

1. Kolmogorov- Smirnov (KS) Test

Step-1: Define the hypothesis for uniformity.

$$H_0 = R_i \sim U(0,1) \quad [R_i = \text{Random}]$$

$$H_1 = R_i \not\sim U(0,1)$$

Step-2: Arrange data in increasing order.

$$R_i = i^{\text{th}} \text{ smallest integer}$$

$$R_1 \leq R_2 \leq \dots \leq R_n$$

Step-3: Compute D^+ and D^-

$$D^+ = \max \{(i/N) - R_i\}; 1 \leq i \leq N$$

$$D^- = \max \{(R_i - (i-1)/N)\}; 1 \leq i \leq N$$

$D^+ = \text{Max KS test Parameter}$

$D^- = \text{Min KS test Parameter}$

Step-4: Compute $D = \max (D^+, D^-)$

Step-5: Determine the critical value D_α for specified α

Step-6: If $D > D_\alpha \rightarrow H_0$ is rejected means no's are not uniform.