## Jashore University of Science and Technology Department of Physics

Bachelor of Science with Honours in Physics First semester of Third year

Course no.: PHY 3103 Course title: Quantum Mechanics I Assignment no.: 01 Date: May 03, 2022

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- 1. Show that the components of angular momentum operator  $\hat{\mathbf{L}}$  do not commute with each other but they all commute with  $\hat{\mathbf{L}}^2$ . [5] 2. Let  $\hat{\mathbf{L}}$  be a quantum-mechanical angular momentum operator. Evaluate  $[[\hat{L}_x, \hat{L}_y], [\hat{L}_y, \hat{L}_z]]$ . [4]
- **3.** Derive the expressions to write angular momentum operators  $\hat{L}_x$ ,  $\hat{L}_y$ ,  $\hat{L}_z$  and  $\hat{\mathbf{L}}^2$  in spherical coordinates. [4]
- **4.** If  $\hat{L}_z Y_{lm} = \hbar m Y_{lm}$ , where  $Y_{lm}$  is the spherical harmonics show that  $m \in \mathbb{Z}$ .
- 5. Write down the properties of eigenvalue of  $\hat{\mathbf{L}}^2$ .