



Fairwashing SHAP

or

Interventional and Observational Shapley Values





Motivation

Someone walks into a bank, applied for a loan, gets rejected.

Why?

2 Kinds of explanations:

Recourse: What could they do to get the loan?

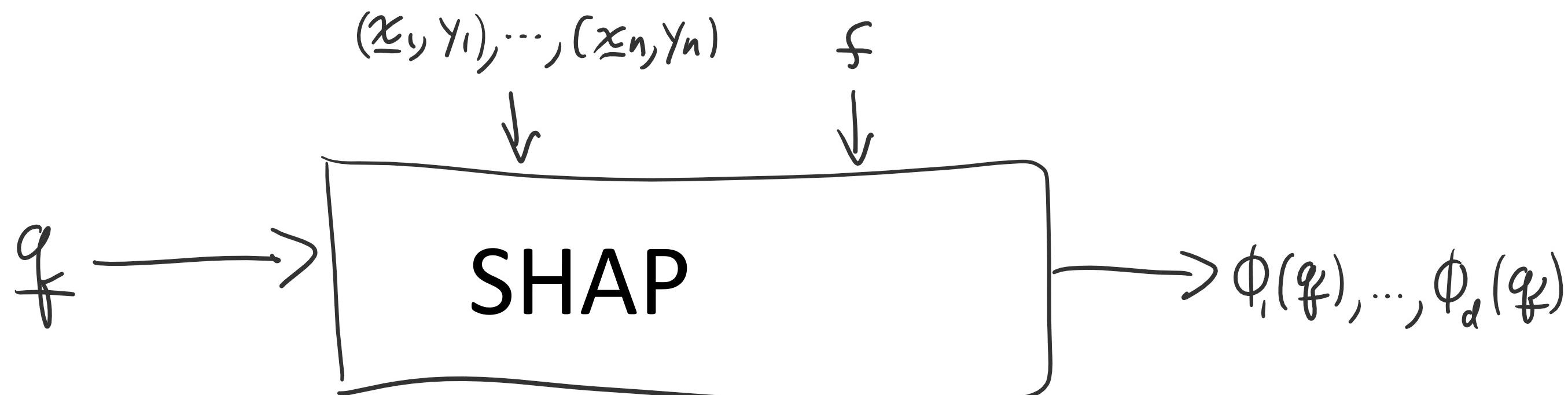
R\AI Developer: Why did the model say no? It is bigoted?
Focus on this

Local Feature Importance

Given: dataset $(\underline{x}_1, y_1), \dots, (\underline{x}_n, y_n) \stackrel{iid}{\sim} \mathcal{D}$, ML model $f(\underline{x})$, query point $\underline{q} \in \mathbb{R}^d$

vectors are underlined

Return: Importance of each feature $\phi_1(\underline{q}), \dots, \phi_d(\underline{q})$



Shap is well used, based on nice game theory -- good about proxy vars!



Fairwashing

Suppose f is very racist.

Then $SHAP(f, \mathbf{x})$ should show that race is an important feature

But, we can make ML model \tilde{f} such that

- ① For almost all \mathbf{x} , $\tilde{f}(\mathbf{x}) = f(\mathbf{x})$
- ② $SHAP(\tilde{f}, \mathbf{x})$ shows almost no importance for race

\tilde{f} is a "**Fairwashed**" version of f . It looks fair, but it ain't!

- At least 2 papers: Umang's paper, [Slack et al. 2020]
- But, how is this possible? What about game theory?



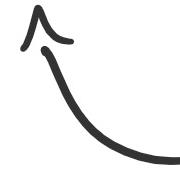
Takeaway

Q: How is fairwashing possible? What about game theory?

A: "Interventional" vs "Observational" Shapley Values



What SHAP and QII do
Bad for proxys



Other papers do this.
Good for proxys.

"True to the Model or True to the Data" (on arXiv)

↳ Great jumping off point, easy read



SHAPLEY VALUES



Some notation

- We have d features: $\underline{x}_1, \dots, \underline{x}_n, \underline{q} \in \mathbb{R}^d$

$$d = 5$$

$$\underline{q} = [9 \ 7 \ 5 \ 3 \ 1]$$

- Let $S \subseteq \{1, 2, 3, \dots, d\}$ be a subset of features

$$S = \{1, 2\}$$

- Let \bar{S} complement of S

$$\bar{S} = \{3, 4, 5\}$$

- Let $(\underline{q})_S$ = entries of \underline{q} indexed by S

$$(\underline{q})_S = [9 \ 7 \ 0 \ 0 \ 0]$$

$$(\underline{q})_{\bar{S}} = [0 \ 0 \ 5 \ 3 \ 1]$$

- Notice: $\underline{q} = (\underline{q})_S + (\underline{q})_{\bar{S}}$

Frankenstein Point: $(\underline{q})_S + (\underline{x}_j)_{\bar{S}}$

$$\underline{x}_1 = [2 \ 2 \ 2 \ 2 \ 2]$$

$$(\underline{q})_S + (\underline{x}_1)_{\bar{S}} = [9 \ 7 \ 2 \ 2 \ 2]$$

Shapley Values

Let $\mathcal{V}_s(\varphi)$ be the **Value** of φ with respect to S .

The average marginal contribution of feature i .

Not "Quantity of Interest"

$$\Phi_i(\varphi) := \underbrace{\sum_{\substack{S \subseteq \{1, \dots, d\} \\ i \notin S}} \frac{1}{d} \cdot \frac{1}{|S|}}_{\text{Average over } S} \underbrace{(\mathcal{V}_{S \cup \{i\}}(\varphi) - \mathcal{V}_S(\varphi))}_{\text{How much } i \text{ increases value, starting from } S}$$

① **Interventional** $\mathcal{V}_s(\varphi) = \mathbb{E}_{\underline{x} \sim p} [f((\varphi)_s + (\underline{x})_{\bar{s}})] \approx \frac{1}{n} \sum_{j=1}^n f((\varphi)_s + (\underline{x}_j)_{\bar{s}})$

- Used by SHAP (by default), QII
- Creates very fake-looking data points (ignores dependencies)



$$\textcircled{1} \text{ Interventional } V_s(q_f) = \mathbb{E}_{\underline{x} \sim p} [f((q_f)_s + (\underline{x})_{\bar{s}})] \approx \frac{1}{n} \sum_{j=1}^n f((q_f)_s + (\underline{x}_j)_{\bar{s}})$$

- Used by SHAP (by default), QII
- Creates very fake-looking data points (ignores dependencies)

$$\textcircled{2} \text{ Observational } V_s(q_f) = \mathbb{E}_{\underline{x} \sim D} [f((q_f)_s + (\underline{x})_{\bar{s}}) \mid (\underline{x})_s = (q_f)_s]$$

\approx Average of $((q_f)_s + (\underline{x}_j)_{\bar{s}})$ for all $(\underline{x}_j)_s = (q_f)_s$?

- Less used, but is used
- Creates real-looking data points
- Hard to compute (few points to average)

How can we compare these 2 approaches?



Simple Linear Model

Suppose $f(\mathbf{q}_f) = \langle \mathbf{w}, \mathbf{q}_f \rangle + \beta$ for some $\mathbf{w} \in \mathbb{R}^d$, $\beta \in \mathbb{R}$.

How do interventional & observational $\Phi_i(\mathbf{q})$ look?

Lemma

Interventionally,

$$\Phi_i(\mathbf{q}_f) = w_i (q_{f,i} - \bar{\mu}_i)$$

average of feature i

Takeaway: Completely ignores proxy variables



Takeaway: Completely ignores proxy variables

✓ $\underline{\chi} = (\text{Kindness}, \text{salary}, \text{age})$ where $\text{salary} = 1000 \cdot \text{age}$

$\underline{w}_{\text{BAD}} = [1, 0, 1000]$ is unfair: uses age a lot

$\phi_{AGE}(q) = 1000(q_i - \mu_i) \neq 0$, great!

$\underline{w}_{\text{WASHED}} = [1, 1, 0]$ makes exact same predictions

$\phi_{AGE}(q) = 0$, terrible!





Lemma Proof: $\phi_i(f) = w_i (f_i - \nu_i)$ interventionally

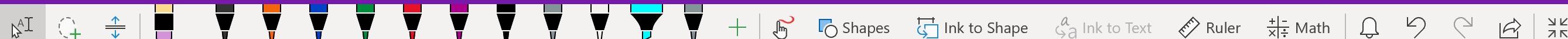
$$\mathcal{V}_s(f) = \frac{1}{n} \sum_{i=1}^n f((\underline{f})_s + (\underline{x_j})_{\bar{s}}) = \frac{1}{n} \sum_{i=1}^n \langle \underline{w}, (\underline{f})_s + (\underline{x_j})_{\bar{s} \setminus i} + (\underline{x_j})_{\bar{s} \setminus \{i\}} \rangle + \kappa$$

$$\downarrow \qquad \qquad \qquad \downarrow \qquad \qquad \qquad \downarrow$$

$$\mathcal{V}_{s \cup \{i\}}(f) = \frac{1}{n} \sum_{i=1}^n f((\underline{f})_{s \cup \{i\}} + (\underline{x_j})_{\bar{s} \setminus i}) = \frac{1}{n} \sum_{i=1}^n \langle \underline{w}, (\underline{f})_s + (\underline{f})_{\{i\}} + (\underline{x_j})_{\bar{s} \setminus \{i\}} \rangle + \kappa$$

$$\begin{aligned} \mathcal{V}_{s \cup \{i\}}(f) - \mathcal{V}_s(f) &= \frac{1}{n} \sum_{i=1}^n \langle \underline{w}, (\underline{f})_{\{i\}} - (\underline{x_j})_{\{i\}} \rangle \\ &= \langle \underline{w}, (\underline{f})_{\{i\}} - (\underline{\nu})_{\{i\}} \rangle \quad [0 \cdots 0(f_i - \nu_i) 0 \cdots 0] \\ &= w_i (f_i - \nu_i) \end{aligned}$$

$\phi_i(f) = \text{Average of } \mathcal{V}_{s \cup \{i\}}(f) - \mathcal{V}_s(f) \text{ across all } = w_i (f_i - \nu_i)$ ■



Beyond Intervensional Value

Above proof does not work for observation values

$$\mathcal{V}_s(\underline{q}) = \mathbb{E}_{\underline{x} \sim p} [f((\underline{q})_s + (\underline{x})_{\bar{s}}) \mid (\underline{x})_s = (\underline{q})_s]$$

Only Frankenstein \underline{q} with \underline{x}_j 's that match \underline{q} on S .
So,

$\mathcal{V}_{S \cup \{i\}}(\underline{q}) - \mathcal{V}_s(\underline{q})$ depends on s , breaking the proof.

Claim

If $f(\underline{q}) = \langle \underline{w}, \underline{q} \rangle + \beta$ and $\underline{x}_j \stackrel{iid}{\sim} \mathcal{N}(\underline{\mu}, \Sigma)$, then we can write $\phi_s(\underline{q})$ exactly (but it's ugly).

But it super depends on correlation in Σ !



Comparison

Let

$$\underline{x}_j \sim N\left(\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} 1 & 0.99 & 0 \\ 0.99 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}\right)$$

Features 2 and 3
are super correlated

$$\underline{w} = [1 \ 2 \ 3], \ q = [1 \ 1 \ 1]$$

Interventional

$$\phi_1(q) = 1$$

$$\begin{aligned} \phi_2(q) &= 2 \\ \phi_3(q) &= 3 \end{aligned}$$

Treated
Very
Different

Observational

$$\phi_1(q) = 1$$

$$\begin{aligned} \phi_2(q) &\approx 2.5 \\ \phi_3(q) &\approx 2.5 \end{aligned}$$

Treated
the
Same!



Interventional

$$\phi_1(q_f) = 1$$

$$\begin{aligned}\phi_2(q_f) &= 2 \\ \phi_3(q_f) &= 3\end{aligned}$$

Treated
Very
Different

If $w_2 = 0$,

Then $\phi_2(q_f) = 0$

Better recourse

IF

Feature are independent

Observational

$$\phi_1(q_f) = 1$$

$$\begin{aligned}\phi_2(q_f) &\approx 2.5 \\ \phi_3(q_f) &\approx 2.5\end{aligned}$$

Treated
the
Same!

If $w_2 = 0$

Then $\phi_2(q_f)$ may be $\neq 0$

If f is blind to age, it possible that $\phi_{AGE}(q_f) \neq 0!$

Better recourse in my opinion
because

Features are dependant



Conclusion

Going back to the bank example,

Both recourse and R\AI Engineering prefer observational values

But we use interventional almost always.
Also, it's harder to compute.