## **Auto-Correlation Test (Example)**

0.19, 0.16, 0.82, 0.63, 0.04, 0.16, 0.30, 0.22, 0.88, 0.48, 0.29, 0.56, 0.44, 0.05, 0.81, 0.38, 0.59, 0.37, 0.71, 0.43, 0.92, 0.45, 0.57, 0.99, 0.20, 0.14, 0.64, 0.50, 0.73, 0.15, 0.02, 0.49, 0.86, 0.24, 0.90, 0.74, 0.41, 0.09, 0.80, 0.42. ( $\alpha$ =0.025, Test No=3 at position 2<sup>nd</sup>, 7<sup>th</sup>, 12<sup>th</sup> are auto correlated) N=40

S1: Define Hypothesis,

**S2:** i=2, lag m=5

S3: Find M,  $i+(M+1)m \le N$ 

$$2+(M+1)5 \le 40$$

$$\rightarrow$$
 (M+1)5 <= 38

$$\rightarrow$$
 (M+1) <= 7.6

$$\rightarrow$$
 M <= 6.6 [So, M= max (6,5, 4...0)]

M=6

**S4:** 
$$\hat{\mathbf{\rho}}_{im} = \frac{1}{M+1}$$
,  $\left[\sum_{k=0}^{M} R_{i+k_m} . R_{i+[k+1]m}\right] - 0.25$ 

$$\hat{\mathbf{p}}_{25} = \frac{1}{6+1} \left[ \sum_{k=0}^{6} R_{2+5k} . R_{2+5[k+1]} \right] - 0.25$$

$$= \frac{1}{7} \left[ R_2. \ R_7 + R_7. \ R_{12} + R_{12}. \ R_{17} + R_{17}. \ R_{22} + R_{22}. \ R_{27} + R_{27}. \ R_{32} + R_{32}. \ R_{37} \right] - 0.25$$

$$= \frac{1}{7} [0.16*0.30 + 0.30*0.56 + 0.56*0.59 + 0.59*0.45 + 0.45*0.64 + 0.64*0.49 + 0.49*0.41]$$

$$=\frac{1}{7}(1.6144)-0.25$$

$$= 0.23063 - 0.25$$

= -0.0193, This is the estimator

**S5:** 
$$\sigma_{\widehat{p}_m} = \frac{\sqrt{13(6)} + 7}{12(6+1)} = \frac{\sqrt{78} + 7}{84} = 0.10975$$

S6: 
$$Z_0 = \frac{\hat{\rho}_{im}}{\sigma_{\hat{p}_m}} = \frac{-0.0193}{0.10975} = -0.17$$

**S7:**  $Z_{0.025} = 1.96$ 

**S8:**  $-Z_{\alpha/2} \le Z_0 \le +Z_{\alpha/2}$ 

-1.96 ≤ -0.17 ≤ 1.96,  $H_0$  is accepted.