

0.12, 0.01, 0.23, 0.28, 0.89, 0.31, 0.64, 0.28, 0.83, 0.93, 0.99, 0.15, 0.33, 0.35, 0.91, 0.41, 0.60, 0.27, 0.75, 0.88, 0.68, 0.49, 0.05, 0.43, 0.95, 0.58, 0.19, 0.36, 0.69, 0.87. ( $\alpha=0.025$ , Test No=3 at position 3<sup>rd</sup>, 8<sup>th</sup>, 13<sup>th</sup> are auto correlated)  $N=30$

**S1:** Define Hypothesis,

**S2:**  $i=3$ , lag/gap  $m=5$

**S3:** Find  $M$ ,  $i+(M+1)m \leq N$

$$3+(M+1)5 \leq 30$$

$$\rightarrow (M+1)5 \leq 27$$

$$\rightarrow (M+1) \leq 5.4$$

$$\rightarrow M \leq 4.4 \text{ [So, } M = \max(4, 3, 2 \dots 0)]$$

**M= 4**

$$\mathbf{S4:} \hat{\rho}_{im} = \frac{1}{M+1} \cdot \left[ \sum_{k=0}^M R_{i+km} \cdot R_{i+[k+1]m} \right] - 0.25$$

$$\hat{\rho}_{35} = \frac{1}{4+1} \left[ \sum_{k=0}^4 R_{3+5k} \cdot R_{3+5[k+1]} \right] - 0.25$$

$$= \frac{1}{5} [R_3 \cdot R_8 + R_8 \cdot R_{13} + R_{13} \cdot R_{18} + R_{18} \cdot R_{23} + R_{23} \cdot R_{28}] - 0.25$$

$$= \frac{1}{5} [0.23 \cdot 0.28 + 0.28 \cdot 0.33 + 0.33 \cdot 0.27 + 0.27 \cdot 0.05 + 0.05 \cdot 0.36]$$

$$= \frac{1}{5} (0.2774) - 0.25$$

$$= 0.05548 - 0.25$$

$$= -0.19452, \text{ This is the estimator}$$

$$\mathbf{S5:} \sigma_{\hat{\rho}_m} = \frac{\sqrt{13(4)+7}}{12(4+1)} = \frac{\sqrt{52+7}}{60} = 0.128$$

$$\mathbf{S6:} Z_0 = \frac{\hat{\rho}_{im}}{\sigma_{\hat{\rho}_m}} = \frac{-0.19452}{0.128} = \mathbf{-1.51}$$

**S7:**  $Z_{0.025} = 1.96$

**S8:**  $-Z_{\alpha/2} \leq Z_0 \leq +Z_{\alpha/2}$

$-1.96 \leq -1.51 \leq 1.96$ ,  $H_0$  is accepted.