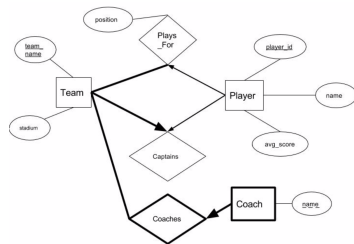


## 1 ER Diagrams

We want to store sports teams and their players in our database. Draw an ER diagram corresponding to data given below:

- Every Team in our database will have a unique team\_name and a stadium where they play their games.
- Each Coach has a name.
- Each Player will have a player\_id, name and their average score.
- Our database will contain who Plays\_For which team and also the "position" that the player plays in. We also need to store who Captains a team, and who Coaches a team.
- Every Team needs players, and needs exactly one captain.
- Each Player can be on at most one team, but may currently be a free agent and not on any team.
- Each team needs coaches and may have many.
- A Coach is uniquely identified by which team they coach.



## 2 Functional Dependencies

1. When there's a lot of symbols floating around, it's best to keep track of the "type" of the various symbols and expressions. Consider a set of functional dependencies  $F = \{X \rightarrow Y, Y \rightarrow Z\}$ . For each of the following symbols or expressions, indicate whether it is (a) an attribute, (b) a set of attributes, (c) a set of sets of attributes, (d) a functional dependency, (e) a set of functional dependencies, or (f) none of the above.

- X (b) a set of attributes
- XY (b) a set of attributes
- $X \rightarrow Y$  (d) a functional dependency
- F (e) a set of functional dependencies
- $F+$  (e) a set of functional dependencies
- $X+$  (b) a set of attributes
- Armstrong's reflexivity axiom (f) an axiom

2. Consider a relation  $R(x, y, z)$  and the list of functional dependencies  $X \rightarrow Y, XY \rightarrow YZ$ , and  $Y \rightarrow X$  where  $X = \{x\}$ ,  $Y = \{y\}$ , and  $Z = \{z\}$ . For each of the following relations, indicate which functional dependencies it might satisfy.

x	y	z
1	2	0
1	2	1
1	3	0
2	3	0

x	y	z
1	2	1
1	3	1
2	3	0

x	y	z
1	3	1
1	3	1
2	3	0

x	y	z
1	3	1
1	3	1
1	3	1

- None
- $XY \rightarrow YZ$
- $X \rightarrow Y, XY \rightarrow YZ$
- $X \rightarrow Y, XY \rightarrow YZ, Y \rightarrow X$

3. Consider the set  $F = \{A \rightarrow B, AB \rightarrow AC, BC \rightarrow BD, DA \rightarrow C\}$  of functional dependencies. Compute the following attribute closures.

- $A+$  ABCD
- $B+$ ,  $C+$ ,  $D+$  B, C, D; B, C, and D do not appear alone on the left of any functional dependency, so nothing is in their attribute closures besides themselves.
- $AB+$ ,  $AC+$ ,  $AD+$  ABCD;  $A+ = ABCD$ , so  $AX = ABCD$  for any X.

- BC+ BCD
- BD+ BD
- CD+ CD
- BCD+ BCD

4. Consider again the set F of functional dependencies from Question 3. Indicate whether the following sets of attributes are candidate keys, superkeys (but not candidate keys), or neither.

- A candidate key
- B, C, D neither
- AB, AC, AD superkey
- BC neither
- BD neither
- CD neither
- BCD neither

## 3 Normal Forms

1. Decompose  $R = ABCDEFG$  into BCNF, given the functional dependency set:  $F = \{AB \rightarrow CD, C \rightarrow EF, G \rightarrow A, G \rightarrow F, CE \rightarrow F\}$ .

$AB \rightarrow CD \Rightarrow$  decompose ABCDEFG into ABCD, ABEFG  
 $G \rightarrow A \Rightarrow$  decompose ABEFG into AG, BEFG  
 $G \rightarrow F \Rightarrow$  decompose BEFG into FG, BEG  
 Final relations: ABCD, AG, FG, BEG.

2. Does the above decomposition preserve dependencies? Why/why not?

No,  $C \rightarrow EF$  and  $CE \rightarrow F$  are not represented in the closure of the union of each subrelation's dependencies.