

Tutorial - 3

① Pseudocode for linear search

```

→ for (i = 0 to n)
  {
    if (arr[i] == value)
      {element found.}
  }
  
```

② void insertion (int arr[], int n) // recursive

```

{
  if (n <= 1)
    return;
  insertion (arr, n-1)
  int nth = arr[n-1];
  int j = n-2;
  while (j >= 0 & arr[j] > nth)
  {
    arr[j+1] = arr[j];
    j--;
  }
  arr[j+1] = nth;
}
  
```

for (i = 1 to n)

```

{
  key ← A[i];
  j ← i-1;
  while (j >= 0 and A[j] > key)
  {
    A[j+1] ← A[j];
    j ← j-1;
  }
  A[j+1] ← key
}
  
```

Insertion sort is online sorting because it doesn't know the whole input, more input can be inserted when the insertion sorting is running

⑧ Complexity

Nature Best

③ ① Bubble sort :

Time complexity - Best case = $O(n^2)$
Worst case = $O(n^2)$

Space complexity - $O(1)$

② Selection sort -

Time complexity - Best case - $O(n^2)$
Worst case - $O(n^2)$

Space complexity - $O(1)$

③ Merge sort -

Time complexity - Best case - $O(n \log n)$
Worst case - $O(n \log n)$

Space complexity - $O(n)$

④ Insertion sort -

Time complexity - Best case - $O(n)$
Worst case - $O(n^2)$

Space complexity - $O(1)$

⑤ Quick sort -

Time complexity - Best case - $O(n \log n)$
Worst case - $O(n^2)$

⑥ Heap sort -

Time complexity - Best case - $O(n \log n)$
 Space complexity = $O(1)$
 Worst case - $O(n \log n)$

⑦

Sorting

	unstable	stable	online
Selection	✓		
Insertion	✓	✓	✓
Merge		✓	
Quick	✓		
heap	✓		
bubble	✓	✓	

⑧

Iterative Binary search.

```
int binarySearch(int arr[], int l, int r, key)
{
```

```
    while (l <= r) {
```

```
        int m = (l+r)/2;
```

```
        if (arr[m] == key)
```

```
            return m;
```

```
        if (arr[m] < key)
```

```
            l = m+1;
```

```
        else
```

```
            r = m-1;
```

```
}
```

```
return -1;
```

```
}
```

Time complexity

Best Case - $O(1)$

Avg Case = $O(\log n)$

Worst Case =

$O(\log n)$

Recursive Binary Search

```
int binarySearch(int arr[], int l, int r, int key)
{
    if (r >= l) {
        int m = (l+r)/2
        if (arr[m] == key)
            return m;
        else if (arr[m] > key)
            return binarySearch(arr, l, mid-1, key);
        else
            return binarySearch(arr, mid+1, r, key);
    }
    return -1;
}
```

Time Complexity

Best case = $O(1)$

Avg case $\Rightarrow O(\log n)$

Worst case $= O(n \log n)$

Linear Search

Time complexity -

Best case $= O(1)$

Avg case $= O(n)$

Worst case $= O(n)$

⑥

Recurrence Relation for binary recursive search

$$T(n) \rightarrow T(n/2) + 1$$

(8) Quick sort is the fastest general purpose sort. In most practical situations, quicksort is the method of choice if stability is important & space is available, merge sort, max might be best.

(9) Insertion count for an array indicates how far (or close) the array is from being sorted. If the array is already sorted then the insertion count is 0 but if the array is sorted in the reverse order, the insertion count is the maximum.

```

arr[] = {7, 2, 31, 8, 10, 1, 20, 6, 4, 5}
#include <iostream>
using namespace std;
int mergesort (int arr[], int temp[], int left,
               int right);
int mergesort (int arr[], int temp[], int left,
               int mid, int right),
int mergesort (int arr[], int temp[], size)
{
    int temp [array_size];
    return mergesort (arr, temp, 0, array_size - 1)
}

```

```

int mergesort (int arr[], int temp[], int left,
               int right)
{
    int mid, invcount = 0;
    if (right > left)

```

```

    {
        mid = left + (right - left) / 2;
        invcount += mergesort(arr, temp,
                               left, mid);
        invcount += mergesort(arr, temp, right,
                               mid + 1);
        invcount += merge(arr, temp, left, mid + 1,
                           right);
    }
    return invcount;
}

```

int merge(int arr[], int temp[], int left, int mid,
 int right)

```

    {
        int i, j, k, inv_count = 0;
        i = left;
        j = mid;
        k = right;
        while ((i < mid - 1) + l(j < right))
        {
            if (arr[i] <= arr[j])
                temp[k++] = arr[i++];
            else
            {
                temp[k++] = arr[j++];
                inv_count += inv_count +
                             (mid - i);
            }
        }
    }

```

while (i < mid - 1)
 temp[i] = arr[i++];
 while (j < right)
 temp[k] = arr[j++]

```
for l < left : j < right ; i++)
    arr[i] = temp[i];
    return inv_count;
```

}
int main()

```
int arr[] = {7, 21, 51, 8, 10, 1, 20, 6, 5};
int n = size of (arr) / size of (arr[0]);
int ans = mergesort(arr, n);
cout << "no of inversions arr" << ans;
return 0;
```

}

- (10) The worst case time complexity of quick sort is $O(n^2)$. The worst case occurs when the picked pivot is always an extreme (smallest or largest) element. This happens when input array is sorted or reverse sorted and either first or last element is picked as pivot.
The best case of quick sort is when we will select pivot as a mean element.

(11) Recurrence relation of:

(a) merge sort $\Rightarrow T(n) = 2T(n/2) + n$

(b) quick sort $\Rightarrow T(n) = 2T(n/2) + n - 1$

→ Merge sort is more efficient & works faster than quick sort in case of larger arrays size or datasets.

→ Worst case complexity for quick sort is $O(n^2)$ whereas $O(n \log n)$ for merge sort.

stable selection sort

Void stableselectionsort (int arr[], int n)

{

for (int i = 0; i < n - 1; i++)

{ int min = i;

for (int j = i + 1; j < n; j++)

{

if (arr[min] > arr[j])

min = j;

}

int key = arr[min];

while (min > i)

{

arr[min] = arr[min - 1];

min --;

}

arr[i] = key;

}

}

int main()

{

int arr[] = {4, 5, 3, 2, 4, 1};

int n = sizeof(arr) / sizeof(arr[0]);

stableselectionsort (arr, n);

for (int i = 0; i < n; i++)

{ cout << arr[i] << " " ; }

cout << endl;

}

(13)

The easiest way to do this is to use external sorting we divide our source file into temporary files of size equal to the size of the RAM & first sort these files

- External sorting : If input data is such that it is cannot adjusted in the memory entirely at once it need to be stored in a hard disk , floppy disk or any other storage device. This is called external sorting.
- Internal sorting : If the input data is such that it can adjusted in the main memory at once it is called internal sorting