

**Algorithm 6.3** Forward propagation through a typical deep neural network and the computation of the cost function. The loss  $L(\hat{\mathbf{y}}, \mathbf{y})$  depends on the output  $\hat{\mathbf{y}}$  and on the target  $\mathbf{y}$  (see section 6.2.1.1 for examples of loss functions). To obtain the total cost  $J$ , the loss may be added to a regularizer  $\Omega(\theta)$ , where  $\theta$  contains all the parameters (weights and biases). Algorithm 6.4 shows how to compute gradients of  $J$  with respect to parameters  $\mathbf{W}$  and  $\mathbf{b}$ . For simplicity, this demonstration uses only a single input example  $\mathbf{x}$ . Practical applications should use a minibatch. See section 6.5.7 for a more realistic demonstration.

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**Require:** Network depth,  $l$

**Require:**  $\mathbf{W}^{(i)}, i \in \{1, \dots, l\}$ , the weight matrices of the model

**Require:**  $\mathbf{b}^{(i)}, i \in \{1, \dots, l\}$ , the bias parameters of the model

**Require:**  $\mathbf{x}$ , the input to process

**Require:**  $\mathbf{y}$ , the target output

$$\mathbf{h}^{(0)} = \mathbf{x}$$

**for**  $k = 1, \dots, l$  **do**

$$\mathbf{a}^{(k)} = \mathbf{b}^{(k)} + \mathbf{W}^{(k)} \mathbf{h}^{(k-1)}$$

$$\mathbf{h}^{(k)} = f(\mathbf{a}^{(k)})$$

**end for**

$$\hat{\mathbf{y}} = \mathbf{h}^{(l)}$$

$$J = L(\hat{\mathbf{y}}, \mathbf{y}) + \lambda \Omega(\theta)$$

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