

Gradient descent

Puteaux, Fall/Winter 2020-2021

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##                               ##  
##  Deep Learning in Python  ##  
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```

§1 Introduction to Deep Learning in Python

§1.2 Optimizing a neural network with backward propagation

§1.2.2 Gradient descent

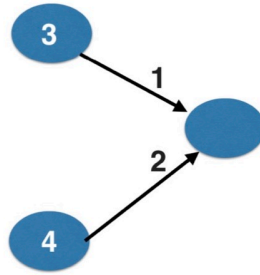
1. How does gradient descent work?

- If the slope is positive:
 - going opposite the slope means moving to lower numbers
 - subtract the slope from the current value
 - too big a step might lead astray
- The solution to avoid leading astray is using the learning rate:
 - update each weight by subtracting $learning\ rate \times slope$

2. What are the steps of the slope calculation?

- To calculate the slope for a weight, need to multiply:
 - the slope of the loss function with respect to value at the node which fed into
 - * e.g., *the slope of the mean-squared loss function*, in this case,
$$2 \cdot (Predicted\ Value - Actual\ Value) = 2 \cdot Error$$
 - the value of the node that feeds into the weight
 - the slope of the activation function with respect to the value fed into

3. Code of the slope calculation and weights updating:



```
[1]: import numpy as np

weights = np.array([1, 2])
input_data = np.array([3, 4])
target = 6
learning_rate = 0.01

preds = (weights * input_data).sum()
error = preds - target
print(error)
```

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```
[2]: gradient = 2 * input_data * error
      gradient
```

```
[2]: array([30, 40])
```

```
[3]: weights_updated = weights - learning_rate * gradient

preds_updated = (weights_updated * input_data).sum()
error_updated = preds_updated - target
print(error_updated)
```

2.5

4. Practice exercises for gradient descent:

► Package pre-loading:

```
[4]: import numpy as np
```

► Data pre-loading:

```
[5]: input_data = np.array([1, 2, 3])

weights = np.array([0, 2, 1])

target = 0
```

► The slope calculation practice:

```
[6]: # Calculate the predictions: preds
preds = (weights * input_data).sum()

# Calculate the error: error
error = preds - target

# Calculate the slope: slope
slope = 2 * error * input_data

# Print the slope
print(slope)
```

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► The model weights improving practice:

```
[7]: # Set the learning rate: learning_rate
learning_rate = 0.01

# Calculate the predictions: preds
preds = (weights * input_data).sum()

# Calculate the error: error
error = preds - target

# Calculate the slope: slope
slope = 2 * input_data * error

# Update the weights: weights_updated
weights_updated = weights - learning_rate * slope

# Get updated predictions: preds_updated
preds_updated = (weights_updated * input_data).sum()

# Calculate updated error: error_updated
error_updated = preds_updated - target

# Print the original error
print(error)

# Print the updated error
print(error_updated)
```

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5.04

► Package re-pre-loading:

```
[8]: import matplotlib.pyplot as plt
```

► Code pre-loading:

```
[9]: def get_error(input_data, target, weights):
    preds = (weights * input_data).sum()
    error = preds - target
    return (error)

def get_slope(input_data, target, weights):
    error = get_error(input_data, target, weights)
    slope = 2 * input_data * error
    return (slope)

def get_mse(input_data, target, weights):
    errors = get_error(input_data, target, weights)
    mse = np.mean(errors**2)
    return (mse)
```

► Weights multiple updates practice:

```
[10]: n_updates = 20
mse_hist = []

# Iterate over the number of updates
for i in range(n_updates):
    # Calculate the slope: slope
    slope = get_slope(input_data, target, weights)

    # Update the weights: weights
    weights = weights - 0.01 * slope

    # Calculate mse with new weights: mse
    mse = get_mse(input_data, target, weights)

    # Append the mse to mse_hist
    mse_hist.append(mse)

# Plot the mse history
plt.plot(mse_hist)
plt.xlabel('Iterations')
plt.ylabel('Mean Squared Error')
plt.show()
```

