

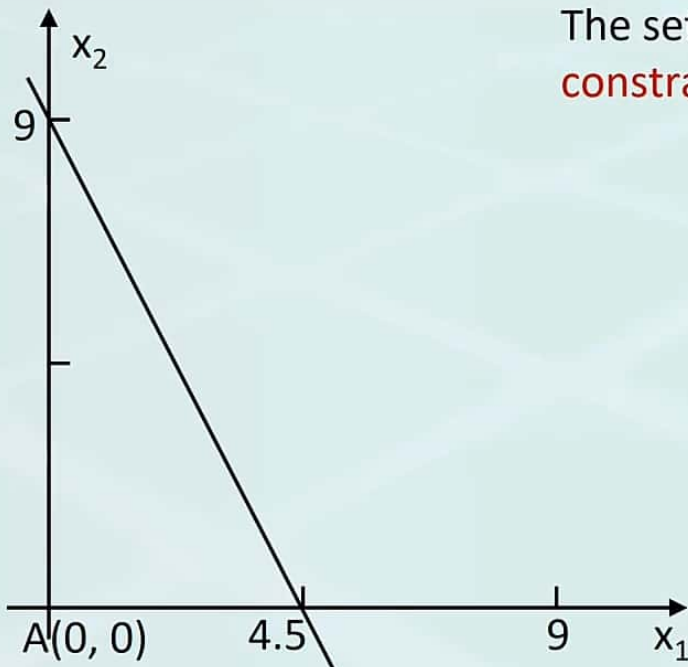
Linear Programming

Feasible Region



BINGHAMTON
UNIVERSITY

Find Feasible Region Graphically



The set of all points satisfying all the LP's constraints and sign restrictions.

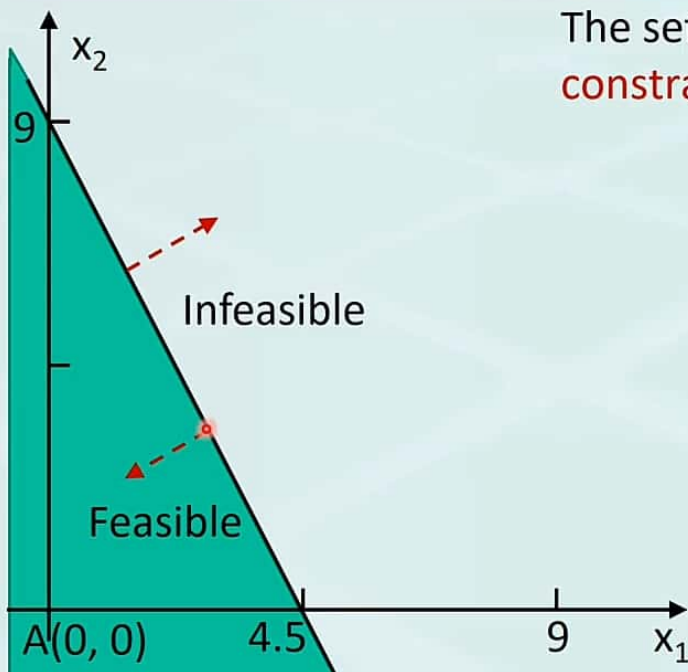
$$2x_1 + x_2 \leq 9$$

$$2x_1 + x_2 = 9$$

$$(x_1=0) \ x_2=9$$

$$x_1=4.5 \ (x_2=0)$$

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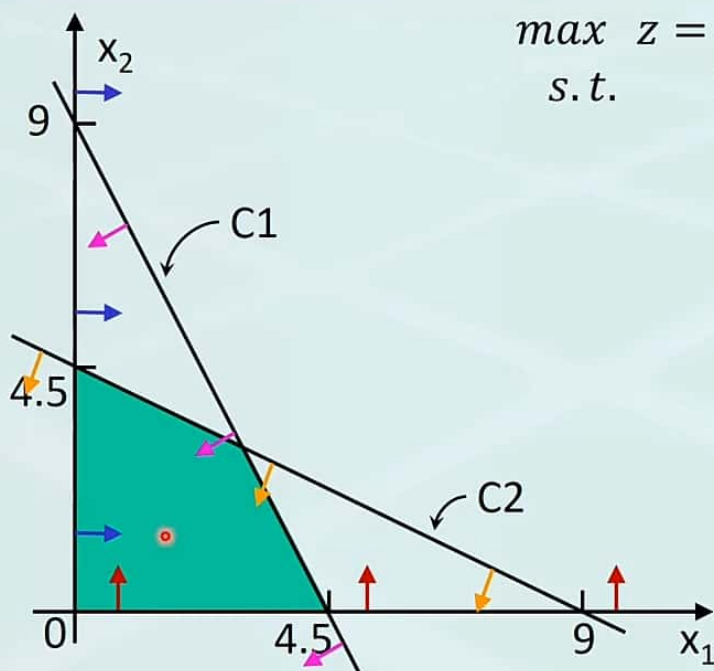
$$(x_1=0) \ x_2=9$$

$$x_1=4.5 \ (x_2=0)$$

Check Point A $(0, 0)$:

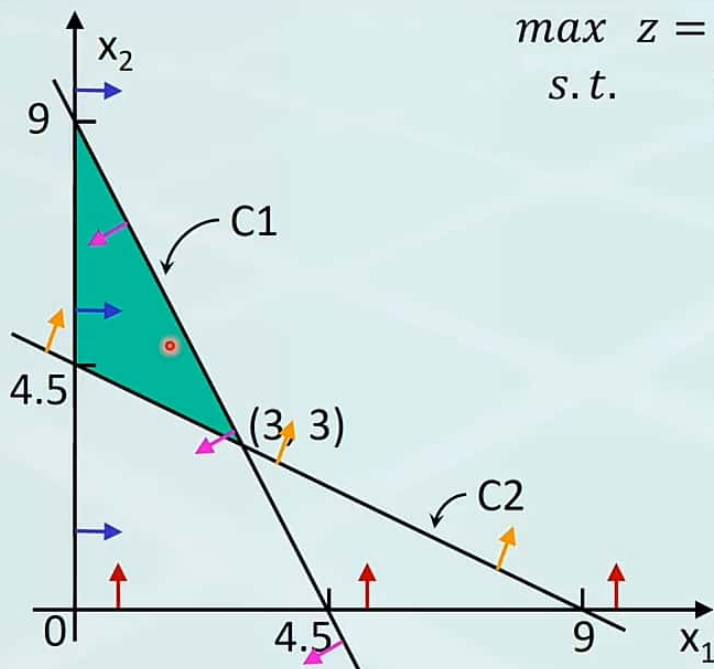
$$2 \times 0 + 0 = 0 \leq 9 \text{ (Feasible)}$$

Feasible Region - Example 1



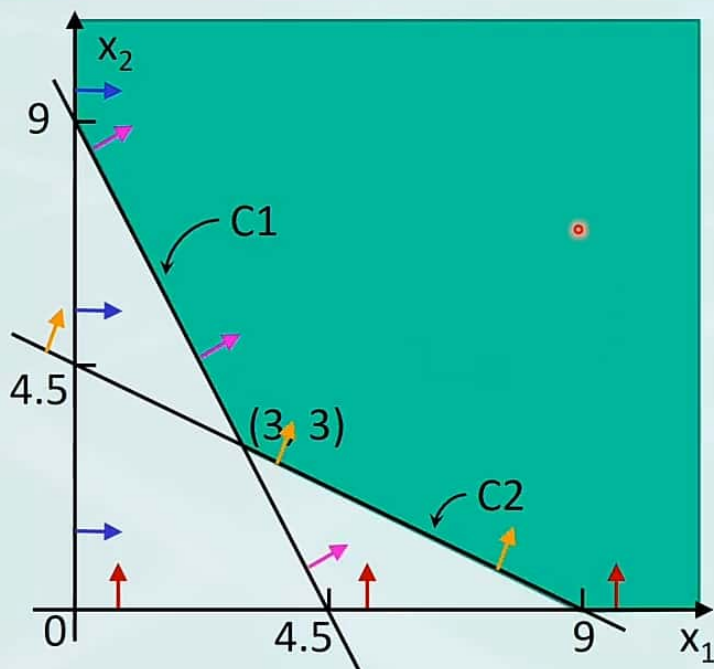
$$\begin{aligned} \max \quad & z = 3x_1 + 2x_2 \\ \text{s.t.} \quad & 2x_1 + x_2 \leq 9 \text{ (C1)} \\ & x_1 + 2x_2 \leq 9 \text{ (C2)} \\ & x_i \geq 0 \text{ (} i = 1, 2 \text{)} \end{aligned}$$

Feasible Region - Example 2



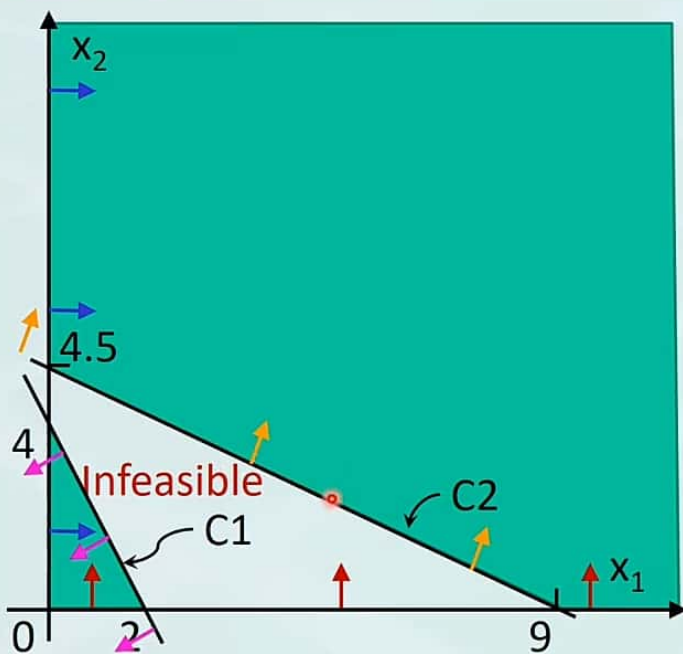
$$\begin{aligned} \max \quad & z = 3x_1 + 2x_2 \\ \text{s.t.} \quad & 2x_1 + x_2 \leq 9 \text{ (C1)} \\ & x_1 + 2x_2 \geq 9 \text{ (C2)} \\ & x_i \geq 0 \text{ (} i = 1, 2 \text{)} \end{aligned}$$

Feasible Region - Example 3



$$\begin{aligned} \max \quad & z = 3x_1 + 2x_2 \\ \text{s.t.} \quad & 2x_1 + x_2 \geq 9 \text{ (C1)} \\ & x_1 + 2x_2 \geq 9 \text{ (C2)} \\ & x_i \geq 0 \text{ (} i = 1, 2 \text{)} \end{aligned}$$

Feasible Region - Example 4



$$\begin{aligned} \max \quad & z = 3x_1 + 2x_2 \\ \text{s.t.} \quad & 2x_1 + x_2 \leq 4 \text{ (C1)} \\ & x_1 + 2x_2 \geq 9 \text{ (C2)} \\ & x_i \geq 0 \text{ (} i = 1, 2 \text{)} \end{aligned}$$