$$dz = \frac{1}{2g} \frac{v_l^2}{v^2 - v_l^2} \, dv^2$$