

RNash_Assign13.rmd

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1

Write a program to compute the derivative of $f(x) = x^3 + 2x^2$ at any value of x . Your function should take in a value of x and return back an approximation to the derivative of $f(x)$ evaluated at that value. You should not use the analytical form of the derivative to compute it. Instead, you should compute this approximation using limits.

```
f <- function(x) {  
  (2*(x**2)) +x**3  
}  
  
derivative <- function(x, func) {  
  h <- .0000000001  
  (f(x+h) - f(x))/h  
}
```

```
g <- D(f(x) ~ x)
```

```
c(derivative(1, f), g(1))
```

```
## [1] 7.000001 7.000000
```

```
c(derivative(2,f),g(2))
```

```
## [1] 20 20
```

2

Now, write a program to compute the area under the curve for the function $3x^2 + 4x$ in the range $x = [1; 3]$. You should first split the range into many small intervals using some really small Δx value (say $1e-6$) and then compute the approximation to the area under the curve.

```
j <- function (x) {  
  3*(x**2)+4*x  
}  
  
reimann <- function(x_1, x_2, func) {  
  delta<- 10**-6  
  s <- seq(from=x_1, to=x_2, by = delta )  
  
  area_under_curve <- 0  
  
  for (x in 1:(length(s)-1)) {  
  
    area_under_curve <- (func(s[x]) *delta) + area_under_curve
```

```
}  
  
  return (area_under_curve)  
}
```

```
reimann(1,3,j)
```

```
## [1] 41.99998
```

```
J <- antiD(j(t) ~ t)  
J(3)-J(1)
```

```
## [1] 42
```

Images of analytical problems

$$\int \sin(x) \cos(x) dx$$

$$f(x) = \cos(x)$$

$$f'(x) = -\sin(x)$$

$$g(x) = \sin(x)$$

$$g'(x) = \cos(x)$$

$$\int f g' dx = fg - \int f' g dx$$

$$\cos(x) \sin(x) - \int -\sin(x) \sin(x) dx$$

$$\cos(x) \sin(x) + \int \sin(x) \sin(x) dx$$

$$\cos(x) \sin(x) + \int \frac{1}{2} [1 - \cos(2x)] dx$$

$$\cos(x) \sin(x) + \frac{1}{2} \int 1 - \cos(2x) dx$$

$$\cos(x) \sin(x) + \frac{1}{2} \left(\int 1 dx - \int \cos(2x) dx \right)$$

$$\cos(x) \sin(x) + \frac{1}{2} \left(x - \int \cos(2x) dx \right)$$

$$\cos(x) \sin(x) + \left(\frac{1}{2} x + \frac{1}{2} \sin(2x) \right) + C$$

Figure 1:

$$\begin{aligned}
 & \int x^2 e^x dx \\
 & \int f g' dx = f g - \int f' g dx \\
 & x^2 \cdot e^x - \int 2x e^x dx \\
 & x^2 \cdot e^x - 2 \int x e^x dx \\
 & x^2 \cdot e^x - 2(x e^x - \int 1 \cdot e^x dx) \\
 & x^2 \cdot e^x - 2(x e^x - e^x) + C \\
 & x^2 e^x - 2x e^x + e^x + C
 \end{aligned}$$

$f(x) = x^2$
 $f'(x) = 2x$
 $g(x) = e^x$
 $g'(x) = e^x$

$f(x) = x$
 $f'(x) = 1$
 $g(x) = e^x$
 $g'(x) = e^x$

Figure 2:

$$\begin{aligned}
 & x \cos(x) dx \\
 & f'(x) g(x) + f(x) g'(x) \\
 & \quad \quad \quad \cos(x) + x (-\sin(x)) \\
 & \cos(x) + x (-\sin(x))
 \end{aligned}$$

Figure 3:

$$\begin{aligned}
 & (e^{x^4}) dx & F'(x) &= f'(g(x)) \cdot g'(x) \\
 & & F(x) &= e^{x^4} \\
 & f(x) = e^x & f'(x) &= e^x \\
 & g(x) = x^4 & g'(x) &= 4x^3 \\
 & e^{g(x)} \cdot 4x^3 & &= \boxed{e^{x^4} \cdot 4x^3}
 \end{aligned}$$

Figure 4: