

$$\begin{cases} \langle \cos^2(x) \rangle = \frac{1}{2\pi} \int_0^{2\pi} \cos^2(t) dt = \frac{1}{2} \\ \langle \sin^2(x) \rangle = \frac{1}{2\pi} \int_0^{2\pi} \sin^2(t) dt = \frac{1}{2} \end{cases}$$