# Relational Algebra

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Chapter 4: Database Management System, 3<sup>rd</sup> Ed. Ramakrishnan & Gehrke

# Relational Query Languages

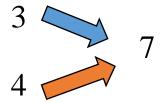
- Languages for describing queries on a relational database
- Structured Query Language (SQL)
  - Predominant application-level query language
  - Declarative
- Relational Algebra
  - Intermediate language used within DBMS
  - Procedural
- Relational Calculus:
  - Lets users describe what they want, rather than how to compute it.
  - Non-operational, declarative.

# What is an Algebra?

- A language based on operators and a domain of values
- Operators map values taken from the domain into other domain values
- Hence, an expression involving operators and arguments produces a value in the domain
- When the domain is a set of all relations (and the operators are as described later), we get the *relational algebra*
- We refer to the expression as a query and the value produced as the query result

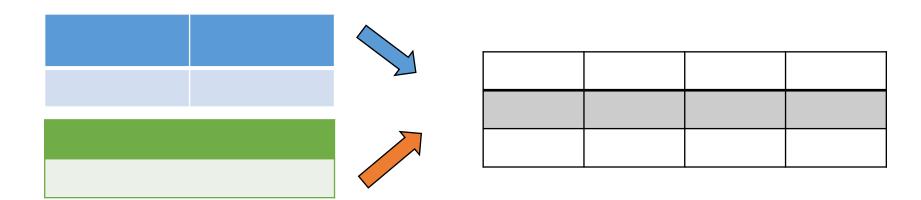
# Algebra

- In math, algebraic operations like +, -, x, /.
- Operate on numbers: input are numbers, output are numbers.
- Can also do Boolean algebra on sets, using union, intersect, difference.
- Focus on algebraic identities, e.g.
  - x (y+z) = xy + xz.
- (Relational algebra lies between propositional and 1st-order logic.)



# Relational Algebra

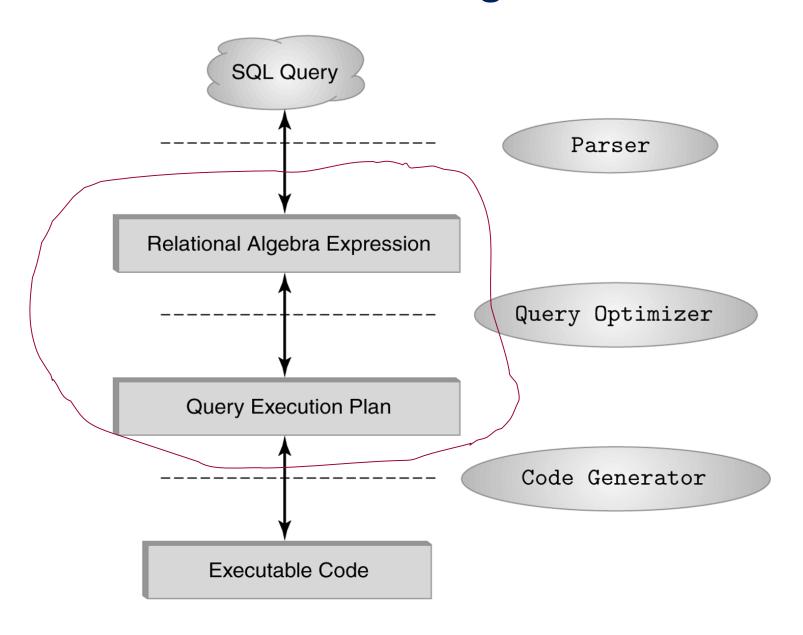
- Every operator takes one or two relation instances
- A relational algebra expression is recursively defined to be a relation
  - Result is also a relation
  - Can apply operator to
    - Relation from database
    - Relation as a result of another operator



# Relational Algebra Operations

- Domain: set of relations
- Basic operations:
  - Selection ( ) Selects a subset of rows from relation.
  - Projection ( $\pi$ ) Deletes unwanted columns from relation.
  - Cross-product (( ) Allows us to combine two relations.
  - Set-difference (\_\_\_) Tuples in reln. 1, but not in reln. 2.
  - Union ([]) Tuples in reln. 1 and in reln. 2.
- Additional derived operations:
  - Intersection, join, division, renaming.
- Since each operation returns a relation, operations can be composed!

### The Role of Relational Algebra in a DBMS



# Projection

- Deletes attributes that are not in *projection list*.
- Schema of result contains exactly the fields in the projection list, with the same names that they had in the (only) input relation.
- Projection operator has to eliminate duplicates!

Produces table containing subset of columns of argument table  $\pi_{attribute\ list}(relation)$ 

# Projection

- Deletes attributes that are not in *projection list*.
- Schema of result contains exactly the fields in the projection list, with the same names that they had in the (only) input relation.
- Projection operator has to eliminate duplicates!

Produces table containing subset of columns of argument table  $\pi_{attribute\ list}(relation)$ 

Relation: S

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

 $\pi_{sname,rating}(S)$ 

sname	rating
yuppy	9
lubber	8
guppy	5
rusty	10

 $\pi_{age}(S)$ 

age 35.0 55.5

Result is a table (no duplicates); can have fewer tuples than the original

#### Example:

#### Person

Id	Name	Address	Hobby
1123	John	123 Main	stamps
1123	John	123 Main	coins
5556	Mary	7 Lake Dr	hiking
9876	Bart	5 Pine St	stamps

### $\pi_{Name, Hobby}$ (Person)

Name	Hobby
John	stamps
John	coins
Mary	hiking
Bart	stamps

### • Example:

#### Person

Id	Name	Address	Hobby
1123	John	123 Main	stamps
		123 Main	-
5556	Mary	7 Lake Dr	hiking
9876	Bart	5 Pine St	stamps

### $\pi_{Name,Address}$ (Person)

Name	Address
John	123 Main
Mary	7 Lake Dr
Bart	5 Pine St

### • Example:

#### Person

Id	Name	Address	Hobby
1123	John	123 Main	stamps
		123 Main	•
5556	Mary	7 Lake Dr	hiking
9876	Bart	5 Pine St	stamps

### $\pi_{Name,Address}$ (Person)

Name	Address
John	123 Main
Mary	7 Lake Dr
Bart	5 Pine St

SELECT Name, Address FROM Person;

### • Example:

Person

Id	Name	Address	Hobby
1123	John	123 Main	stamps
		123 Main	_
5556	Mary	7 Lake Dr	hiking
9876	Bart	5 Pine St	stamps

 $\pi_{Name,Address}$ (Person)

Name	Address
John	123 Main
Mary	7 Lake Dr
Bart	5 Pine St

SELECT Name, Address FROM Person;

SELECT \* FROM Person; ????

### Selection

- Selects rows that satisfy *selection condition*.
- No duplicates in result!
- Schema of result identical to schema of (only) input relation.
- Selection conditions:
  - simple conditions comparing attribute values (variables) and / or constants or
  - complex conditions that combine simple conditions using logical connectives AND and OR.

Produce table containing subset of rows of argument table satisfying condition  $\sigma_{condition}$  (relation)

### Selection

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Produce table containing subset of rows of argument table satisfying condition  $\sigma_{condition}$  (relation)

#### Relation: S

sid	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

$$\sigma_{rating>8}(S)$$

sid	sname	rating	age
28	yuppy	9	35.0
58	rusty	10	35.0

## **Select Operator**

#### SELECT \* FROM Person WHERE Hobby='stamps'

#### Example:

#### Person

Id	Name	Address	Hobby
1123	John	123 Main	stamps
1123	John	123 Main	coins
5556	Mary	7 Lake Dr	hiking
9876	Bart	5 Pine St	stamps

## $\sigma_{Hobby='stamps'}$ (Person)

Id	Name	Address	Hobby
1123	John	123 Main	stamps
9876	Bart	5 Pine St	stamps

### **Selection Condition**

- Operators: <, ≤, ≥, >, =, ≠
- Simple selection condition:
  - <attribute> operator <constant>
  - <attribute> operator <attribute>
- <condition> AND <condition>
- <condition> OR <condition>
- NOT < condition >

## **Select Operator**

SELECT \* FROM Person WHERE Hobby='stamps' AND Name='John';

#### Example:

#### Person

Id	Name	Address	Hobby
1123	John	123 Main	stamps
1123	John	123 Main	coins
5556	Mary	7 Lake Dr	hiking
9876	Bart	5 Pine St	stamps

## σ<sub>Hobby='stamps' AND Name='John'</sub>(Person)

Id	Name	Address	Hobby
1123	John	123 Main	stamps

## Selection and Projection

$$\pi_{Id, Name}$$
 ( $\sigma_{Hobby='stamps' OR Hobby='coins'}$  (Person))

Id	Name	Address	Hobby
1123	John	123 Main	stamps
1123	John	123 Main	coins
5556	Mary	7 Lake Dr	hiking
	•	5 Pine St	•

Id	Name
1123	John
9876	Bart

Result

Person

SELECT Id, Name FROM Person WHERE Hobby='stamps' OR Hobby='coin'

## **Selection and Projection**

Relation: S

sid	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

 $\pi_{sname,rating}(\sigma_{rating} > 8^{(S)})$ 

sname	rating
yuppy	9
rusty	10

SELECT sname, rating FROM S WHERE rating > 8

Sailors(sid: integer, sname: string, rating: integer, age: real)

Boats(bid: integer, bnarne: string, coloT: string)

Reserves (sid: integer, bid: integer, day: date)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

An Instance of Boats

sid	ব্যস্থ	rationa	mns
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

An Instance of Sailors

 sid
 bid
 day

 22
 101
 10/10/98

 22
 102
 10/10/98

 22
 103
 10/8/98

 22
 104
 10/7/98

 31
 102
 11/10/98

 31
 103
 11/6/98

 31
 104
 11/12/98

 64
 101
 9/5/98

 64
 102
 9/8/98

 74
 103
 9/8/98

An Instance of Reserves

### Find names of sailors who've reserved boat #103

$$\pi_{sname}(\sigma_{sid=Rsid}(\sigma_{bid=103}\rho(T1(4\rightarrow Rsid), Reserves \times Sailors)))$$

$$\pi_{sname}(\sigma_{sid=RsidANDbid=103}\rho(T1(4\rightarrow Rsid), Reserves \times Sailors))$$

## **Set Operators**

- Relation is a set of tuples, so set operations should apply:  $\cap$ ,  $\cup$ , (set difference)
- Result of combining two relations with a set operator is a relation =>
   all its elements must be tuples having same structure
- Hence, scope of set operations limited to union compatible relations

# **Union Compatible Relations**

- Two relations are union compatible if
  - Both have same number of columns
  - Names of attributes are the same in both
  - Attributes with the same name in both relations have the same domain
- Union compatible relations can be combined using union, intersection, and set difference

## Example

```
Tables:
     Person (SSN, Name, Address, Hobby)
     Professor (Id, Name, Office, Phone)
are not union compatible.
But
     \pi_{Name} (Person) and \pi_{Name} (Professor)
are union compatible so
     \pi_{Name} (Person) - \pi_{Name} (Professor)
makes sense.
```

# Union, Intersection, Set-Difference

*S*1

sid	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

S2

sid	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

sid	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0
44	guppy	5	35.0
28	yuppy	9	35.0

sid	sname	rating	age
22	dustin	7	45.0

sid	sname	rating	age
31	lubber	8	55.5
58	rusty	10	35.0

$$S1-S2$$

$$S1 \cap S2$$

## UNION, INTERSECT, EXCEPT

#### $S1 \cup S2$

```
SELECT column_name(s) FROM table1 UNION SELECT column_name(s) FROM table2; S1 \cap S2 SELECT column_name(s) FROM table1 INTERSECT SELECT column_name(s) FROM table2;
```

#### S1-S2

SELECT column\_name(s) FROM table1

MINUS

SELECT column\_name(s) FROM table1

EXCEPT

SELECT column\_name(s) FROM table2;

SELECT column\_name(s) FROM table2;

## UNION, INTERSECT, EXCEPT

#### $S1 \cup S2$

```
SELECT column name(s) FROM table1
UNION
SELECT column_name(s) FROM table2;
S1 \cap S2
SELECT column name(s) FROM table1
INTERSECT
SELECT column_name(s) FROM table2;
S1-S2
SELECT column_name(s) FROM table1
                                         SELECT column_name(s) FROM table1
MINUS
                                         EXCEPT
SELECT column name(s) FROM table2;
                                         SELECT column name(s) FROM table2;
MySQL
select a.id from table1 as a where <condition>
      AND a.id NOT IN
```

(select b.id from table2 as b where <condition>);

### UNION, INTERSECT, EXCEPT

#### $S1 \cup S2$

```
SELECT column_name(s) FROM table1
UNION
SELECT column_name(s) FROM table2;
```

#### $S1 \cap S2$

SELECT column\_name(s) FROM table1
INTERSECT
SELECT column\_name(s) FROM table2;

#### S1-S2

SELECT column\_name(s) FROM table1
MINUS
SELECT column\_name(s) FROM table3

SELECT column\_name(s) FROM table

#### Renaming

EXCEPT

SELECT column\_name(s) FROM table1

SELECT column\_name(s) FROM table2;

#### **MySQL**

select a.id from table1 as a where <condition>
AND a.id NOT IN

(select b.id from table2 as b where <condition>);

## **EXCEPT/MINUS**

```
S1-S2
```

SELECT column\_name(s) FROM table1

MINUS

SELECT column\_name(s) FROM table1

EXCEPT

SELECT column\_name(s) FROM table2;

SELECT column\_name(s) FROM table2;

#### **MySQL**

SELECT \* FROM table1 AS a WHERE <condition>
AND a.id NOT IN

(SELECT b.id FROM table2 AS b WHERE <condition>);

OR

SELECT \* FROM table1 a WHERE NOT EXISTS (SELECT \* FROM table2 b WHERE a.id = b.id);

### Cartesian Product

- If *R* and *S* are two relations, *R* × *S* is the set of all concatenated tuples <*x*,*y*>, where *x* is a tuple in *R* and *y* is a tuple in *S* 
  - R and S need not be union compatible.
  - But R and S must have distinct attribute names.

## **Cartesian Product**

- If *R* and *S* are two relations, *R* × *S* is the set of all concatenated tuples <*x*,*y*>, where *x* is a tuple in *R* and *y* is a tuple in *S* 
  - R and S need not be union compatible.
  - But R and S must have distinct attribute names.

SELECT \* FROM R, S;

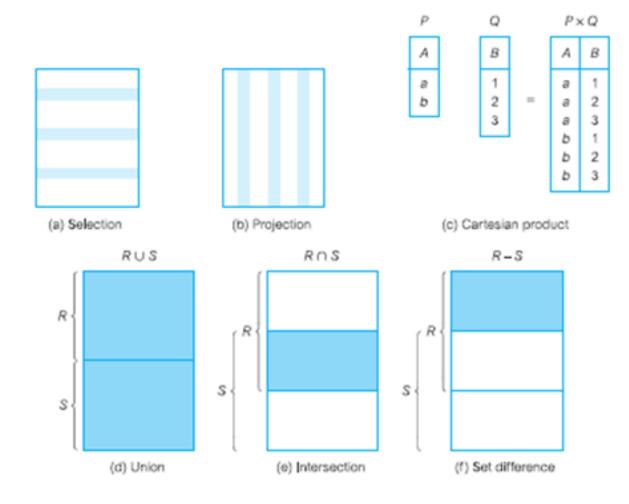
## Renaming

• Renaming operator:

$$\rho(C(1 \rightarrow X, 3 \rightarrow Y), R \times S)$$

$$\rho(\Pi_{A,\rho(A \to X)}(R) \times \Pi_{A,\rho(A \to Y)}(S)$$

# Summary



# Examples

Professor(<u>ssn</u>, profname, status)
Course(<u>crscode</u>, crsname, credits)
Taught(<u>crscode</u>, <u>semester</u>, ssn)

Find those professors who have taught 'csc6710' but never 'csc7710'.

# Examples

Professor(<u>ssn</u>, profname, status)
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Find those professors who have taught 'csc6710' but never 'csc7710'.

$$\pi_{ssn}(\sigma_{crscode=csc6710}, crscode!=csc7710}, (Taught))$$

# Examples

Professor(<u>ssn</u>, profname, status)
Course(<u>crscode</u>, crsname, credits)
Taught(<u>crscode</u>, <u>semester</u>, ssn)

Find those professors who have taught 'csc6710' but never 'csc7710'.

$$\pi_{ssn}(\sigma_{crscode='csc6710})$$
 (rscode!='csc7710', (Taught))

Professor(<u>ssn</u>, profname, status)
Course(<u>crscode</u>, crsname, credits)
Taught(<u>crscode</u>, <u>semester</u>, ssn)

Find those professors who have taught 'csc6710' but never 'csc7710'.

$$\pi_{ssn}(\sigma_{crscode='csc6710}, (Taught)) - \pi_{ssn}(\sigma_{crscode='csc7710}, (Taught))$$

Professor(<u>ssn</u>, profname, status)
Course(<u>crscode</u>, crsname, credits)
Taught(<u>crscode</u>, <u>semester</u>, ssn)

Find those professors who have taught 'csc6710' but never 'csc7710'.

$$\pi_{ssn}(\sigma_{crscode='csc6710}, (Taught)) - \pi_{ssn}(\sigma_{crscode='csc7710}, (Taught))$$

SELECT x.ssn FROM Taught AS x WHERE x.crscode='csc6710' AND x.ssn NOT IN

(SELECT ssn FROM Taught WHERE y.crscode='csc7710');

SELECT x.ssn FROM Taught AS x WHERE x.crscode='csc6710' AND NOT EXIST

(SELECT y.ssn FROM Taught AS y WHERE y.crscode='csc7710' AND x.ssn=y.ssn);

Professor(<u>ssn</u>, profname, status)
Course(<u>crscode</u>, crsname, credits)
Taught(<u>crscode</u>, <u>semester</u>, ssn)

Return those professors who have taught both 'csc6710' and 'csc7710'.

Professor(<u>ssn</u>, profname, status)
Course(<u>crscode</u>, crsname, credits)
Taught(<u>crscode</u>, <u>semester</u>, ssn)

Return those professors who have taught both 'csc6710' and 'csc7710'.

$$\pi_{ssn}(\sigma_{crscode='csc6710', \land crscode='csc7710'}, (Taught))$$

Professor(<u>ssn</u>, profname, status)
Course(<u>crscode</u>, crsname, credits)
Taught(<u>crscode</u>, <u>semester</u>, ssn)

Return those professors who have taught both 'csc6710' and 'csc7710'.

$$\pi_{ssn}(\sigma_{crscode='csc6710}, (Taught))$$
 $\pi_{ssn}(\sigma_{crscode='csc6710}, (Taught)) \cap$ 
 $\pi_{ssn}(\sigma_{crscode='csc7710}, (Taught))$ 

SELECT ssn FROM Taught WHERE crscode='csc6710' INTERSECT

SELECT ssn FROM Taught WHERE crscode='csc7710';

Professor(<u>ssn</u>, profname, status)
Course(<u>crscode</u>, crsname, credits)
Taught(<u>crscode</u>, <u>semester</u>, ssn)

#### Return those professors who have taught both 'csc6710' and 'csc7710'.

$$\pi_{ssn}(\sigma_{crscode='csc6710}, (crscode='csc7710', (Taught))$$

$$\pi_{ssn}(\sigma_{crscode='csc6710}, (Taught)) \cap \pi_{ssn}(\sigma_{crscode='csc7710}, (Taught))$$

SELECT x.ssn FROM Taught AS x WHERE x.crscode='csc6710' AND x.ssn IN

(SELECT y.ssn FROM Taught AS y WHERE y. crscode='csc7710');

Professor(<u>ssn</u>, profname, status)
Course(<u>crscode</u>, crsname, credits)
Taught(<u>crscode</u>, <u>semester</u>, ssn)

#### Return those professors who have taught both 'csc6710' and 'csc7710'.

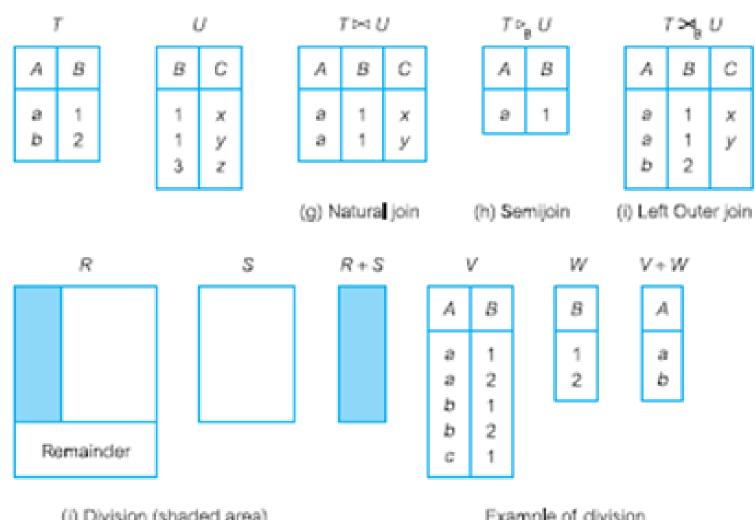
$$\pi_{ssn}(\sigma_{crscode='csc6710}, (crscode='csc7710', (Taught))$$

$$\pi_{ssn}(\sigma_{crscode='csc6710}, (Taught)) \cap \pi_{ssn}(\sigma_{crscode='csc7710}, (Taught))$$

SELECT x.ssn FROM Taught AS x WHERE x.crscode='csc6710' AND EXIST

(SELECT y.ssn FROM Taught AS y WHERE y.crscode='csc7710' AND x.ssn=y.ssn);

## Derived Operators Join and Division



(i) Division (shaded area)

Example of division

### Joins

• Condition Join:

$$R \bowtie_{c} S = \sigma_{c}(R \times S)$$

(sid)	sname	rating	age	(sid)	bid	day
22	dustin	7	45.0	58	103	11/12/96
31	lubber	8	55.5	58	103	11/12/96

$$S1 \bowtie S1.sid < R1.sid$$

- Result schema same as that of cross-product.
- Fewer tuples than cross-product, might be able to compute more efficiently.
- Sometimes called a *theta-join*.

### Joins

• <u>Equi-Join</u>: A special case of condition join where the condition *c* contains only **equalities**.

sid	sname	rating	age	bid	day
22	dustin	7	45.0	101	10/10/96
58	rusty	10	35.0	103	11/12/96

$$S1 \bowtie Rsid = S.sid R1$$

- Result schema similar to cross-product, but only one copy of fields for which equality is specified.
- <u>Natural Join</u>: Equijoin on *all* common fields. Without specified condition means the natural join of A and B.  $A \bowtie B$

## Natural Join (cont'd)

More generally:

$$R \bowtie S = \pi_{attr-list} (\sigma_{join-cond} (R \times S))$$

where

attr-list = attributes (R)  $\cup$  attributes (S) (duplicates are eliminated) and join-cond has the form:

$$R.A_1 = S.A_1$$
 AND ... AND  $R.A_n = S.A_n$   
where  $\{A_1 ... A_n\} = attributes(R) \cap attributes(S)$ 

SELECT \* FROM table1 join\_type table2 [ON (join\_condition)]

- EQUI JOIN
  - INNER JOIN
  - OUTER JOIN
    - LEFT OUTER JOIN
    - RIGHT OUTER JOIN
    - FULL OUTER JOIN
- NON EQUI JOIN
- NATURAL JOIN
- CROSS JOIN

loan-number	branch-name	amount
L-170	Downtown	3000
L-230	Redwood	4000
L-260	Perryridge	1700

customer-name	loan-number
Jones	L-170
Smith	L-230
Hayes	L-155

loan borrower

#### SELECT \* FROM table1 join\_type table2 [ON (join\_condition)]

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loan-number	branch-name	amount	customer-name	loan-number
L-170	Downtown	3000	Jones	L-170
L-230	Redwood	4000	Smith	L-230

loan-number	branch-name	amount
L-170	Downtown	3000
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loan-number	branch-name	amount	customer-name
L-170	Downtown	3000	Jones
L-230	Redwood	4000	Smith

loan-number	branch-name	amount
L-170	Downtown	3000
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loan

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loan-number	branch-name	amount	customer-name	loan-number
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L-170	Downtown	3000	Jones
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loan-number	branch-name	amount	customer-name	loan-number
L-170	Downtown	3000	Jones	L-170
L-230	Redwood	4000	Smith	L-230
L-260	Perryridge	1700	null	null

loan-number	branch-name	amount
L-170	Downtown	3000
L-230	Redwood	4000
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customer-name	loan-number
Jones	L-170
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loan borrower

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loan-number	branch-name	amount	customer-name	loan-number
L-170	Downtown	3000	Jones	L-170
L-230	Redwood	4000	Smith	L-230
null	null	null	Hayes	L-155

loan-number	branch-name	amount
L-170	Downtown	3000
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customer-name	loan-number
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borrower

SELECT \* FROM table1 join\_type table2 [ON (join\_condition)]

loan

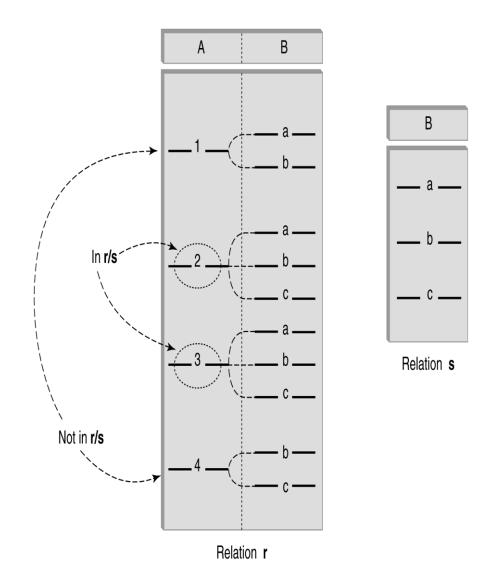
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    - LEFT OUTER JOIN
    - RIGHT OUTER JOIN
    - FULL OUTER JOIN
- NON EQUI JOIN
- NATURAL JOIN
- CROSS JOIN

loan-number	branch-name	amount	customer-name	loan-number
L-170	Downtown	3000	Jones	L-170
L-230	Redwood	4000	Smith	L-230
L-260	Perryridge	1700	null	null
null	null	null	Hayes	L-155

### Division

- Goal: Produce the tuples in one relation r, that match all tuples in another relation s
  - $r(A_1, ...A_n, B_1, ...B_m)$
  - $s(B_1...B_m)$
  - r/s, with attributes A<sub>1</sub>, ...A<sub>n</sub>, is the set of all tuples <a> such that for every tuple <b> in s, <a,b> is in r

**Example:** List of sailors who've reserved all boats



# Examples of Division A/B

sno	pno	pno	pno	pno
s1	p1	prio p2	p2	p1
s1	p2		p4	p2
s1	p2 p3 p4	B1	1	p4
s1	p4		<i>B</i> 2	1
s2	p1	sno		В3
s2 s3	p2	s1		
s3	p2	$\frac{s_1}{s_2}$	sno	
s4	p2 p4	s3	s1	sno
s4	p4	$\frac{s}{s}$	s4	s1
	A	A/B1	A/B2	A/B3

### Division

Given two relations(tables): R(x,y), S(y).

**R(x,y)** div **S(y)** means gives all distinct values of x from R that are associated with all values of y in S.

**Computation of Division :** R(x,y) div S(y) **Steps:** 

•Find out all possible combinations of S(y) with R(x) by computing R(x) x(cross join) S(y)

• 
$$r1 = R(x) X S(y)$$

•Subtract actual R(x,y) from r1, say r2  $\pi_{\chi}((\pi_{\chi}(A) \times B) - A)$ •r2 = r1 -R(x,y)

•x in r2 are those that are not associated with every value in S(y); therefore R(x)-r2(x) gives us x that are associated with all values in S  $\pi_{\,\,\chi}(A) \,-\, \pi_{\,\chi}((\pi_{\chi}(A)\!\!\times\!\!B)\!\!-\!\!A)$ 

```
\rho \; (Tempsids, (\pi_{sid,bid} Reserves) \, / \, (\pi_{bid} Boats))
\pi \; sname \; (Tempsids \bowtie Sailors)
```

$$\rho \; (Tempsids, (\pi_{sid,bid} Reserves) \; / \; (\pi_{bid} Boats))$$

$$\pi \; _{sname} \; (Tempsids \bowtie Sailors)$$

To find sailors who've reserved all 'red boats:

$$\rho_{bid}(S_{color='red'},Boats)$$

```
\rho (Tempsids, (\pi_{sid,bid}Reserves) / (\pi_{bid}Boats))
\pi_{sname} (Tempsids \bowtie Sailors)
SELECT sid FROM Reserves WHERE bid NOT IN
  (SELECT sid FROM (
                     (SELECT sid, bid FROM
                          ( SELECT bid FROM Boats
                                                                  //S(y) \times R(x)
                          CROSS JOIN
                          SELECT DISTINCT sid FROM Reserves
                         ) AS r1
                                                                 // r1(x,y) = S(y) x R(x)
                    EXCEPT
                    (SELECT sid, bid FROM Reserves)
                   ) AS r2
                                                                 // r2=r1 – R
                                                                 // R/S
```

```
\rho \text{ (Tempsids, } (\pi_{sid,bid} \text{Reserves)} / (\pi_{bid} \text{Boats)})
\pi_{sname} \text{ (Tempsids} \bowtie \text{Sailors)}
```

```
SELECT * FROM Reserves AS r WHERE

NOT EXISTS

((SELECT b.bid FROM Boats AS b)

EXCEPT

(SELECT t.bid FROM Reserves AS t WHERE t.bid = r.bid)
);
```

### Aggregate Functions and Operations

 Aggregation function takes a collection of values and returns a single value as a result.

avg: average value

min: minimum value

max: maximum value

**sum**: sum of values

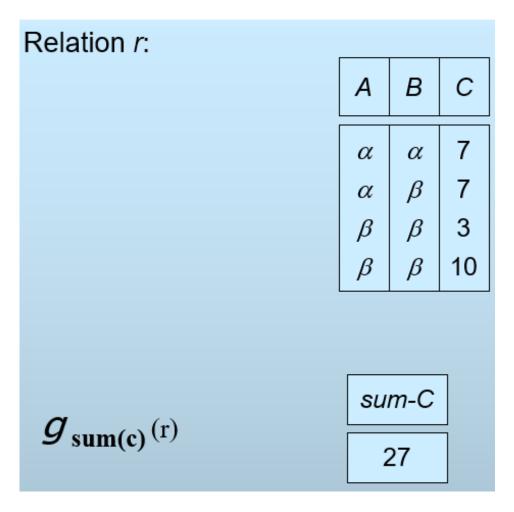
count: number of values

Aggregate operation in relational algebra

G1, G2, ..., Gn 
$$\mathcal{G}_{F1(A1), F2(A2),..., Fn(An)}(E)$$

- E is any relational-algebra expression
- $G_1$ ,  $G_2$  ...,  $G_n$  is a list of attributes on which to group (can be empty)
- Each F<sub>i</sub> is an aggregate function
- Each A<sub>i</sub> is an attribute name

# Aggregate Operation – Example



# Aggregate Operation – Example

#### Relation *account* grouped by *branch-name*:

branch-name	account-number	balance
Perryridge	A-102	400
Perryridge	A-201	900
Brighton	A-217	750
Brighton	A-215	750
Redwood	A-222	700

 $branch-name g_{sum(balance)}(account)$ 

branch-name	balance
Perryridge	1300
Brighton	1500
Redwood	700

# Aggregate Functions (Cont.)

- Result of aggregation does not have a name
  - Can use rename operation to give it a name
  - For convenience, we permit renaming as part of aggregate operation

branch-name g sum(balance) as sum-balance (account)