

# Utilization of environmental and epidemiological indicators in the study of malaria dynamics

Raphael Felberg Levy<sup>a</sup>, Flavio Codeço Coelho<sup>a</sup>

<sup>a</sup>School of Applied Mathematics, EMAP FGV, Praia de Botafogo 190, Rio de Janeiro, 22250-145, RJ, Brazil

## ARTICLE INFO

### Keywords:

Biological modelling  
Malaria  
Amazon  
SIR  
SEI

## ABSTRACT

This paper aims to analyze the behavior of malaria transmission in the Amazon region based on climatic and environmental changes, such as temperature, precipitation and deforestation, through proposed modifications to the SIR and SEI models, in order to contribute to the study of applications of external effects on the evolution of the disease. The Trajetórias Project, developed by the Synthesis Center on Biodiversity and Ecosystem Services (SinBiose/CNPq) was used as an initial reference for the study. This work employs a modified SIR/SEI methodology, based on work from Parham and Michael (2010) which takes into account rainfall and temperature, with further modifications to avoid delay equations. Primary results show that the model is too sensible on some parameters, and using values indicated by other papers did not give the same results, opening up future work to compare the modified model equations with the originals. With the obtained results, it was possible to verify a strong effect caused by increased contact of host and vectors on the transmission of the disease.

## 1. Introduction

The Amazon is one of the largest and most biodiverse tropical forests in the world, harboring numerous species of plants, animals, and microorganisms, including vectors and pathogens responsible for the transmission of various diseases. Among them, one of the most common is malaria, caused by protozoa of the genus *Plasmodium*, transmitted by the bite of the infected female mosquito of the genus *Anopheles*. It is present in 22 American countries, but the areas with the highest risk of infection are located in the Amazon region, encompassing nine countries, which accounted for 68% of infection cases in 2011 [? ]. Although malaria is prevalent in the Americas, it is not limited to this continent and is found in countries in Africa and Asia, resulting in more than two million cases of infection and 445,000 deaths worldwide in 2016 [? ].

Notably, vector-borne disease transmission is closely related to environmental changes that interfere with the ecosystem of both transmitting organisms and affected organisms. In the case of the Amazon, agricultural and livestock settlements are among the factors that most favor disease transmission, both due to the deforestation they cause for establishment and the clustering of people in environments close to the vector's habitat [? ], especially by clustering non-immune migrants near these natural and artificial breeding sites [? ].

Additionally, other factors such as rainfall, wildfires, and mining also significantly influence disease transmission in the region. These events result in habitat loss, ecosystem fragmentation, and climate changes, affecting the distribution and abundance of vectors and hosts, as well as their interaction with pathogens. Furthermore, population growth

and urbanization also play a crucial role in disease spread, increasing human exposure to vectors and infection risks.

In this context, this work aims to investigate vector-borne disease transmission in the Amazon and analyze how environmental impacts influence the dynamics of malaria transmission, the ecological and socioeconomic factors affecting this spread, and possible prevention and control strategies. The main reference for this research is the Trajetórias Project, developed by the Center for Biodiversity and Ecosystem Services (SinBiose/CNPq), which is a dataset including environmental, epidemiological, economic, and socioeconomic indicators for all municipalities in the Legal Amazon, analyzing the spatial and temporal relationship between economic trajectories linked to the dynamics of agrarian systems, whether they are family-based rural or large-scale agricultural and livestock production, the availability of natural resources, and the risk of diseases [? ].

## 2. Model formulation


Based on previous work developed to model the transmission of malaria based on precipitation and temperature dynamics [? ], we focus on two different sets of compartments: susceptible hosts ( $S_H$ ), infected hosts ( $I_H$ ), recovered hosts ( $R_H$ ), susceptible vectors ( $S_M$ ), exposed vectors ( $E_M$ ) and infected vectors ( $I_M$ ). The equations that describe the transmission are given as:

$$\frac{dS_H}{dt} = -ab_2 \left( \frac{I_M}{N} \right) S_H \quad (1)$$

$$\frac{dI_H}{dt} = ab_2 \left( \frac{I_M}{N} \right) S_H - \gamma I_H \quad (2)$$

$$\frac{dR_H}{dt} = \gamma I_H \quad (3)$$

$$\frac{dS_M}{dt} = b - ab_1 \left( \frac{I_H}{N} \right) S_M - \mu S_M \quad (4)$$

 raphael.levy147@gmail.com (R.F. Levy);

flavio.codeco.coelho@fgv.br (F.C. Coelho)

ORCID(s):

$$\frac{dE_M}{dt} = ab_1 \left( \frac{I_H}{N} \right) S_M - \mu E_M - ab_1 \left( \frac{I_H}{N} \right) S_M l(\tau_M) \quad (5)$$

$$\frac{dI_M}{dt} = ab_1 \left( \frac{I_H}{N} \right) S_M l(\tau_M) - \mu I_M \quad (6)$$

The parameters are given in Table 1, while the variables are given in Table 2, which can be found in the Appendix. The selected human population was from the rural area of Manaus, between the years of 2004 to 2008, as this locality had the highest incidence of malaria caused by *P. vivax* in the Amazon region [? ]. This species of Plasmodium was chosen as it is responsible for the highest number of malaria cases in Brazil [? ? ]. With the incidence function [? ] we have that

$$\text{Inc}(d, m, z, t_1, t_2) = \frac{\text{Cases}(d, m, z, t_1, t_2)}{\text{Pop}(m, z, (t_1 + t_2)/2) \times 5 \text{ years}} \times 10^5, \quad (7)$$

where  $\text{Cases}(d, m, z, t_1, t_2)$  is the number of cases of disease  $d$  in zone  $z$  of municipality  $m$ , and  $t_1$  and  $t_2$  are the initial and final years of the interval, while  $\text{Pop}(m, z, (t_1 + t_2)/2) \times 5 \text{ years}$  is the population in zone  $z$  of municipality  $m$  in the middle of the period multiplied by the total number of observation years. In this case, we could indicate as:

$$\begin{aligned} \text{Inc}(\text{Vivax}, \text{Manaus}, \text{Rural}, 2004, 2008) &= \frac{\text{Cases}(\text{Vivax}, \text{Manaus}, \text{Rural}, 2004, 2008)}{\text{Pop}(\text{Manaus}, \text{Rural}, 2006) \times 5 \text{ years}} \times 10^5 \\ &= \frac{78745}{5 \times 184030.8} \times 10^5 \approx 8558 \end{aligned} \quad (8) \quad (9)$$

Using data on the total population of Manaus in this period, with an incidence of 3106.429047 and a number of cases of 262264, the total population of the municipality was estimated to be 1688524 inhabitants, which corresponds to the value found in the official census [? ]. Thus, the rural population could be considered as approximately 0.5% of the municipality's population.

Having estimated the percentage size of the rural population in the city, it was possible to calculate this population for each of the years of the analysis through linear interpolation using historical series data from IBGE [? ]:

Given there was only population data for the years of 2000, 2007, and 2010, interpolations were performed with different initial and final points, using data from 2000 to 2007 for 2004-2007 and from 2007 to 2010 for 2008-2009, ensuring the correct use of the 2007 population.

As for the theory behind environmental factors, according to [? ], the removal of tree canopies allowed the resurgence of malaria in South America. In deforested areas, without tree canopies covering the ground, water puddles under sunlight attract mosquitoes of the species *Anopheles darlingi*, the main vector related to human malaria in the Amazon [? ]. They are usually less commonly

found in still intact forests. This is because light and heat favor the development of larvae and pupae, in addition to a greater availability of algae for larval feeding [? ]. The increase in ambient temperature also favors the vectorial capacity of mosquitoes.

Deforestation also attracts and brings humans closer to take part in logging, agriculture, and road construction activities, bringing individuals infected with *Plasmodium* to an area where both the vector and the environment have already been modified to favor transmission. Furthermore, agriculture also promotes river sedimentation, providing suitable environments for breeding sites. Therefore, it can be considered a relevant change for the model to take into account deforestation, the increase in survival probabilities of eggs, larvae, and pupae, as well as increasing the proportion of bites that lead to infection, due to the increased human population density in areas near mosquito breeding sites.

### 3. Front matter

The author names and affiliations could be formatted in two ways:

- (1) Group the authors per affiliation.
- (2) Use footnotes to indicate the affiliations.

See the front matter of this document for examples. You are recommended to conform your choice to the journal you are submitting to.

### 4. Bibliography styles

There are various bibliography styles available. You can select the style of your choice in the preamble of this document. These styles are Elsevier styles based on standard styles like Harvard and Vancouver. Please use BibTeX to generate your bibliography and include DOIs whenever available.

Here are two sample references: [? ] [? ? ] [? ? ]

### 5. Floats

Figures may be included using the command, `\includegraphics` in combination with or without its several options to further control graphic. `\includegraphics` is provided by `graphic[s,x].sty` which is part of any standard L<sup>A</sup>T<sub>E</sub>X distribution. `graphicx.sty` is loaded by default. L<sup>A</sup>T<sub>E</sub>X accepts figures in the postscript format while pdfL<sup>A</sup>T<sub>E</sub>X accepts \*.pdf, \*.mps (metapost), \*.jpg and \*.png formats. pdfL<sup>A</sup>T<sub>E</sub>X does not accept graphic files in the postscript format.

The table environment is handy for marking up tabular material. If users want to use `multirow.sty`, `array.sty`, etc., to fine control/enhance the tables, they are welcome to load any package of their choice and `cas-dc.cls` will work in combination with all loaded packages.

### 6. Theorem and theorem like environments

`cas-dc.cls` provides a few shortcuts to format theorems and theorem-like environments with ease. In all commands



**Figure 1:** The beauty of Munnar, Kerala. (See also Table 1).

**Table 1**

This is a test caption. This is a test caption. This is a test caption. This is a test caption. Use `{table*}` instead of `{table}` if you want a two column spanned table.

Col 1	Col 2	Col 3	Col4
12345	12345	123	12345
12345	12345	123	12345
12345	12345	123	12345
12345	12345	123	12345
12345	12345	123	12345

the options that are used with the `\newtheorem` command will work exactly in the same manner. `cas-dc.cls` provides three commands to format theorem or theorem-like environments:

```
\newtheorem{theorem}{Theorem}
\newtheorem{lemma}[theorem]{Lemma}
\newdefinition{rmk}{Remark}
\newproof{pf}{Proof}
\newproof{pot}{Proof of Theorem \ref{thm2}}
```

The `\newtheorem` command formats a theorem in  $\text{\LaTeX}$ 's default style with italicized font, bold font for theorem heading and theorem number at the right hand side of the theorem heading. It also optionally accepts an argument which will be printed as an extra heading in parentheses.

```
\begin{theorem}
  For system (8), consensus can be achieved with
   $|T_{\omega} z| \leq \dots$ 
  \begin{eqnarray} \label{10}
    \dots
  \end{eqnarray}
\end{theorem}
```

**Theorem 1.** *For system (8), consensus can be achieved with  $\|T_{\omega} z\| \dots$*

$$\dots \quad (10)$$

The `\newdefinition` command is the same in all respects as its `\newtheorem` counterpart except that the font shape is roman instead of italic. Both `\newdefinition` and `\newtheorem` commands automatically define counters for the environments defined.

The `\newproof` command defines proof environments with upright font shape. No counters are defined.

## 7. Enumerated and Itemized Lists

`cas-dc.cls` provides an extended list processing macros which makes the usage a bit more user friendly than the default  $\text{\LaTeX}$  list macros. With an optional argument to the `\begin{enumerate}` command, you can change the list counter type and its attributes.

```
\begin{enumerate}[1.]
\item The enumerate environment starts with an optional
      argument `1.', so that the item counter will be suffixed
      by a period.
\item You can use `a)' for alphabetical counter and `(i)'
      for roman counter.
\begin{enumerate}[a)]
\item Another level of list with alphabetical counter.
\item One more item before we start another.
\item One more item before we start another.
\item One more item before we start another.
\item One more item before we start another.
```

Further, the enhanced list environment allows one to prefix a string like ‘step’ to all the item numbers.

```
\begin{enumerate}[Step 1.]
\item This is the first step of the example list.
\item Obviously this is the second step.
\item The final step to wind up this example.
\end{enumerate}
```

## 8. Cross-references

In electronic publications, articles may be internally hyperlinked. Hyperlinks are generated from proper cross-references in the article. For example, the words Fig. 1 will never be more than simple text, whereas the proper cross-reference `\ref{tiger}` may be turned into a hyperlink to the figure itself: Fig. 1. In the same way, the words Ref. [1] will fail to turn into a hyperlink; the proper cross-reference is `\cite{Knuth96}`. Cross-referencing is possible in  $\text{\LaTeX}$  for sections, subsections, formulae, figures, tables, and literature references.

## 9. Bibliography

Two bibliographic style files (\*.bst) are provided — `model1-num-names.bst` and `model2-names.bst` — the first one can be used for the numbered scheme. This can also be used for the numbered with new options of `natbib.sty`. The second one is for the author year scheme. When you use `model2-names.bst`, the citation commands will be like `\citep`, `\cit`, `\citealt` etc. However when you use `model1-num-names.bst`, you may use only `\cite` command.

the `bibliography` environment. Each reference is a `\bibitem` and each `\bibitem` is identified by a label, by which it can be cited in the text:

