

```

231
232
233
234
235
236
237
238
239
240
241
242
243
244
245
246
247
248
249
250
251
252
253
254
255
256

```

```

    /// <summary>
    /// Bellman-Ford algorithm to find the shortest path from a source vertex to
    /// all other vertices in the graph and detect negative weight cycles that
    /// are reachable from the source
    /// </summary>
    /// <param name="s">the source vertex</param>
    /// <returns>Tuple containing 3 elements:
    ///     - a vector of distances from the source to each vertex
    ///     - a vector of predecessors for each vertex which helps to recreate the path
    ///     - a boolean indicating whether a negative cycle was detected
    /// </returns>
    std::tuple<std::vector<int>, std::vector<int>, bool> bellman_ford(int s)
    {
        // vector to hold the shortest distances from the source to all vertices
        // vertices are initialized with infinity(2e9) except for the source vertex
        // which is initialized with a distance of 0
        std::vector<int> distance(get_nr_of_vertices(), 2e9);
        distance[s] = 0;

        // vector to hold the predecessor for each vertex which helps us to
        // recreate the shortest path, because it tells us the previous vertex
        // of current one
        // It is initialized with -1 because, initially, we don't know the predecessor
        std::vector<int> predecessor(get_nr_of_vertices(), -1);

```

```

256
257 // Relaxing the edges
258 // Iterate V - 1 times where V is the number of vertices
259 // Since the shortest path in a graph with V vertices can have at most V - 1 edges
260 for (int k = 1; k <= get_nr_of_vertices() - 1; ++k)
261 {
262     for (auto p : get_edges())
263         // Check every edge in the graph to see if the distance to the vertex
264         // at the end of the edge can be improved by going through the vertex
265         // at the start of the edge
266         if (distance[p.second] > distance[p.first] + get_cost(p.first, p.second))
267         {
268             distance[p.second] = distance[p.first] + get_cost(p.first, p.second);
269             predecessor[p.second] = p.first;
270         }
271     }
272
273 // Check for negative weight cycles
274 // One more pass over all the edges to check for negative weight cycles
275 for (auto p : get_edges())
276     // If a negative cycle is detected, return True indicating the cycle's presence
277     if (distance[p.second] > distance[p.first] + get_cost(p.first, p.second))
278         return std::make_tuple(distance, predecessor, true);
279
280 // Return the distances, the predecessor for each vertex and False
281 // because there is no cycle
282 return std::make_tuple(distance, predecessor, false);
283

```