

# Dynamic Priority Scheduling

## Real-Time Operative Systems Course

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October 24, 2022



- 1 Preliminaries
- 2 Online scheduling with dynamic priorities
- 3 Analysis: CPU utilization bound
- 4 Analysis: CPU Load Analysis
- 5 Other deadline assignment criteria

# Last lecture

## Fixed-priority online scheduling

- Rate-Monotonic scheduling
- Deadline-Monotonic and arbitrary priorities
- Analysis:
  - The CPU utilization bound
  - Worst-Case Response-Time analysis



# Agenda for today

- Online scheduling with dynamic priorities
  - Earliest Deadline First scheduling
  - Analysis: CPU utilization bound and CPU Load Analysis
- Optimality and comparison with RM
  - Schedulability level, number of preemptions, jitter and response time
- Other dynamic priority criteria
  - Least Slack First, First Come First Served

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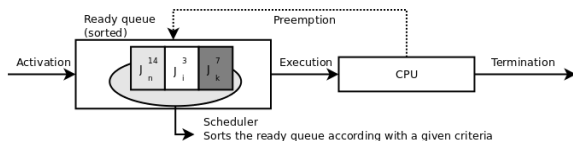
# On-line scheduling with dynamic priorities

## Dynamic priorities

**Ready Queue** sorted by instantaneous priorities and dynamically re-sorted (if/when necessary)

- Scheduling is based in dynamic criteria, i.e. one that is known only at run-time
- The dynamic parameter used to sort the ready tasks can be understood as a dynamic priority
- The ready queue is (re)sorted according with decreasing priorities whenever there is a priority change. Executes first the task that has the greater instantaneous priority
  - Complexity  $O(n \cdot \log(n))$

maior comple



# On-line scheduling with dynamic priorities

## Pros

- Scales well (wrt SCS)
  - Changes made to the task set are immediately seen by the scheduler
- Accommodates easily sporadic tasks (wrt SCS)
- Allows higher utilization levels than Fixed Priorities

## Cons

- More complex implementation (wrt SCS and FP)
- Higher overhead (wrt SCS and FP) > complexidade => overhead
  - Re-sorting of ready queue; depends on the algorithm
- “Unpredictability” on overloads (wrt FP)
  - It is not possible to know a priori which tasks will fail deadlines

# On-line scheduling with dynamic priorities

## Priority allocation approaches

- Inversely proportional to the time to the deadline
  - EDF – Earliest Deadline First deadline absoluta
    - Optimal among all dynamic priority criteria
- Inversely proportional to the laxity or slack dar prioridade a
  - LSF (LST or LLF) – Least Slack First
    - Optimal among all dynamic priority criteria
- Inversely proportional to the service waiting time
  - FCFS –First Come First Served
    - Not optimal with respect to meet deadlines; extremely poor real-time performance
- etc.



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# On-line scheduling with dynamic priorities

## Schedulability tests

- Since the schedule is built online it is important to determine a priori if a given task set meets or not its temporal requirements
- There are three types of schedulability tests:
  - Based on CPU utilization
  - Based on CPU load (processor demand)
  - Based on response time

# EDF Scheduling

EDF tests based on CPU utilization (n independent tasks, with full preemption)

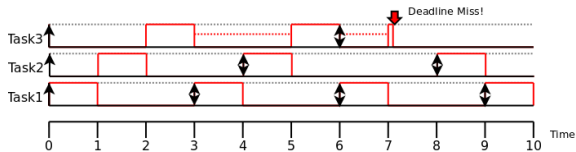
- $D = T$ 
  - $U(n) = \sum_{i=1}^n (\frac{C_i}{T_i}) \leq 1 \Leftrightarrow$  Task set is schedulable
  - Allows using 100% of CPU with timeliness guarantees
- $D < T$ 
  - $U(n) = \sum_{i=1}^n (\frac{C_i}{D_i}) \leq 1 \Rightarrow$  Task set is schedulable
  - Sufficient condition, only.
  - Pessimistic test (as for RM, inflates the utilization)

vantagem d

# RM Scheduling - example

rate monotonic como na aula passada - prioridades fixas

$\tau$	C	T
1	1	3
2	1	4
3	2.1	6



- $U = \frac{1}{3} + \frac{1}{4} + \frac{2.1}{6} = 0.93 > 0.78 \Rightarrow 1$  activation per period NOT guaranteed.
- In fact  $\tau_3$  fails a deadline!

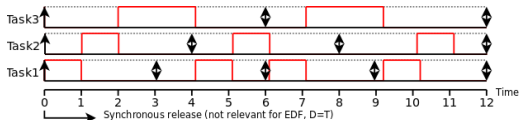
## EDF Scheduling – same example

prioridades dinamicas

caso haja empate tanto fazse a

Same example as before!

$\tau$	C	T
1	1	3
2	1	4
3	2.1	6

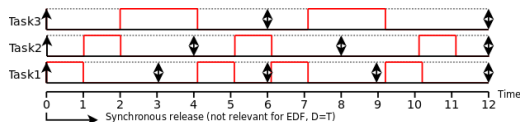


- $U = \frac{1}{3} + \frac{1}{4} + \frac{2.1}{6} = 0.93 \leq 1 \Leftrightarrow$  one activation per period IS guaranteed.

# EDF Scheduling – same example

Same example as before!

$\tau$	C	T
1	1	3
2	1	4
3	2.1	6



## Note:

- No deadline misses
- Less preemptions
- Higher jitter on quicker tasks
- The worst-case response time does not coincide necessarily with the synchronous release

# EDF Scheduling

Notion of **fairness** nao existe sistemas mais importantes que outras as

- Be fair on the attribution of resources (e.g. CPU)
- EDF is intrinsically fairer than RM, in the sense that tasks see its relative deadline increased as the absolute deadline approaches, independently of its period or any other static parameter.
- Consequences:
  - Deadlines are easier to met
  - As the deadline approaches preemptions suffered by a given task are reduced
  - The slack of tasks that are quick but have large deadlines can be used by other task (higher jitter on tasks with shorter periods)

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# CPU Load Analysis

- For  $D < T$ , the biggest period during which the CPU is permanently used (i.e. without interruption, idle time) corresponds to the scenario in which all tasks are activated synchronously. This period is called **synchronous busy period** and has duration  $L$
- $L$  can be computed by the following iterative method, which returns the first instant since the synchronous activation in which the CPU completes all the submitted jobs

## Computation of $L$

$$L(0) = \sum_i (C_i)$$

$$L(m+1) = \sum_i (\lceil \frac{L(m)}{T_i} \rceil \cdot C_i)$$

Stop condition:  $L(m+1) = L(m)$

# CPU Load Analysis

- Knowing  $L$ , we have to guarantee the **Load Condition**, i.e.

$$h(t) \leq t, \forall t \in [0, L[ \Rightarrow \textit{Task set is schedulable}$$

- The Load Condition refers to all the work that must be **completed by  $t$** .
- How to compute  $h(t)$ ?
- Example:
  - Task set  $\Gamma = \{(2, 4), (2, 8), (3, 16)\}$
- Draw the Gantt chart and mark the points where tasks must complete
- Write a suitable equation

# CPU Load Analysis

Knowing  $L$  we have to guarantee the load condition, i.e.

$$h(t) \leq t, \forall t \in [0, L[$$

And  $h(t)$  can be computed as follows:

$$h(t) = \sum_{i=1..N} \max(0, 1 + \lfloor \frac{t - D_i}{T_i} \rfloor) \cdot C_i$$

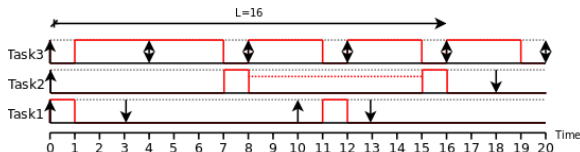
- The computation of  $h(t)$  for all values of  $t \in [0, L[$  is unfeasible.
  - However it is enough computing the load condition for the instants in which the load function varies, i.e.

$$S = \bigcup_i (S_i), S_i = \{m \cdot T_i + D_i\}, m = 0, 1, \dots$$

- Note: there are other, possibly shorter, values for  $L$

# EDF Scheduling

$\tau$	C	D	T
1	1	3	10
2	2	18	20
3	3	4	4



- $\sum_{i=1..N} \frac{C_i}{D_i} = \frac{1}{3} + \frac{2}{18} + \frac{3}{4} = 1.194 > 1 \Rightarrow$  Schedulability not guaranteed
- But the CPU load analysis indicates that the task set is schedulable!

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# LSF Scheduling

**Least Slack First** : Executes first the task with smaller slack  
 $(L_i(t) = d_i - c_i(t))$

LSF vs EDF short comparison

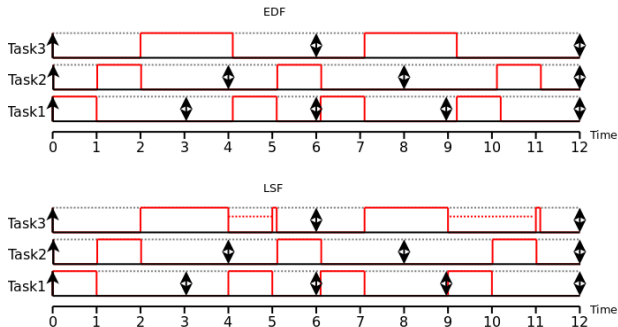
Vao estar sempre a entrar e a sair tarefas mu

- LS is optimal (as EDF)
- As the slack  $\uparrow$  the priority  $\downarrow$
- Priority of ready tasks increases as time goes by
  - Rescheduling only on instants where there are activations or terminations. **Why?**
- Priority of the task in the running state does not change
  - In EDF the priorities of all tasks (ready and executing) increase equally as time goes by
- Causes an higher number of preemptions than EDF (and thus higher overhead)
- No significant advantages with respect to EDF!

# LSF scheduling example

## LSF vs EDF

$\tau$	C	T
1	1	3
2	1	4
3	2.1	6



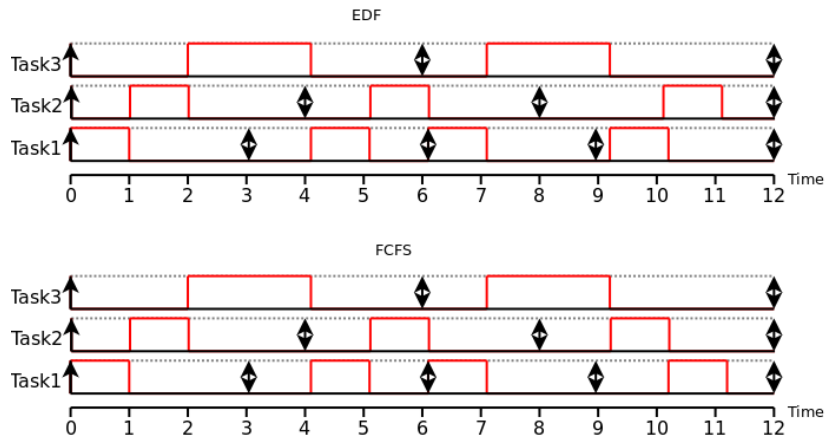
# FCFS Scheduling

Execute tasks as they arrive. Priority depends on the arrival order.  
A brief comparison between FCFS and EDF/LLF

- Non optimal
  - May lead to deadline misses even with very low CPU utilization rates
- Job age  $\uparrow$  Priority  $\uparrow$
- Priority of the ready and running tasks increases as time goes by (as in EDF)
- New jobs always get the lower priority
- There are no preemptions (smaller overhead and facilitates the implementation)
- Very poor temporal behavior!



# FCFS – same example



- When the “age” is the same the tie break criteria is decisive!

# Summary

- On-line scheduling with dynamic priorities
- The EDF - Earliest Deadline First criteria: CPU utilization bound and CPU Load Analysis
- Optimality of EDF and comparison with RM:
  - Schedulability level, number of preemptions, jitter and response time
- Other dynamic priority criteria:
  - LLF (LST) - Least Laxity (Slack) First
  - FCFS - First Come First Served