



1.

	Unsigned	Signed	Unsigned Fixed Point	Signed Fixed Point
10000000	128	-128	$32 + 0/4 = 32$	$-32 + 0/4 = -32$
10000011	131	-125	$32 + \frac{3}{4} = \frac{(128+3)}{4} = 131/4$	$-31 - \frac{1}{4} = \frac{(-124-1)}{4} = -125/4$
10000001	129	-127	$32 + \frac{1}{4} = \frac{(128+1)}{4} = 129/4$	$-31 - \frac{3}{4} = -127/4$
01000001	65	+65	$16 + \frac{1}{4} = \frac{(64+1)}{4} = 65/4$	$16 + \frac{1}{4} = +65/4$
01111111	127	+127	$31 + \frac{3}{4} = \frac{(124+3)}{4} = 127/4$	$31 + \frac{3}{4} = +127/4$
11111111	255	-1	$63 + \frac{3}{4} = \frac{(252+3)}{4} = 255/4$	$-1 + \frac{3}{4} = -1/4$
11111100	252	-4	$63 + 0/4 = 63$	$-1 + 0/4 = -1$
00000000	0	+0	$0 + 0 = 0$	$+0 + 0 = +0$
01111110	126	+126	$31 + \frac{1}{2} = \frac{(62+1)}{2} = 63/2$	$+31 + \frac{1}{2} = +63/2$
10001110	142	-114	$35 + \frac{1}{2} = \frac{(70+1)}{2} = 71/2$	$-28 - \frac{1}{2} = \frac{(-56-1)}{2} = -57/2$
00010011	19	+19	$4 + \frac{3}{4} = \frac{(16+3)}{4} = 19/4$	$4 + \frac{3}{4} = +19/4$

1. NONE. Given 16 bits of representation, minus 6 bits for the fractional part, leaves us with 10 bits for the integer part, but since it's signed, the integer range is  $-2^9$  to  $+2^9 - 1$ .  $-2^9 = -512$ , but since all of the answers are less than -512, none are correct.

2.

	0x0.E	0000.1110	14/16
	-		
	0x0.F	0000.1111	-15/16
	$\sim(0x0.F) + .1 = 0xF.0 + .1$ $= 0xF.1$ $0x0.E$ $+ 0xF.1 = 0xF.F$	$-00001111 =$ $\sim(00001111) + 1 =$ $11110000 + 1 =$ $11110001$  $0000.1110 + 1111.0001 =$ $1111.1111$	
Result	0xF.F	0b1111 1111	-1/16

3.

-127.75 requires two bits to represent the fractional part, and 8 to represent the integer part. To prove this, if we take 127.75 represented in binary: 0111 1111.11 and negate it by inverting and adding 1:  $\sim(01111111.11) + 1$  we get 1000,0000.01, which has  $8 + 2 = 10$  bits, so it takes 10 bits:

1) 1000000001

2) 10 bits

4. 1000 0000.01  $\ll 4 = 100000000100$ .4.1.  $\sim 100000000100 + 1 = 01111111011 + 1 = 01111111100 = -1020$