



Implement principal component analysis from scratch, that can be used with either eigen decomposition and singular value decomposition.

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Implementing Principal Component Analysis (PCA) from scratch involves a few steps, and it can be implemented using either Eigen Decomposition or Singular Value Decomposition (SVD). I'll guide you through both methods.

## 1. Standardize the Data

First, we standardize the dataset. Standardization involves subtracting the mean and dividing by the standard deviation for each feature.

## 2. Computing the Covariance Matrix (for Eigen Decomposition)

The next step is to compute the covariance matrix, which is used in the eigen decomposition method.

## 3. Eigen Decomposition Method

- Calculate the eigenvalues and eigenvectors of the covariance matrix.
- Sort the eigenvectors by decreasing eigenvalues and choose the top  $kk$  eigenvectors.

## 4. Singular Value Decomposition (SVD) Method

Alternatively, PCA can be performed using SVD:

- Compute the SVD of the data matrix.
- The principal components are given by the first  $kk$  right singular vectors.

## 5. Project Data onto Principal Components

Finally, project the data onto the selected principal components.

Here's the implementation in Python:

```
python
import numpy as np

def standardize_data(X):
    return (X - np.mean(X, axis=0)) / np.std(X, axis=0)

def pca_eigen(X, num_components):
    # Standardize the data
    X_std = standardize_data(X)
    # Covariance matrix
    covariance_matrix = np.cov(X_std.T)
```

```

# Eigen decomposition
eigenvalues, eigenvectors = np.linalg.eig(covariance_matrix)
# Sort eigenvectors by eigenvalues in descending order
idx = eigenvalues.argsort()[::-1]
eigenvalues = eigenvalues[idx]
eigenvectors = eigenvectors[:,idx]
# Select top num_components eigenvectors
eigenvectors = eigenvectors[:, :num_components]
return X_std.dot(eigenvectors)

def pca_svd(X, num_components):
    # Standardize the data
    X_std = standardize_data(X)
    # Compute SVD
    U, S, Vt = np.linalg.svd(X_std)
    # Select top num_components eigenvectors (right singular vectors)
    V = Vt.T
    return X_std.dot(V[:, :num_components])

# Example usage
X = np.array([[1, 2], [3, 4], [5, 6]]) # Replace with your dataset
num_components = 1 # Number of components you want to keep

# Using Eigen Decomposition
pca_eigen_results = pca_eigen(X, num_components)

# Using SVD
pca_svd_results = pca_svd(X, num_components)

```

Replace X with your dataset and num\_components with the number of principal components you wish to keep. This code will give you the PCA transformed data using both methods.

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