

## Association Analysis

"association" in a rule

quantify the strength of this association.

mining of these rules from a list of thousands of items using Apriori Algorithm.

### Market basket Analysis

↓  
Association Rules.

helping stores cross-sell in the process.

Association - Do not tie back a user's different transactions overtime to identify relationships.

- List of items with unique transaction IDs from all users are studied as one group.

Collaborative filtering - Ties back all transactions corresponding to a user ID to identify similarity between user preferences.

Association Rules

- Antecedent {items}
- Consequent {items}

itemset - Items of both Ant. and Cons.

Various metrics to understand strength b/w Ant. and Cons.

1) Support

2) Confidence

3) Lift.

$\{\text{Bread, Egg}\} \rightarrow \{\text{milk}\}$   
Antecedent                      Consequent

Itemset =  $\{\text{Bread, Egg, milk}\}$

$$\text{Support}(\{x\} \rightarrow \{y\}) = \frac{\text{no}(x \text{ and } y)}{\text{Total Transactions}} \quad \left| \quad \text{Support}(\{y\}) = \frac{\text{no.}(y)}{\text{Total.}} \right.$$

$$\text{Confidence}(\{x\} \rightarrow \{y\}) = \frac{\text{no.}(x \text{ and } y)}{\text{no.}(x)}$$

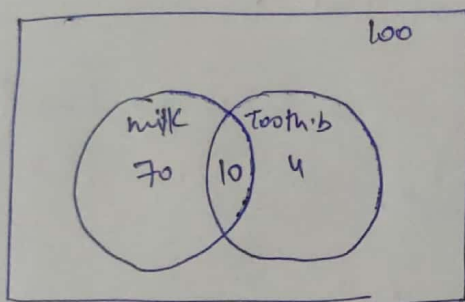
Similar to  $P(y|x)$

$\{Yogurt\} \rightarrow \{Milk\}$

$\{Butter\} \rightarrow \{Bread\}$

$\{Toothbrush\} \rightarrow \{Milk\} \rightarrow ???$

Very frequent Consequent  $\Rightarrow$  high confidence



$$\text{Confidence}(\{Toothbrush\} \rightarrow \{milk\}) = \frac{10}{10+4} = 0.7$$

$$\text{Lift} = \frac{\text{Confidence}(\{x\} \rightarrow \{y\})}{\text{Fraction of } \{y\}} = \frac{0.7}{80/100} = 0.87 < 1$$

$$\text{Lift} = \frac{\text{Confidence}(\{x\} \rightarrow \{y\})}{\text{Support}(\{y\})}$$

Next step  $\rightarrow$  Association Rule mining for entire list of items.

10 items  $\rightarrow$  will lead to 57000 rules.

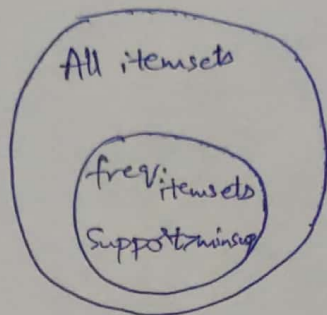
Hence

**Apriori Algorithm**

## Rule generation process

- 1) Generate an item set.
- 2) Generate a rule from each itemset.

Step 1



Brute force technique  $\rightarrow$  form all possible itemsets

Apriori principle

- All subsets of a frequent itemset must also be frequent.

Anti-monotone property of support.

$$\text{Support}(\{a\}, \{b\}, \{c\}) < \text{Support}(\{a\}, \{b\}) \\ < \text{Support}(\{a\}).$$

Helpful in pruning of infrequent itemsets.

Step 2 Generating all possible rules from the frequent itemsets.

Do a binary partition of each itemset.

Confidence of rules generated from the same itemset also follows an anti-monotone property (w.r.t consequent)

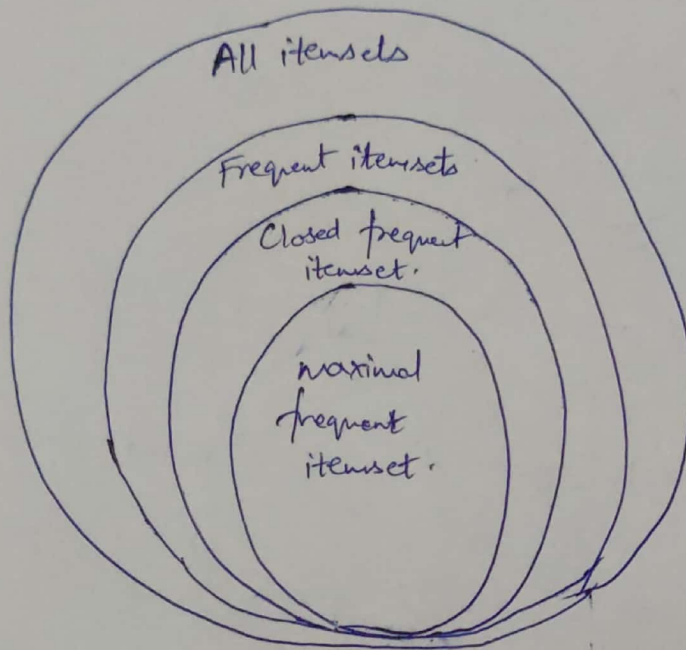
$$\text{Conf}(A, B, C \rightarrow D) \geq \text{Conf}(B, C \rightarrow A, D) \geq \text{Conf}(C \rightarrow A, B, D)$$

$$\text{Conf}(X \rightarrow Y) = \frac{\text{Support}(X, Y)}{\text{Support}(X)}$$



Thus after ~~so~~ step 1 and 2, we get subset of Rules.

In these subset of Rules, search for the ones which give highest lift.



max. frequent itemset

$\{x\}$        $\{x, y\}$        $\rightarrow$  frequent itemset with none of  
 minsup ☒      minsup ☐      the immediate supersets  
    are frequent.

Closed frequent itemset

$$\text{Support}(\{x\}) \neq \text{Support}(\{x, y\})$$

Means  $x$  is not accompanied by occurrence of  $y$ .

apriori, mlxtend.

## Eclat Algorithm

↳ Equivalence class clustering and bottom-up lattice traversal.

Apriori algorithm works in a horizontal sense  
(Breadth first search of a graph)

Eclat algorithm works in a vertical sense  
(Depth-first search of a graph)

The basic idea is to use transaction ID sets (tidsets) intersections to compute the support value of a candidate and avoiding the generation of subsets which do not exist in the prefix tree.

FP-Growth tree → No library for this available.