x - \frac{x}{5} = 12$

$$\Leftrightarrow \frac{4x}{5} = 12 \Leftrightarrow x = \left(\frac{12 \times 5}{4}\right) = 15.$$

18. Let the number be x.

Then,
$$\frac{1}{7}x - \frac{1}{11}x = 100 \iff \frac{4x}{77}$$

= 100 $\iff x = \frac{7700}{4} = 1925.$

19. Let the number be x.

Then,
$$\left(\frac{1}{2}x + \frac{1}{5}x\right) - \frac{1}{3}x = \frac{22}{3} \iff \frac{11x}{30}$$

= $\frac{22}{3} \iff x = \left(\frac{22 \times 30}{3 \times 11}\right) = 20.$

20. Let the number be x.

Then,
$$2x + 20 = 8x - 4 \Leftrightarrow 6x = 24$$

$$\Leftrightarrow x = 4.$$

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21. Let the number be x.

Then,
$$\frac{2}{3}x - 50 = \frac{1}{4}x + 40 \iff \frac{2}{3}x - \frac{1}{4}x = 90$$

$$\iff \frac{5x}{12} = 90 \iff x = \left(\frac{90 \times 12}{5}\right) = 216.$$

22. Let the number be x.

Then,
$$\left[\frac{(x/2)}{6} + \frac{(x/2)}{4}\right] - \frac{x}{5} = 4 \Leftrightarrow \frac{x}{12} + \frac{x}{8} - \frac{x}{5} = 4$$
$$\Leftrightarrow \frac{10x + 15x - 24x}{120} = 4$$
$$\Leftrightarrow x = 4 \times 120 = 480.$$

23. Let the number be x.

Then,
$$\frac{x}{3} - \frac{(x+1)}{4} = 1 \iff 4x - 3(x+1) = 12 \iff x = 15.$$

24. Let the number be x.

Then,
$$x + x^2 = 182 \Leftrightarrow x^2 + x - 182 = 0$$

 $\Leftrightarrow (x + 14) (x - 13) = 0 \Leftrightarrow x = 13.$

25. Let the number be x.

Then,
$$x^2 - (73)^2 = 5075 \Leftrightarrow x^2 - 5329 = 5075$$

 $\Leftrightarrow x^2 = 5075 + 5329 = 10404$
 $\Leftrightarrow x = \sqrt{10404} = 102.$

26. Let the integer be x.

Then,
$$x^2 - 20x = 96$$

 $\Leftrightarrow x^2 - 20x - 96 = 0$
 $\Leftrightarrow (x + 4)(x - 24) = 0$
 $\Leftrightarrow x = 24$.

27. Let the number be x.

Then,
$$3x^2 - 4x = x + 50$$

 $\Leftrightarrow 3x^2 - 5x - 50 = 0$
 $\Leftrightarrow (3x + 10)(x - 5) = 0$
 $\Leftrightarrow x = 5$.

28. Let the number be x.

Then,
$$x + \frac{1}{x} = \frac{34}{8} \Leftrightarrow \frac{x^2 + 1}{x} = \frac{34}{8}$$

 $\Leftrightarrow 8x^2 - 34x + 8 = 0$
 $\Leftrightarrow 4x^2 - 17x + 4 = 0$
 $\Leftrightarrow (4x - 1)(x - 4) = 0$
 $\Leftrightarrow x = 4$.

$$\left[\text{neglecting } x = \frac{1}{4}, \text{ as } x \text{ is a natural no.} \right]$$

 \therefore Required number = $4 \times \sqrt{4} = 4 \times 2 = 8$.

29. Let the number be x.

Then,
$$\frac{2}{3}x = \frac{25}{216} \times \frac{1}{x} \iff x^2 = \frac{25}{216} \times \frac{3}{2}$$
$$= \frac{25}{144} \iff x = \sqrt{\frac{25}{144}} = \frac{5}{12}.$$

30. Let the required number be x.

Then,
$$x + 20 = \frac{69}{x} \Leftrightarrow x^2 + 20x - 69 = 0$$

$$\Leftrightarrow x^2 + 23x - 3x - 69 = 0$$

$$\Leftrightarrow x(x + 23) - 3(x + 23) = 0$$

$$\Leftrightarrow (x + 23) (x - 3) = 0$$

$$\Leftrightarrow x = 3 \qquad [\because x \neq -23]$$

31. Let the number be x.

Then,
$$x - 4 = \frac{21}{x} \iff x^2 - 4x - 21 = 0$$

$$\iff (x - 7)(x + 3) = 0 \iff x = 7.$$

32. Let the numbers be x and y.

Then, x + y = 12 and xy = 35.

$$\therefore \frac{1}{x} + \frac{1}{y} = \frac{x+y}{xy} = \frac{12}{35}$$

33. Let the number be x.

Then,
$$x + \frac{1}{x} = 3\left(x - \frac{1}{x}\right)$$

 $\Leftrightarrow \frac{x^2 + 1}{x} = 3\left(\frac{x^2 - 1}{x}\right)$
 $\Leftrightarrow x^2 + 1 = 3x^2 - 3$
 $\Leftrightarrow 2x^2 = 4$
 $\Leftrightarrow x^2 = 2$

34. Let the numbers be a and b.

Then,
$$ab = 37 \implies a = 1$$
 and $b = 37$.

So,
$$\sqrt{b-a} = \sqrt{37-1} = \sqrt{36} = 6$$
.

35. Let the numbers be a and b.

Then, $ab = 17 \implies a = 1$ and b = 17.

So,
$$\frac{1}{a^2} + \frac{1}{b^2} = \frac{a^2 + b^2}{a^2 b^2} = \frac{1^2 + (17)^2}{(1 \times 17)^2} = \frac{290}{289}$$
.

36. Let the number be x. Then

$$\frac{4\frac{1}{2}\left(x+2\frac{1}{2}\right)+3}{1\frac{1}{5}} = 25 \iff \frac{\frac{9}{2}\left(x+\frac{5}{2}\right)+3}{\frac{6}{5}} = 25$$
$$\Leftrightarrow \frac{9x}{2} + \frac{45}{4} + 3 = 25 \times \frac{6}{5} = 30$$
$$\Leftrightarrow \frac{9x}{2} = 30 - \frac{57}{4} \Leftrightarrow \frac{9x}{2} = \frac{63}{4}$$
$$\Leftrightarrow x = \left(\frac{63}{4} \times \frac{2}{9}\right) = \frac{7}{2} = 3\frac{1}{2}.$$

37. Let the numbers be 4x, 5x and 6x.

Then,
$$\frac{4x+5x+6x}{3} = 25 \iff 5x = 25 \iff x = 5.$$

 \therefore Largest number = 6x = 30.

38. Let the numbers be 3x, 4x and 6x.

Then, $3x \times 4x \times 6x = 1944$

$$\Leftrightarrow 72x^3 = 1944 \Leftrightarrow x^3 = 27$$

 $\Leftrightarrow x = 3.$

 \therefore Largest number = 6x = 18.

39. Let the ten's digit be x. Then, unit's digit = x + 3. Number = 10x + (x + 3) = 11x + 3.

Sum of digits = x + (x + 3) = 2x + 3.

$$\therefore \frac{11x+3}{2x+3} = \frac{4}{1} \Leftrightarrow 11x+3 = 8x+12$$

Hence, required number = $11x + 3 = 11 \times 3 + 3 = 36$.

40. Let the numbers be 3x and 4x.

Then,
$$(4x)^2 = 8 \times (3x)^2 - 224$$

 $\Leftrightarrow 16x^2 = 72x^2 - 224$
 $\Leftrightarrow 56x^2 = 224 \Leftrightarrow x^2 = 4$
 $\Leftrightarrow x = 2$.

So, the numbers are 6 and 8.

41. Let the numbers be 4x and 7x.

Then,
$$\frac{4x+4}{7x+4} = \frac{3}{5} \iff 5(4x+4) = 3(7x+4) \iff x = 8.$$

 \therefore Larger number = 7x = 56.

42. Let the second number be x. Then, first number = 2x and third number = $\frac{2x}{3}$.

$$\therefore 2x + x + \frac{2x}{3} = 264 \iff \frac{11x}{3} = 264$$
$$\Leftrightarrow x = \left(\frac{264 \times 3}{11}\right) = 72.$$

43. Let the numbers be x and (22 - x). Then, 5x = 6(22 - x) $\Leftrightarrow 11x = 132 \Leftrightarrow x = 12$.

So, the numbers are 12 and 10.

44. Let the numbers be x and y. Then, $\frac{1}{5}x = \frac{5}{8}y \iff y = \frac{8}{25}x$.

Now,
$$x + 35 = 4y \iff x + 35 = \frac{32}{25}x$$

$$\Leftrightarrow \frac{7}{25} x = 35 \Leftrightarrow x = \left(\frac{35 \times 25}{7}\right) = 125.$$

$$\therefore \quad \text{Second number} = y = \frac{8}{25} x = \left(\frac{8}{25} \times 125\right) = 40.$$

45. Let the numbers be x and y.

Then,
$$x + y = 25$$
 and $x - y = 13$.
 $4xy = (x + y)^2 - (x - y)^2 = (25)^2 - (13)^2$
 $= 625 - 169 = 456 \implies xy = 114$.

46. Let the numbers be x and y. Then,

$$x + y = 33$$
 ...(*i*)
and $x - y = 15$...(*ii*)

Solving (i) and (ii), we get : x = 24, y = 9.

∴ Smaller number = 9.

47. Let the numbers be x and y.

Then,
$$\frac{x+y}{x-y} = \frac{40}{4} = 10 \iff (x+y) = 10(x-y)$$

$$\Leftrightarrow$$
 $9x = 11y \Leftrightarrow \frac{x}{y} = \frac{11}{9}.$

48. Let the numbers be x and (28 - x). Then, $x (28 - x) = 192 \Leftrightarrow x^2 - 28x + 192 = 0$

$$\Leftrightarrow$$
 $(x - 16) (x - 12) = 0$
 \Leftrightarrow $x = 16$ or $x = 12$.

So, the numbers are 16 and 12.

49. Let the numbers be x and y. Then,

$$2x + 3y = 100$$
 ...(i)

and
$$3x + 2y = 120$$
 ...(*ii*)

Adding (i) and (ii), we get: 5x + 5y = 220

or
$$x + y = 44$$
 ...(iii)

Subtracting (i) from (ii); we get : x - y = 20 ...(iv)

Adding (iii) and (iv), we get: 2x = 64 or x = 32.

Putting x = 32 in (iii), we get : y = 12.

Hence, larger number = 32.

50. Let the numbers be x and y. Then,

$$xy = 1092$$
And, $(x + y) - (x - y) = 42$

$$\Leftrightarrow 2y = 42$$

$$\Leftrightarrow y = 21.$$

Putting y = 21 in (i), we get : $x = \frac{1092}{21} = 52$.

Hence, greater number = 52.

51. Let the integers be x and (x + 5). Then,

$$x (x + 5) = 500 \Leftrightarrow x^2 + 5x - 500 = 0$$
$$\Leftrightarrow (x + 25) (x - 20) = 0$$
$$\Leftrightarrow x = 20.$$

So, the numbers are 20 and 25.

52. Let the numbers be x and y.

Then,
$$x - y = 5$$
 and $xy = 336$.

$$(x + y)^2 = (x - y)^2 + 4xy = 25 + 4 \times 336 = 1369$$

 $\Rightarrow x + y = \sqrt{1369} = 37.$

- **53.** Since 1. x < 1 + x, so one of the numbers is 1.
- **54.** Let the numbers be x and y.

Then,
$$xy = 9375$$
 and $\frac{x}{y} = 15$.

$$\frac{xy}{(x/y)} = \frac{9375}{15} \iff y^2 = 625 \iff y = 25$$

$$\Rightarrow x = 15y = (15 \times 25) = 375.$$

 \therefore Sum of the numbers = 375 + 25 = 400.

55. Let the numbers be x and (x + 1365).

Then,
$$x + 1365 = 6x + 15 \Leftrightarrow 5x = 1350 \Leftrightarrow x = 270$$
.

56. Let the numbers be x and (x + 16).

Then,
$$\frac{x}{3} - \frac{(x+16)}{7} = 4 \Leftrightarrow 7x - 3(x+16)$$

= 84 $\Leftrightarrow 4x = 84 + 48$
= 132 $\Leftrightarrow x = 33$.

Hence, the numbers are 33 and 49.

57. Let the numbers be x and y.

Then, x + y = 40 and xy = 375.

$$\therefore \frac{1}{x} + \frac{1}{y} = \frac{x+y}{xy} = \frac{40}{375} = \frac{8}{75}.$$

58. Let the numbers be x and y such that x > y.

Then,
$$x(x + y) = 204 \Rightarrow x^2 + xy = 204$$
 ...(i)

and
$$y(x - y) = 35 \Rightarrow xy - y^2 = 35$$
 ...(ii)

Subtracting (ii) from (i), we get: $x^2 + y^2 = 169$.

The only triplet satisfying this condition is (12, 5, 13). Thus, x = 12, y = 5.

59. Let the numbers be x and y.

Then,
$$x + y = 20$$
 and $x - y = 8$.

$$\therefore x^2 - y^2 = (x + y) (x - y) = 20 \times 8 = 160.$$

60. Let the numbers be x and y.

Let
$$a - b = k$$
 ...(i)

$$ab = 24k$$
 ...(iii)

Adding (i) and (ii), we get : 2a = 8k or a = 4k.

Putting a = 4k in (i), we get : b = 3k.

Putting a = 4k and b = 3k in (iii), we get : $4k \times 3k$ = $24k \Leftrightarrow 12k^2 = 24k \Leftrightarrow k = 2$.

Hence, product of numbers = $24k = 24 \times 2 = 48$.

61. Let the numbers be x and y.

Then,
$$xy = 120$$
 and $x^2 + y^2 = 289$.

$$\therefore (x + y)^2 = x^2 + y^2 + 2xy = 289 + 240 = 529.$$

$$x + y = \sqrt{529} = 23.$$

62. Let the numbers be x and y.

Then, xy = 45 and $x^2 + y^2 = 106$.

$$(x+y) = \sqrt{(x^2+y^2) + 2xy}$$

= $\sqrt{106+90} = \sqrt{196} \implies x+y = 14$...(i

$$(x - y) = \sqrt{(x^2 + y^2) - 2xy}$$
$$= \sqrt{106 - 90} = \sqrt{16} \implies x - y = 4 \qquad ...(ii)$$

Solving (i) and (ii), we get : x = 9 and y = 5.

63. Let the numbers be x and y. Then,

$$x^2 + y^2 = 3341 \qquad ...(i)$$

and
$$x^2 - y^2 = 891$$
 ...(ii)

Adding (i) and (ii), we get:

$$2x^2 = 4232$$
 or $x^2 = 2116$ or $x = 46$.

Subtracting (ii) from (i), we get:

$$2y^2 = 2450$$
 or $y^2 = 1225$ or $y = 35$.

So, the numbers are 35 and 46.

64. Let the numbers be x and (x + 3). Then,

$$x^2 + (x+3)^2 = 369$$

$$\Leftrightarrow$$
 $x^2 + x^2 + 9 + 6x = 369$

$$\Leftrightarrow 2x^2 + 6x - 360 = 0$$

$$\Leftrightarrow \quad x^2 + 3x - 180 = 0$$

$$\Leftrightarrow$$
 $(x + 15)(x - 12) = 0$

 $\Leftrightarrow x = 12.$

So, the numbers are 12 and 15.

:. Required sum = (12 + 15) = 27.

65. Let the numbers be x and y.

Then,
$$(x + y) = 22$$
 and $x^2 + y^2 = 404$.

Now,
$$2xy = (x + y)^2 - (x^2 + y^2) = (22)^2 - 404$$

= $484 - 404 = 80 \implies xy = 40$.

66. Let the numbers be x and y.

Then,
$$x^2 - y^2 = 256000$$
 and $x + y = 1000$.

On dividing, we get : x - y = 256.

Solving x + y = 1000 and x - y = 256,

we get : x = 628 and y = 372.

67. Let the numbers be x and y.

Then,
$$x^2 - y^2 = 63$$
 and $x - y = 3$.

On dividing, we get : x + y = 21.

Solving x + y = 21 and x - y = 3,

we get : x = 12 and y = 9.

- ∴ Larger number = 12.
- **68.** Let A = x, B = x + 2, C = x + 4,

$$D = x + 6$$
 and $E = x + 8$.

Then, $A + C = 146 \Rightarrow x + (x + 4) = 146$

- \Rightarrow $2x = 142 \Rightarrow x = 71.$
- E = x + 8 = 71 + 8 = 79.
- **69.** Let the six numbers be x, x + 1, x + 2, x + 3, x + 4 and x + 5.

Then,
$$x + (x + 1) + (x + 2) = 27 \implies 3x + 3 = 27$$
.

Required sum =
$$(x + 3) + (x + 4) + (x + 5)$$

$$= 3x + 12 = (3x + 3) + 9 = 27 + 9 = 36.$$

70. Let the seven numbers be x, x + 1, x + 2, x + 3, x + 4, x + 5 and x + 6.

Then,
$$x + (x + 1) + (x + 2) + (x + 3) + (x + 4) + (x + 5) + (x + 6) = 175$$

$$\Leftrightarrow$$
 $7x + 21 = 175 \Leftrightarrow 7x = 154$

$$\Leftrightarrow$$
 $x = 22.$

Required difference = 2(x + 6) - 3x = 12 - x

$$= 12 - 22 = -10.$$

71. Let the five numbers be x, x + 2, x + 4, x + 6 and x + 8.

Then,
$$x + (x + 2) + (x + 4) + (x + 6) + (x + 8) = 575$$

$$\Leftrightarrow \quad 5x + 20 = 575 \quad \Leftrightarrow \quad 5x = 555 \quad \Leftrightarrow \quad x = 111.$$

Required sum =
$$(x + 10) + (x + 12) + (x + 14) + (x + 16) + (x + 18)$$

$$= 5x + 70 = 5 \times 111 + 70 = 555 + 70 = 625.$$

- **72.** Let the three odd numbers be x, x + 2,
 - x + 4 and the three even numbers be x + 11, x + 13 and x + 15.

Then,
$$x + (x + 2) + (x + 4) + (x + 11) + (x + 13)$$

$$+(x + 15) = 231$$

$$\Leftrightarrow$$
 6x + 45 = 231 \Leftrightarrow 6x = 186 \Leftrightarrow x = 31.

- \therefore Required sum = $(x + 4) + (x + 15) = 2x + 19 = 2 \times 31 + 19 = 62 + 19 = 81.$
- 73. Let the three integers be x, x + 2 and x + 4.

Then,
$$3x = 2(x + 4) + 3 \iff x = 11$$
.

- \therefore Third integer = x + 4 = 15.
- **74.** Let the four integers be x, x + 2, x + 4 and x + 6. Then, x + (x + 2) + (x + 4) + (x + 6) = 1284

$$\Leftrightarrow$$
 $4x = 1272 \Leftrightarrow x = 318.$

 \therefore Greatest integer = x + 6 = 324.

- **75.** Let the numbers be x, x + 2 and x + 4. Then, x + (x + 2) + (x + 4) = x + 20 $\Leftrightarrow 2x = 14 \Leftrightarrow x = 7$. \therefore Middle number = x + 2 = 9.
- **76.** Let the numbers be x, x + 2 and x + 4.

Then,
$$\frac{x(x+2)(x+4)}{8} = 720$$

 $\Rightarrow x(x+2)(x+4) = 5760.$
 $\therefore \sqrt{x} \times \sqrt{(x+2)} \times \sqrt{(x+4)}$
 $= \sqrt{x(x+2)(x+4)} = \sqrt{5760} = 24\sqrt{10}.$

- 77. Let the numbers be 3x, 3x + 3 and 3x + 6. Then, 3x + (3x + 3) + (3x + 6) = 72 $\Leftrightarrow 9x = 63$ $\Leftrightarrow x = 7$.
 - \therefore Largest number = 3x + 6 = 27.
- **78.** Let the numbers be x and x + 2.

Then,
$$(x + 2)^2 - x^2 = 84$$

$$\Leftrightarrow$$
 $4x + 4 = 84$

$$\Leftrightarrow$$
 $4x = 80$

$$\Leftrightarrow$$
 $x = 20.$

$$\therefore$$
 Required sum = $x + (x + 2) = 2x + 2 = 42$.

79. Let the numbers be x, x + 1 and x + 2.

Then,
$$x^2 + (x + 1)^2 + (x + 2)^2 = 2030$$

 $\Leftrightarrow 3x^2 + 6x - 2025 = 0$
 $\Leftrightarrow x^2 + 2x - 675 = 0$
 $\Leftrightarrow (x + 27) (x - 25) = 0$
 $\Leftrightarrow x = 25$.

- \therefore Middle number = (x + 1) = 26.
- **80.** $120 = 2 \times 2 \times 2 \times 3 \times 5 = (2 \times 2) \times 5 \times (2 \times 3) = 4 \times 5 \times 6$. Clearly, the three consecutive integers whose product is 120 are 4, 5 and 6.

Required sum = 4 + 5 + 6 = 15.

81. Let the numbers be x and y.

Then,
$$2x + 3y = 39$$
 ...(*i*) and $3x + 2y = 36$...(*ii*) On solving (*i*) and (*ii*), we get : $x = 6$ and $y = 9$.

∴ Larger number = 9.

82. Let the ten's digit be x. Then, unit's digit = 4x. $\therefore x + 4x = 10 \Leftrightarrow 5x = 10 \Leftrightarrow x = 2$. So, ten's digit = 2, unit's digit = 8.

Hence, the required number is 28.

83. Let the ten's digit be x.

Then, number = 10x + 3 and sum of digits = (x + 3).

So,
$$(x+3) = \frac{1}{7}(10x+3) \iff 7x+21$$

= $10x+3 \iff 3x = 18 \iff x = 6$.

Hence, the number is 63.

84. Let the ten's digit be x and the unit's digit be y. Then, number = 10x + y.

$$\therefore 10x + y = k (x + y) \implies k = \frac{10x + y}{x + y}.$$

Number formed by interchanging the digits = 10y + x. Let 10y + x = h(x + y).

Then,
$$h = \frac{10y + x}{x + y} = \frac{11(x + y) - (10x + y)}{x + y}$$

= $11 - \frac{10x + y}{x + y} = 11 - k$.

85. Let the ten's digit be x.

Then, unit's digit = 2x.

Number = 10x + 2x = 12x; Sum of digits = x + 2x = 3x.

$$12x - 3x = 18 \iff 9x = 18 \iff x = 2.$$

Hence, required number = 12x = 24.

86. Let the ten's digit be x and unit's digit be y.

Then, x + y = 15 and x - y = 3 or y - x = 3. Solving x + y = 15 and x - y = 3, we get : x = 9, y = 6. Solving x + y = 15 and y - x = 3, we get : x = 6, y = 9. So, the number is either 96 or 69. Hence, the number cannot be determined.

87. Let the ten's digit be x and the unit's digit be y.

Then, number = 10x + y.

$$\therefore 10x + y = 7(x + y) \iff 3x = 6y \iff x = 2y.$$

Number formed by reversing the digits = 10y + x.

$$\begin{array}{ll} \therefore & (10x+y)-(10y+x)=18 \Leftrightarrow 9x-9y=18 \Leftrightarrow x-y \\ =2 \Leftrightarrow 2y-y=2 \Leftrightarrow y=2. \end{array}$$

So,
$$x = 2y = 4$$
.

Hence, required number = 10x + y = 40 + 2 = 42.

88. Let the ten's digit be x and the unit's digit be y. Then, number = 10x + y.

New number = $10 \times 2x + \frac{y}{2} = 20x + \frac{y}{2}$

$$\therefore 20x + \frac{y}{2} = 10y + x \Rightarrow 40x + y = 20y + 2x$$

$$\Rightarrow$$
 38 $x = 19y \Rightarrow y = 2x$.

So, the unit's digit is twice the ten's digit.

89. Let the ten's digit be x. Then, unit's digit = x + 2.

Number = 10x + (x + 2) = 11x + 2; Sum of digits = x + (x + 2) = 2x + 2.

$$\therefore (11x + 2) (2x + 2) = 144$$

$$\Leftrightarrow 22x^2 + 26x - 140 = 0$$

$$\Leftrightarrow 11x^2 + 13x - 70 = 0$$

$$\Leftrightarrow (x - 2) (11x + 35) = 0$$

$$\Leftrightarrow x = 2.$$

Hence, required number = 11x + 2 = 24.

90. Let the ten's digit be x and unit's digit be y.

Then, number = 10x + y.

Number obtained by interchanging the digits = 10y + x.

$$(10x + y) + (10y + x)$$

= 11 (x + y), which is divisible by 11.

91. Let the ten's digit be x and unit's digit be y.

Then,
$$(10x + y) - (x + y) = 9$$
 or $x = 1$.

From this data, we cannot find y, the unit's digit. So, the data is inadequate.

92. Let the ten's digit be x and unit's digit be y. Then, (10x + y) - (10y + x) = 36

$$\Leftrightarrow 9 (x - y) = 36 \Leftrightarrow x - y = 4.$$

93. Let the ten's digit be x and unit's digit be y.

Then,
$$(10x + y) - (10y + x) = 63$$

$$\Leftrightarrow$$
 9 $(x - y) = 63 \Leftrightarrow x - y = 7.$

Thus, none of the numbers can be determined.

94. Let the ten's digit be
$$x$$
 and unit's digit be y .

Then,
$$x + y = \frac{1}{5} [(10x + y) - (10y + x)]$$

$$\Leftrightarrow \ 5x + 5y = 9x - 9y \ \Leftrightarrow \ 4x = 14y.$$

Thus, the value of (x - y) cannot be determined from the given data.

95. Let ten's digit = x. Then, unit's digit = (12 - x).

$$[10x + (12 - x)] - [10 (12 - x) + x]$$

$$= 54 \Leftrightarrow 18x - 108 = 54 \Leftrightarrow 18x = 162 \Leftrightarrow x = 9.$$

So, ten's digit = 9 and unit's digit = 3. Hence, original number = 93.

96. Since the number is greater than the number obtained on reversing the digits, so the ten's digit is greater than the unit's digit.

Let the ten's and unit's digits be 2x and x respectively.

Then,
$$(10 \times 2x + x) - (10x + 2x) = 36 \Leftrightarrow 9x = 36 \Leftrightarrow x = 4$$
.

$$\therefore \text{ Required difference} = (2x + x) - (2x - x) = 2x = 8.$$

97. Let ten's digit = x. Then, unit's digit = x^2 . Then, number

Clearly, since $x^2 > x$, so the number formed by interchanging the digits is greater than the original number.

$$\therefore (10x^2 + x) - (10x + x^2)$$

$$= 54 \Leftrightarrow 9x^2 - 9x = 54 \Leftrightarrow x^2 - x$$

$$= 6 \Leftrightarrow x^2 - x - 6 = 0$$
$$\Leftrightarrow x^2 - 3x + 2x - 6 = 0$$

$$\Rightarrow x(x + 2) + 2(x + 2) = 0$$

$$\Leftrightarrow x(x-3) + 2(x-3) = 0$$

$$\Leftrightarrow (x-3)(x+2) = 0$$

$$\Leftrightarrow x = 3.$$

So, ten's digit = 3, unit's digit = $3^2 = 9$.

Original number = 39.

Required result = 40% of 39 = 15.6.

98. Let the middle digit be x.

Then,
$$2x = 10$$
 or $x = 5$.

So, the number is either 253 or 352.

Since the number increases on reversing the digits, so the hundred's digit is smaller than the unit's digit. Hence, required number = 253.

99. Since the number reduces on reversing the digits, so ten's digit is greater than the unit's digit.

Let the unit's digit be x.

Then, ten's digit = (x + 1).

$$10x + (x+1) = \frac{5}{6} [10(x+1) + x] \iff 66x + 6$$
$$= 55x + 50 \iff 11x = 44 \iff x = 4.$$

Hence, required number = 54.

- **100.** Let the two-digit number be 10x + y.
 - Then, number formed by reversing the digits = 10y + x.

Difference of squares of the numbers

$$= (10x + y)^2 - (10y + x)^2$$

$$= (100x^2 + y^2 + 20xy) - (100y^2 + x^2 + 20xy)$$

=
$$99(x^2 - y^2)$$
, which is divisible by both 9 and 11

101. Let the unit's digit be x. Then, ten's digit = (x - 2).

$$\therefore 3[10(x-2)+x] + \frac{6}{7}[10x+(x-2)] = 108$$

$$\Leftrightarrow 231x - 420 + 66x - 12 = 756$$

$$\Leftrightarrow$$
 297 $x = 1188$

$$\Leftrightarrow x = 4.$$

Hence, sum of the digits = x + (x - 2) = 2x - 2 = 6.

102. Let the ten's digit be x and unit's digit be y.

Then,
$$\frac{10 x + y}{2} = 10y + (x + 1)$$

$$\Leftrightarrow 10x + y = 20y + 2x + 2$$

$$\Leftrightarrow 8x - 19y = 2 \qquad \dots(i)$$

and
$$x + y = 7$$
 ...(*ii*)

Solving (i) and (ii), we get : x = 5, y = 2. Hence, required number = 52.

103. Let the ten's digit be x.

Then, unit's digit = 2x + 1.

$$[10x + (2x + 1)] - [\{10 (2x + 1) + x\} - \{10x + (2x + 1)\}] = 1$$

$$\Leftrightarrow$$
 $(12x + 1) - (9x + 9) = 1 \Leftrightarrow 3x = 9 \Leftrightarrow x = 3.$

So, ten's digit = 3 and unit's digit = 7. Hence, original number = 37.

104. Let the ten's digit be x and unit's digit be y.

Then,
$$10x + y = 3(x + y) \Rightarrow 7x - 2y = 0$$
 ...(i)

$$10x + y + 45 = 10y + x \Rightarrow y - x = 5$$
 ...(ii)

Solving (i) and (ii), we get : x = 2 and y = 7.

- Required number = 27.
- 105. Let the ten's and unit's digits be x and $\frac{8}{x}$ respectively.

Then,
$$\left(10x + \frac{8}{x}\right) + 18 = 10 \times \frac{8}{x} + x$$

$$\Leftrightarrow 10x^2 + 8 + 18x = 80 + x^2$$

$$\Leftrightarrow 9x^2 + 18x - 72 = 0$$

$$\Leftrightarrow x^2 + 2x - 8 = 0$$

$$\Leftrightarrow$$
 $(x+4)(x-2)=0$

$$\Leftrightarrow$$
 $r=2$

So, ten's digit = 2 and unit's digit = 4. Hence, required number = 24.

- 106. Clearly, there are 4 such numbers: 161, 242, 323 and 404.
- **107.** Let hundred's digit = x.

Then, ten's digit = (x + 1).

Unit's digit = 75% of
$$(x + 1) = \frac{3}{4} (x + 1)$$
.

$$\therefore \quad (x+1)+x=15 \ \Leftrightarrow \ 2x=14 \ \Leftrightarrow \ x=7.$$

So, hundreds' digit = 7; ten's digit = 8; unit's digit = $\frac{3}{4}$

$$(7+1) = \frac{3}{4} \times 8 = 6.$$

Hence, required number = 786.

108. Let the two fractions be a and b. Then, $ab = \frac{14}{15}$ and $\frac{a}{b} = \frac{35}{24}$.

$$\frac{ab}{(a\,/\,b)} = \left(\frac{14}{15} \times \frac{24}{35}\right) \iff b^2 = \frac{16}{25} \iff b = \frac{4}{5};$$

$$ab = \frac{14}{15} \implies a = \left(\frac{14}{15} \times \frac{5}{4}\right) = \frac{7}{6}.$$

Since a > b, so greater fraction is $\frac{7}{6}$.

109.
$$A = 2B \implies B = \frac{1}{2} A$$
. So, $AB = \frac{2}{25}$
 $\Rightarrow \frac{1}{2} A^2 = \frac{2}{25} \implies A^2 = \frac{4}{25} \implies A = \frac{2}{5}$

110. Let the fraction be $\frac{a}{1}$.

Then,
$$\frac{1}{a} - a = \frac{9}{20} \iff \frac{1 - a^2}{a} = \frac{9}{20}$$

$$\Leftrightarrow$$
 20 - 20 a^2 = 9 a

$$\Leftrightarrow 20a^2 + 9a - 20 = 0$$

$$\Leftrightarrow 20a^2 + 25a - 16a - 20 = 0$$

$$\Leftrightarrow 5a (4a + 5) - 4 (4a + 5) = 0$$

$$\Leftrightarrow (4a+5) (5a-4) = 0 \Leftrightarrow a = \frac{4}{5} \cdot \left[\because a \neq -\frac{5}{4} \right].$$

111. Let the fraction be $\frac{x}{y}$.

Then,
$$x + y = 11$$
 ...(*i*)

$$\frac{x+1}{y-2} = \frac{2}{3} \implies 3(x+1)$$

$$= 2(y-2) \implies 3x-2y = -7$$
 ...(ii)

Solving (i) and (ii), we get: x = 3 and y = 8.

So, the fraction is $\frac{3}{8}$.

112. Let the numerator be x. Then, denominator = x + 3.

Now,
$$\frac{x+4}{(x+3)+4} = \frac{4}{5} \iff 5(x+4)$$

$$=4(x+7) \iff x=8$$

So, the fraction is $\frac{8}{11}$.

113. Let the denominator be x.

Then, numerator = x + 5.

Now,
$$\frac{x+5}{x} - \frac{x+5}{x+5} = \frac{5}{4} \iff \frac{x+5}{x} = \frac{5}{4} + 1 = \frac{9}{4} = 2\frac{1}{4}$$
.

So, the fraction is $2\frac{1}{4}$.

114. Let the fraction be $\frac{2x}{3x}$

Then,
$$\frac{2x-6}{3x} = \frac{2}{3} \times \frac{2x}{3x} \Leftrightarrow \frac{2x-6}{3x}$$
$$= \frac{4x}{9x} \Leftrightarrow 18x^2 - 54x = 12x^2$$

$$\Leftrightarrow$$
 $6x^2 = 54x \Leftrightarrow x = 9.$

Hence, numerator of the original fraction = 2x = 18.

115. Let the fraction be $\frac{x}{y}$. Then,

$$\frac{x}{y+1} = \frac{1}{2} \iff 2x - y = 1 \qquad \dots(i)$$

and,
$$\frac{x+1}{y} = 1 \iff x - y = -1 \qquad \dots(ii)$$

Solving (i) and (ii), we get: x = 2, y = 3.

Hence, the required fraction is $\frac{2}{3}$.

116. Let the fraction be $\frac{x}{y}$. Then,

$$\frac{x+2}{y+3} = \frac{7}{9} \iff 9x - 7y = 3 \dots (i)$$

and

$$\frac{x-1}{y-1} = \frac{4}{5} \iff 5x - 4y = 1 \dots (ii)$$

Solving (i) and (ii), we get : x = 5, y = 6.

Hence, the original fraction is $\frac{5}{6}$.

117. Let the fraction be $\frac{x}{y}$. Then,

$$\frac{x + \frac{1}{4}}{y - \frac{1}{2}} = \frac{33}{64} \Leftrightarrow \frac{3(4x + 1)}{4(3y - 1)} = \frac{33}{64} \Leftrightarrow \frac{4x + 1}{3y - 1} = \frac{33}{64} \times \frac{4}{3} = \frac{11}{16}$$

$$\Leftrightarrow$$
 16(4x + 1) = 11(3y - 1)

$$\Leftrightarrow 64x + 16 = 33y - 11$$

 \Leftrightarrow 64x - 33y = -27, which cannot be solved to find $\frac{x}{y}$.

Hence, the original fraction cannot be determined from the given data.

118. Let the fraction be $\frac{x}{y}$

Then,
$$\frac{x + 200\% \text{ of } x}{y + 300\% \text{ of } y} = \frac{15}{26} \Leftrightarrow \frac{3x}{4y} = \frac{15}{26} \Leftrightarrow \frac{x}{y} = \frac{15}{26} \times \frac{4}{3} = \frac{10}{13}$$

119. Let the fraction be $\frac{x}{y}$.

Then,
$$\frac{x+4}{y} - \frac{x}{y} = \frac{2}{3} \iff \frac{4}{y} = \frac{2}{3} \iff y = \left(\frac{4 \times 3}{2}\right) = 6.$$

 \therefore Denominator = 6

120. Let the fraction be $\frac{x}{y}$.

Then,
$$\frac{110\% \text{ of } 2x}{70\% \text{ of } 3y} = 11\% \text{ of } \frac{16}{21} \iff \frac{22x}{21y} = \frac{11}{100} \times \frac{16}{21}$$

$$\Leftrightarrow \quad \frac{x}{y} = \left(\frac{11}{100} \times \frac{16}{21} \times \frac{21}{22}\right) = \frac{2}{25}$$

121. Let the two parts be (54 - x) and x.

Then, $10(54 - x) + 22x = 780 \Leftrightarrow 12x = 240 \Leftrightarrow x = 20$.

:. Bigger part =
$$(54 - x) = 34$$

122. Let the three parts be A, B and C.

Let
$$\frac{A}{2} = \frac{B}{3} = \frac{C}{4} = x$$
.

Then, A = 2x, B = 3x and C = 4x.

So,
$$A : B : C = 2 : 3 : 4$$
.

$$\therefore \quad \text{Largest part} = \left(243 \times \frac{4}{9}\right) = 108.$$

123. Let the four numbers be A, B, C and D.

Let A + 3 = B - 3 = 3C =
$$\frac{D}{3}$$
 = x.

Then, A =
$$x - 3$$
, B = $x + 3$, C = $\frac{x}{3}$ and D = $3x$.

$$A + B + C + D = 64 \implies (x - 3) + (x + 3) + \frac{x}{3} + 3x = 64$$

$$\Rightarrow 5x + \frac{x}{3} = 64 \Rightarrow 16x = 192 \Rightarrow x = 12.$$

Thus, the numbers are 9, 15, 4 and 36.

Required difference =
$$(36 - 4) = 32$$
.

124. Let the numbers be *a*, *b* and *c*. Then, $a^2 + b^2 + c^2 = 138$ and (ab + bc + ca) = 131.

$$(a + b + c)^2 = a^2 + b^2 + c^2 + 2 (ab + bc + ca) = 138 + 2 \times 131 = 400$$

$$\Rightarrow (a+b+c) = \sqrt{400} = 20.$$

125. A: B = 2: 3 and B: C = 5:
$$3 = \frac{3}{5} \times 5: \frac{3}{5} \times 3 = 3: \frac{9}{5}$$

So, A : B : C = 2 : 3 :
$$\frac{9}{5}$$
 = 10 : 15 : 9.

∴ Second number =
$$\left(136 \times \frac{15}{34}\right) = 60$$
.

126. Let the numbers be x, y and z.

Then, x + y = 73, y + z = 77 and 3x + z = 104.

$$y = 73 - x$$
, $z = 77 - y = 77 - (73 - x) = 4 + x$.

$$3x + 4 + x = 104 \Leftrightarrow 4x = 100 \Leftrightarrow x = 25.$$

$$y = (73 - 25) = 48 \text{ and } z = (4 + 25) = 29.$$

- \therefore Third number = 29.
- **127.** Let two numbers be a and b

Given
$$ab = 5$$
 and $a = \frac{3}{2}$

$$\Rightarrow b = \frac{5}{a}$$

$$b = \frac{5}{3} = \frac{5 \times 2}{3} = \frac{10}{3}$$

 \therefore Required sum of $a + b = \frac{3}{2} + \frac{10}{3}$

LCM of 2 and
$$3 = 6$$

$$=\frac{9+20}{6}=\frac{29}{6}=4\frac{5}{6}$$

128. Let the positive integers be a and b where a > b. According to the question,

$$a^2 + b^2 = 100$$
(i)

$$a^2 - b^2 = 28$$
(

By adding (i) and (ii), we get

$$a^2 + b^2 + a^2 - b^2 = 100 + 28$$

$$\Rightarrow 2a^2 = 128$$

$$\Rightarrow a^2 = \frac{128}{2} = 64$$

:.
$$a = \sqrt{64} = 8$$

From equation (i).

$$8^2 + b^2 = 100$$

$$\Rightarrow b^2 = 100 - 64 = 36$$

$$\Rightarrow b = \sqrt{36} = 6$$

$$a+b=8+6=14$$

129. Let the numbers be a and b where a > b.

According to the question,

$$a + b = 37$$
 and $a^2 - b^2 = 185$

$$\Rightarrow (a+b)(a-b) = 185$$

$$\Rightarrow 37(a-b) = 185$$

$$\Rightarrow a - b = \frac{185}{37} = 5$$

130. Let the total number of eggs bought be a.

10% of eggs are rotten.

:. Remaining eggs

$$= a - 10\%$$
 of $a = a - \frac{10a}{100} = \frac{100a - 10a}{100} = \frac{90a}{100} = \frac{9a}{100}$

Man gives 80% of $\frac{9a}{100}$ eggs to his neighbour

$$=\frac{80}{100}\times\frac{9a}{10}=\frac{72a}{100}$$

Remaining eggs = $\frac{9a}{10} - \frac{72a}{100} = \frac{90a - 72a}{100} = \frac{18a}{100} = \frac{9a}{50}$

According to the question.

$$\frac{9a}{50} = 36 \Rightarrow 9a = 36 \times 50$$

$$\Rightarrow a = \frac{36 \times 50}{9} = 200$$

Hence the total number of eggs. bought be 200.

131. Let the numbers be a and b.

According to the question.

$$a + b = 75$$

$$a - b = 25$$

$$\therefore (a+b)^2 - (a-b)^2 = 4ab$$

$$\Rightarrow 75^2 - 25^2 = 4ab$$

$$4ab = (75 + 25)(75 - 25)$$

$$\left[\because a^2 - b^2 = (a+b)(a-b) \right]$$

$$\Rightarrow 4ab = 100 \times 50$$

$$\Rightarrow ab = \frac{100 \times 50}{4} = 1250$$

132. Let the five successive odd number be, x, x+2, x+4, x+6, x+8

Then, according to given information 185 = x + x + 2 + x + 4 + x + 6 + x + 8

$$\Rightarrow 185 = 5x + 20$$

$$\Rightarrow 5x = 185 - 20 = 165$$

$$\Rightarrow x = 33$$

Highest number = 33 + 8 = 41

133. Let the numbers be a and b where a > b.

According to the questions,

$$a - b = 10$$
 ...

And
$$\frac{a+b}{5} = 8$$

By cross multiplying, we get

$$\Rightarrow a + b = 40$$
 ...(ii)

By subtracting equation (ii) from (i) we get

$$2b = 40 - 10 = 30$$

$$\Rightarrow b = \frac{30}{2} = 15$$

And from (i)

$$a = 10 + 15 = 25$$

$$\Rightarrow a = 23$$

EXERCISE

(DATA SUFFICIENCY TYPE QUESTIONS)

Directions (Questions 1 to 15): Each of the questions given below consists of a statement and/or a question and two statements numbered I and II given below it. You have to decide whether the data provided in the statement(s) is/are sufficient to answer the question. Read both the statements and

Give answer (a) if the data in Statement I alone are sufficient to answer the question, while the data in Statement II alone are not sufficient to answer the question;

Give answer (b) if the data in Statement II alone are sufficient to answer the question, while the data in Statement I alone are not sufficient to answer the question;

Give answer (c) if the data either in Statement I or in Statement II alone are sufficient to answer the question;

Give answer (d) if the data even in both Statements I and II together are not sufficient to answer the question;

Give answer (e) if the data in both Statements I and II together are necessary to answer the question.

- 1. What is the two-digit number? (Bank P.O., 2008)
 - I. The difference between the two digits is 9.
 - II. The sum of the digits is equal to the difference between the two digits.
- **2.** What is the value of the two-digit number *ab*?
 - I. The difference between its digits is 2.
 - II. The sum of its digits is 4.
- **3.** What is the two-digit number where the digit at the unit's place is smaller?
 - I. The difference between the two digits is 5.

(Bank P.O., 2006)

(M.A.T., 2005)

- II. The sum of the two digits is 7.
- 4. How much is four-fifths of the number? (Bank P.O., 2009)
 - Three-fourths of the number is 2.5 less than its fourfifths.
 - II. Half of the number added to it is 75.
- 5. What is the smaller of the two numbers?
 - **I.** The difference between these two numbers is one-third of the greater number.
 - II. The sum of these two numbers is 30.

6. What is the two-digit number? (Bank

(Bank P.O., 2009)

- **I.** Sum of the digits is 6.
- **II.** Digit in the ten's place is double the digit in the unit's place.
- 7. What is the difference between the digits of a two-digit number? (M.A.T., 2007)
 - **I.** The sum of the digits of that number is 8.
 - II. One-fifth of that number is 15 less than half of 44.
- 8. What is the three-digit number? (Bank P.O., 2008)
 - **I.** Two-fifth of that number is less than half of that number by 20.
 - II. One-fourth of that number is 25% of that number.
- **9.** What is the difference between two two-digit numbers?

(Bank. P.O., 2010)

- **I.** The square of the first number is 9 times the second number.
- **II.** The ratio of the first number to the second number is 3:4.
- 10. What is the third number of 8 consecutive real numbers?

(M.A.T., 2001)

- I. Product of the numbers is 34,459,425.
- II. Sum of numbers is 84.
- 11. What is the ratio between the two numbers?
 - I. The sum of two numbers is twice their difference.
 - II. The smaller number is 6.
- **12.** What is the two-digit number whose first digit is *a* and the second digit is *b*? The number is greater than 9.

(M.A.T., 2000)

- **I.** The number is a multiple of 51.
- **II.** The sum of the digits *a* and *b* is 6.
- 13. What is the two-digit number? (SIDBI, 2006)
 - **I.** The sum of the two digits of the number is 13.
 - II. The number obtained by interchanging the two digits of the number is smaller than the original number by 45.
- 14. What is the original number? (M.B.A., 2007)
 - **I.** Sum of the two digits of a number is 10. The ratio between the two digits is 1 : 4.

- II. Product of two digits of a number is 16 and quotient of two digits is 4.
- 15. What is the value of the two-digit number?

(Bank P.O., 2009)

- I. The product of the digits is 72 and the difference between the digits is 1.
- II. The digit at the unit place is greater than the other.

Directions (Questions 16 to 22): Each of the questions given below consists of a question followed by three statements. You have to study the question and the statements and decide which of the statement(s) is/are necessary to answer the given question.

16. What is the two-digit number?

(M.B.A., 2002)

- I. Sum of the digits is 7.
- II. Difference between the number and the number obtained by interchanging the digits is 9.
- III. Digit in the ten's place is bigger than the digit in the unit's place by 1.
- (a) I and II only
- (b) II and III only
- (c) I and III only
- (d) All I, II and III
- (e) None of these
- 17. What is the sum of the digits of the two-digit number?
 - I. The ratio between the ten's digit and unit's digit of the number is 3:2.
 - II. The number obtained on revering the order of its digits is 18 less than the original number.
 - III. The product of the digits is 24.
 - (a) Any two of the three
- (b) I only or II and III only
- (c) All I, II and III
- (d) I and II only
- (e) None of these
- 18. What will be the sum of two numbers?
 - I. Among the two numbers, the bigger number is greater than the smaller number by 6.
 - II. 40% of the smaller number is equal to 30% of the bigger number.
 - III. The ratio between half of the bigger number and one-third of the smaller number is 2:1.

- (a) I and II only
- (b) II and III only
- (c) All I, II and III
- (d)Any two of the three
- (e) None of these
- **19.** What is the two-digit number?

(M.A.T., 2005)

- I. The difference between the two-digit number and the number formed by interchanging the digits is 27.
- **II.** The difference between the two digits is 3.
- III. The digit at unit's place is less than that at ten's place by 3.
- (a) I and II only
- (b) I and III only
- (c) All I, II and III
- (d) I, and either II or III
- (e) Even with all I, II and III, answer cannot be given.
- **20.** What is the two-digit number? (Bank P.O., 2004)
 - I. Digit in the ten's place is cube of the digit in unit's place.
 - II. Digit in the ten's place is four times the digit in the unit's place.
 - III. The two digits are not equal.
 - (a) I and II only
- (b) I and III only
- (c) Any two of the three
 - (d) I and either II or III only
- (e) None of these
- 21. Find three positive consecutive even numbers.

(M.A.T., 2006)

- I. The average of four consecutive even numbers starting from the last of the given numbers is 17.
- II. The difference of the highest and the lowest numbers
- **III.** The sum of the squares of the three numbers is 440.
- (a) I only
- (b) I and II only
- (c) III only
- (d) Either I or III
- **22.** What is the two-digit number? (Bank P.O., 2006)
 - I. The number obtained by interchanging the digits of the number is greater than the original number by
 - II. Sum of the digits of the number is 14.
 - III. Difference between the two digits of the number is 2.

 - (a) Any two of the three (b) Only I and III
 - (c) II and either I or III
- (d) III and either I or II
- (e) All of these

ANSWERS

(1. (a)	2. (<i>d</i>)	3. (<i>e</i>)	4. (c)	5. (<i>e</i>)	6. (<i>e</i>)	7. (<i>b</i>)	8. (a)	9. (<i>e</i>)	10. (b)
	11. (a)	12. (<i>a</i>)	13. (<i>e</i>)	14. (<i>b</i>)	15. (<i>e</i>)	16. (<i>e</i>)	17. (<i>a</i>)	18. (<i>e</i>)	19. (<i>e</i>)	20. (<i>a</i>)
	21. (<i>d</i>)	22. (c)								

SOLUTIONS

- 1. I. Two digits with difference 9 are 9 and 0. And, the two-digit number formed using 9 and 0 is 90.
 - **II.** Let the ten's and unit's digits be *x* and *y* respectively. Then, $x - y = x + y \Leftrightarrow 2y = 0 \Leftrightarrow y = 0$. So, the ten's digit cannot be determined. Thus, I only gives the answer, while II does not. \therefore The correct answer is (a).
- **2. I.** gives, a b = 2b - a = 2or
- ...(i) ...(ii)
- gives, a + b = 4

...(iii)

Solving (i) and (iii), we get : a = 3 and b = 1. Solving (ii) and (iii), we get : a = 1 and b = 3.

So, the required number is either 13 or 31.

Thus, even both I and II together do not give the answer.

 \therefore The correct answer is (*d*).

- **3.** Let the ten's and unit's digits be *x* and *y* respectively, where *x* > *y*.
 - I. gives, x y = 5 ...(i)
 - I. gives, x + y = 7 ...(*ii*)

Solving (i) and (ii), we get : x = 6 and y = 1. So, the required number is 61.

Thus, both I and II together give the answer.

- \therefore The correct answer is (*e*).
- **4.** Let the required number be x.

I.
$$\frac{4}{5}x - \frac{3}{4}x = 2.5 \Leftrightarrow \frac{x}{20} = 2.5 \Leftrightarrow x = 50.$$

So,
$$\frac{4}{5} x = \left(\frac{4}{5} \times 50\right) = 40.$$

II.
$$x + \frac{x}{2} = 75 \iff \frac{3x}{2} = 75 \iff x = \left(\frac{75 \times 2}{3}\right) = 50.$$

So,
$$\frac{4}{5}x = \left(\frac{4}{5} \times 50\right) = 40.$$

Thus, either I or II alone gives the answer.

- \therefore The correct answer is (*c*).
- **5. II.** Let the greater number be x. Then, smaller number = (30 x).

I.
$$x - (30 - x) = \frac{x}{3} \Leftrightarrow 2x - 30 = \frac{x}{3} \Leftrightarrow 6x - 90 = x$$

$$\Leftrightarrow$$
 $5x = 90 \Leftrightarrow x = 18.$

So, smaller number = 30 - 18 = 12.

Thus, both I and II together give the answer.

- \therefore The correct answer is (e).
- **6.** Let the ten's and unit's digits be *x* and *y* respectively.

I.
$$x + y = 6$$
 ...(*i*)

II.
$$x = 2y$$
 ...(*ii*)

Solving (i) and (ii), we get : x = 4, y = 2. So, the required number is 42.

Thus, both I and II together give the answer.

- \therefore The correct answer is (e).
- **7. I.** Let the ten's and unit's digits of the number be *a* and *b* respectively.

Then, a + b = 8.

II. Let the required number be x.

Then,
$$\frac{x}{5} = \left(\frac{1}{2} \text{ of } 44\right) - 15 = 7 \iff x = 35.$$

So, the required number is 35.

Thus, II alone gives the answer.

- \therefore The correct answer is (*b*).
- **8.** Let the required number be x.

I.
$$\frac{x}{2} - \frac{2x}{5} = 20 \Leftrightarrow \frac{5x - 4x}{10} = 20 \Leftrightarrow \frac{x}{10} = 20 \Leftrightarrow x = 200.$$

II.
$$\frac{x}{4} = 25\%$$
 of $x \Leftrightarrow \frac{x}{4} = \frac{x}{4}$

Thus, I alone gives the answer.

 \therefore The correct answer is (a).

- **9. II.** Let the two numbers be 3x and 4x.
 - $I. \qquad (3x)^2 = 9 \times 4x \Leftrightarrow 9x^2 = 36x \Leftrightarrow x = 4.$

So, the numbers are 12 and 16.

 \therefore Required difference = 16 - 12 = 4.

Thus, both I and II together give the answer.

 \therefore The correct answer is (e).

- **10.** Let the 8 consecutive real numbers be x, (x + 1), (x + 2), (x + 3), (x + 4), (x + 5), (x + 6) and (x + 7).
 - I. gives, x(x + 1)(x + 2)(x + 3)(x + 4)(x + 5)(x + 6)(x + 7) = 34459425.

This equation cannot be solved for x.

- II. gives, x + (x + 1) + (x + 2) + (x + 3) + (x + 4) + (x + 5) + (x + 6) + (x + 7) = 84 $\Leftrightarrow 8x + 28 = 84 \Leftrightarrow 8x = 56 \Leftrightarrow x = 7.$
- .. Third number = x + 2 = 7 + 2 = 9.

Thus, II alone gives the answer.

- \therefore The correct answer is (b).
- **11.** Let the two numbers be x and y.
 - I. gives, $x + y = 2(x y) \iff x = 3y$

$$\Leftrightarrow \frac{x}{y} = \frac{3}{1} \Leftrightarrow x : y = 3 : 1.$$

Thus, I only gives the answer.

- II. does not give the answer.
- \therefore Correct answer is (a).
- **12.** The only two-digit number which is a multiple of 51, is 51. So, I alone gives the answer while II alone does not.
 - \therefore The correct answer is (a).
- **13.** Let the ten's digit be x and the unit's digit be y.

Then, number = 10x + y.

- I. $x + y = 13 \Leftrightarrow y = (13 x)$.
- So, number = 10x + (13 x).
- II. [10x + (13 x)] [10(13 x) + x] = 45 $\Leftrightarrow (9x + 13) - (130 - 9x) = 45$

$$\Leftrightarrow 18x = 162 \Leftrightarrow x = 9.$$

$$y = 13 - x = 13 - 9 = 4$$
.

So, required number = 94.

Thus, both I and II together give the answer.

- The correct answer is (e).
- **14.** Let the ten's and unit's digits be x and y respectively.

I.
$$x + y = 10 \text{ and } \frac{x}{y} = \frac{1}{4}$$

II. xy = 16 and $\frac{x}{y} = \frac{4}{1}$.

$$\therefore$$
 II gives, $x^2 = 64 \Leftrightarrow x = 8$. So, $4y = 8 \Leftrightarrow y = 2$.

Thus, II alone gives the answer while I alone does not.

- \therefore The correct answer is (*b*).
- **15.** Let the ten's digit be x and the unit's digit be y.
 - II. y > x.
 - I. xy = 72 and y x = 1 or y = x + 1

$$\Leftrightarrow x(x+1) = 72 \Leftrightarrow x^2 + x - 72 = 0$$

$$\Leftrightarrow x^2 + 9x - 8x - 72 = 0$$

$$\Leftrightarrow x(x+9) - 8(x+9) = 0$$

$$\Leftrightarrow$$
 $(x+9)(x-8)=0 \Leftrightarrow x=8.$

So,
$$y = x + 1 = 9$$

 \therefore Required number = 89.

Thus, both I and II together give the answer.

- \therefore The correct answer is (*e*).
- **16.** Let the ten's and unit's digit be x and y respectively.
 - I. x + y = 7.

II.
$$(10x + y) - (10y + x) = 9 \implies x - y = 1.$$

III.
$$x - y = 1$$
.

Thus, I and II as well as I and III give the answer. \therefore Correct answer is (e).

17. Let the ten's and unit's digit be 3x and 2x respectively.

II.
$$(30x + 2x) - (20x + 3x) = 18 \iff x = 2$$
.

III.
$$3x \times 2x = 24 \iff x^2 = 4 \iff x = 2$$
.

Thus, any two of the three will give the answer.

 \therefore Correct answer is (a).

18. Let the required numbers be x and y, where x > y.

I.
$$x - y = 6$$
 ...(*i*)

II.
$$\frac{30}{100}x = \frac{40}{100}y \iff 3x - 4y = 0$$
 ...(ii)

III.
$$\frac{\frac{1}{2}x}{\frac{1}{3}y} = \frac{2}{1} \Leftrightarrow \frac{3x}{2y} = \frac{2}{1} \Leftrightarrow \frac{x}{y} = \frac{4}{3} \Leftrightarrow 3x - 4y = 0$$
 ...(iii)

So, we may solve (i) and (ii) or (i) and (iii) together to find x and y.

Thus, I, and either II or III together give the answer.

- \therefore Correct answer is (e).
- **19.** Let the ten's and unit's digit be x and y respectively.

I.
$$(10x + y) - (10y + x) = 27 \iff x - y = 3$$
.

II.
$$x - y = 3$$
.

III.
$$x - y = 3$$
.

Thus, even all the given three statements together do not give the answer.

- \therefore Correct answer is (*e*).
- **20.** Let the ten's digit be x and the unit's digit be y.

I.
$$x = y^3$$
 ...(*i*)

II.
$$x = 4y$$
 ...(ii)

III.
$$x \neq y$$
 ...(iii)

From (i) and (ii), we have : $y^3 = 4y \Leftrightarrow y^3 - 4y = 0$ $\Leftrightarrow y (y^2 - 4) = 0$

$$\Leftrightarrow y^2 - 4 = 0$$

$$\Leftrightarrow y^2 = 4 \Leftrightarrow y = 2.$$

So,
$$x = y^3 = 2^3 = 8$$
.

:. The required number is 82.

Thus, I and II together give the answer.

- Correct answer is (a).
- **21.** Let the three consecutive even numbers be x, (x + 2) and (x + 4).

I.
$$\frac{(x+4)+(x+6)+(x+8)+(x+10)}{4} = 17$$

$$\Leftrightarrow$$
 $4x + 28 = 68 \Leftrightarrow 4x = 40 \Leftrightarrow x = 10.$

So, the required numbers are 10, 12 and 14.

II.
$$(x + 4) - x = 4 \iff 4 = 4$$
.

So, the value of x cannot be determined.

III.
$$x^2 + (x + 2)^2 + (x + 4)^2 = 440$$

$$\Leftrightarrow x^2 + x^2 + 4 + 4x + x^2 + 16 + 8x = 440$$

$$\Leftrightarrow 3x^2 + 12x - 420 = 0$$

$$\Leftrightarrow x^2 + 4x - 140 = 0$$

$$\Leftrightarrow x^2 + 14x - 10x - 140$$

$$\Leftrightarrow$$
 $x(x + 14) - 10(x + 14) = 0$

$$\Leftrightarrow$$
 $(x + 14) (x - 10) = 0$

$$\Leftrightarrow x = 10.$$

So, the required numbers are 10, 12 and 14.

Thus, I alone or III alone gives the answer.

- \therefore Correct answer is (*d*).
- **22.** Let the ten's digit be x and unit's digit be y.

(I and II).
$$x + y = 14$$
 or $y = (14 - x)$...(i)

And,
$$[10 (14 - x) + x] - [10x + (14 - x)]$$

= 18 \Leftrightarrow (140 - 9x) - (9x + 14) = 18

$$\Leftrightarrow 18x = 108 \Leftrightarrow x = 6.$$

So,
$$y = 14 - 6 = 8$$
.

 \therefore Required number = 68.

(II and III).
$$x + y = 14$$
 ...(ii)

and
$$x - y = \pm 2$$
 ...(iii)

Solving (ii) and (iii), we get : x = 6 or 8.

If
$$x = 6$$
, $y = 8 & If $x = 8$, $y = 6$.$

:. Required number is either 68 or 86.

(I and III). Since the number obtained by interchanging the digits is greater, the ten's digit is smaller than the unit's digit.

$$x + y = 14 \qquad \dots (iv)$$

And,
$$y - x = 2$$
 ...(v)

Solving (iv) and (v), we get : y = 8.

So,
$$x = 14 - y = 6$$
.

:. Required number = 68.

Thus, II and either I or III gives the answer.

 \therefore Correct answer is (*c*).