

Chi-Square Test

"Which pet do you prefer?" Using Chi-Square Test. Significance 5%=0.05

	Cat	Dog
Men	207	282
Women	231	242

The two **hypotheses** are.

- Gender and preference for cats or dogs are **independent**.
- Gender and preference for cats or dogs are **not independent**.

By doing the calculations (shown later), we come up with:

Add up rows and columns:

	Cat	Dog	
Men	207	282	489
Women	231	242	473
	438	524	962

Calculate "**Expected Value**" for each entry:

Multiply each row total by each column total and divide by the overall total:

	Cat	Dog	
Men	$\frac{489 \times 438}{962}$	$\frac{489 \times 524}{962}$	489
Women	$\frac{473 \times 438}{962}$	$\frac{473 \times 524}{962}$	473
	438	524	962

Which gives us:

	Cat	Dog	
Men	222.64	266.36	489
Women	215.36	257.64	473
	438	524	962

Subtract expected from observed, square it, then divide by expected:

In other words, use formula $(O-E)^2/E$ where

- O = **Observed** (actual) value
- E = **Expected** value

	Cat	Dog	
Men	$\frac{(207 - 222.64)^2}{222.64}$	$\frac{(282 - 266.36)^2}{266.36}$	489
Women	$\frac{(231 - 215.36)^2}{215.36}$	$\frac{(242 - 257.64)^2}{257.64}$	473
	438	524	962

Which gets us:

	Cat	Dog	
Men	1.099	0.918	489
Women	1.136	0.949	473
	438	524	962

Now add up those calculated values:

$$1.099 + 0.918 + 1.136 + 0.949 = 4.102$$

Chi-Square is 4.102

Degrees of Freedom(DF):

First we need a "Degree of Freedom"

$$\text{Degree of Freedom} = (\text{rows} - 1) \times (\text{columns} - 1)$$

For our example we have 2 rows and 2 columns:

$$\text{DF} = (3 - 1) \times (2 - 1) = 1 \times 1 = 2$$