

T-SNE on MNIST

Group points based on their visual similarity.

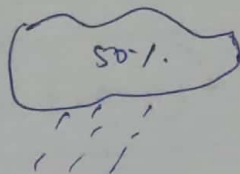
Visual a 784d dataset $\xrightarrow{\text{by embedding the dataset}}$ 2D

Entropy, Cross-Entropy and KL-Divergence

↓
Cost fn for
classifiers

Claude Shannon
↓
Information theory.

→ to transmit 1 bit of
info is to reduce
the recipient's
uncertainty by 2.

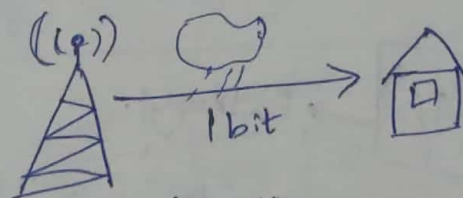


$$P = \frac{1}{2}$$

$$\text{now } P = \frac{1}{2} \times 2 = 1$$

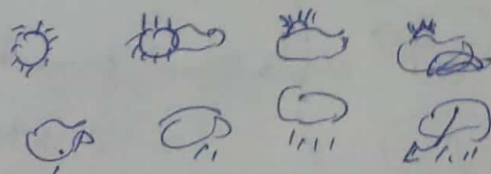
~~2~~

$$\frac{1}{2} = 2$$



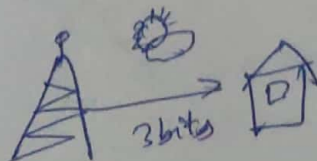
"Raining"

40 bit message \Rightarrow but actually 1 bit of info.



$$2^3 = 8$$

\Rightarrow 3 bits.

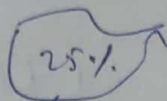


\Rightarrow Dividing your uncertainty
by a factor of 8.
 \Rightarrow 3 bits of useful info.

$$\log_2(8) = 3$$

↓
binary logarithm
of the uncertainty
reduction factor

$$\log\left(\frac{1}{n}\right) = -\log(n)$$



?

How much info. from the weather
station are you getting on an
average?

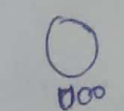
$$\begin{aligned} & 75\% \cdot [-\log_2(0.75)] \\ & + 25\% \cdot [-\log_2(0.25)] \\ & = 75\% \cdot [0.41] + 25\% \cdot [2] \\ & = \underline{\underline{0.81 \text{ bits}}} \end{aligned}$$

(or)

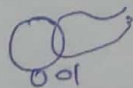
Avg. amt of info.
from 1 sample from
a probability
distribution.

$$H(P) = \left[-\sum_i P_i \log_2(P_i) \right] \rightarrow \text{Entropy.}$$

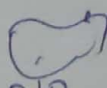
Cross-Entropy \rightarrow Avg. msg length. $\rightarrow \underline{\underline{3 \text{ bits}}}$



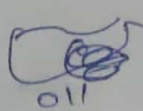
000



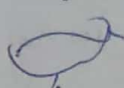
001



010



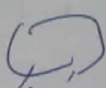
011



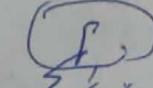
100



101

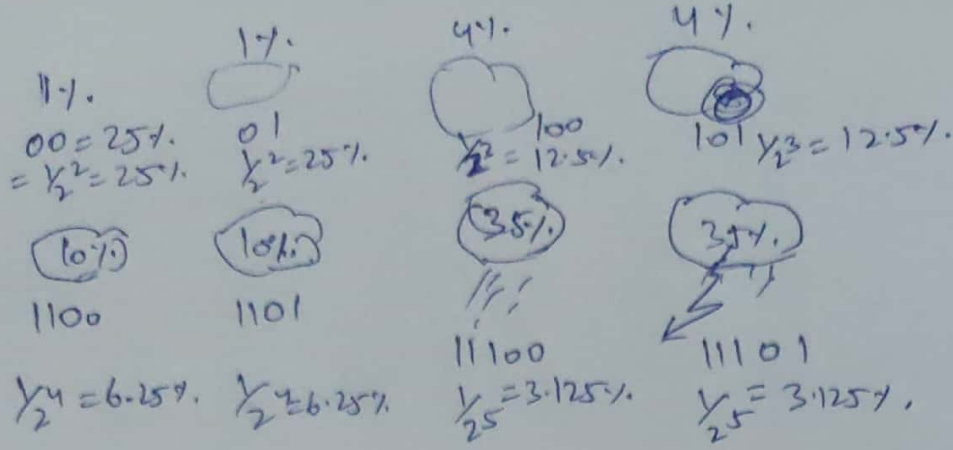


110



111

} Equal probability
 $\Rightarrow 3 \text{ bits}$



P = true distribution. (sums to 100%)
 q = predicted distribution. (Does not sum to 100%)

$$H(P) = -\sum_i P_i \log_2(P_i) \rightarrow \text{Entropy.}$$

$$H(P, q) = -\sum_i P_i \log_2(q_i) \rightarrow \text{Cross Entropy.}$$

$$\text{Cross-Entropy} = \text{Entropy} + \text{KL Divergence}$$

$$D_{KL}(P \parallel q) = H(P, q) - H(P)$$

$$\log_2(x) = \frac{\log(x)}{\log(2)}$$

True Distribution

Predicted Distribution

Hot vector, i.e. 1 class has a prob. of 100% (true class)

0%	0%	0%	0%	100%	0%	0%
Cat	Dog	Fox	Goat	Panda	Bear	Dolphin
2%	30%	45%	0%	25%	5%	0%

$$\text{Cross Entropy loss} = -\sum_i P_i \log(q_i)$$

$$= -1 \cdot \log(0.25) = 1.386$$

In case this is 0.
 $-\log(0) = \text{undefined} \rightarrow \text{cost will grow very large.}$
 In case this is 100%.

$-\log(1) = 0$
 If both distributions are same $C.E = \text{Entropy}$