

Inside or Outside

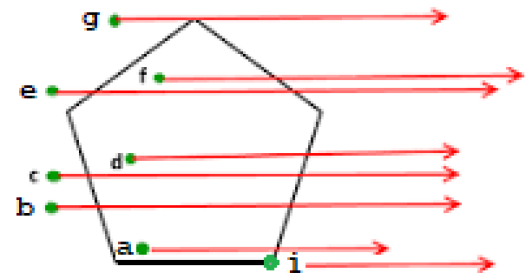
The motivation for this problem comes from this problem asked by Nvidia.

You are given a list of N points $(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N)$ representing a convex polygon. You can assume these points are given in order; that is, you can construct the polygon by connecting point 1 to point 2, point 2 to point 3, and so on, finally looping around to connect point N to point 1.

Determine if a new point p lies inside this polygon.

Note: If p is on the boundary of the polygon, return false.

For example, in the figure to the right, the points a, d, and f all lie inside the polygon, the remaining points (including point i which lies on an edge) are all considered to lie outside the polygon.



My first step in solving this problem was to Google it, and according to:

<https://www.geeksforgeeks.org/how-to-check-if-a-given-point-lies-inside-a-polygon/>

1. Draw a horizontal line to the right of the point and extend it to infinity.
2. Count the number of times the line intersects with polygon edges.
3. If either the count of intersections is even (remember, zero is even), or if the point lies on an edge of polygon, the point lies outside.
4. A point is inside the polygon if the count of intersections is odd and does NOT lie on an edge.

To help with this problem, you have been given the completed `Point` class. The constructor for this class has two parameters, the first parameter is the x-coordinate and the second is the y-coordinate. It has accessor methods `getX()` that returns the x-value and `getY()` that returns the y-value.

The first method to implement is the static method `getSlopeIntercept(Point p1, Point p2)`, which given two points `p1` and `p2`, returns a `double[]` containing two values. The value in index 0 is the slope of the line containing the points `p1` and `p2`. The value in index 1 is the y-intercept of the line containing the points `p1` and `p2`. You may assume the line determined by `p1` and `p2` is not a vertical line.

The following code shows the results of the `getSlopeIntercept` method.

The following code	Returns
<pre>double[] eq = InsideOrOutside.getSlopeIntercept(new Point(1., 2.), new Point(3., 7.));</pre>	
<code>eq[0]</code>	2.5
<code>eq[1]</code>	-0.5

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The second method to implement is the static method

`intersectsLineSegmentToRight(Point p, Point t1, Point t2)`, which returns a `boolean`. The method returns true if:

- The ray drawn horizontally to the right from the parameter `p` intersects the (interior of the) line segment connecting points `t1` and `t2`. That is, if the ray intersects at the endpoints, the method returns false.
- And the Point `p` is not on the line segment connecting points `t1` and `t2`.

The following code shows the results of the `intersectsLineSegmentToRight` method.

The following code	Returns
<pre>boolean doesInter = InsideOrOutside.intersectsLineSegmentToRight (new Point(1., 1.), new Point(0., 0.), new Point(6., 3.));</pre>	
<pre>doesInter</pre>	true
<pre>boolean doesInter = InsideOrOutside.intersectsLineSegmentToRight (new Point(3., 2.), new Point(1., 4.), new Point(2., 7.));</pre>	
<pre>doesInter</pre>	false
<pre>doesInter = InsideOrOutside.intersectsLineSegmentToRight (new Point(-2., 4.), new Point(1., 4.), new Point(2., 7.));</pre>	
<pre>doesInter</pre>	false
<pre>doesInter = InsideOrOutside.intersectsLineSegmentToRight(new Point(2., 5.), new Point(1., 4.), new Point(4., 7.));</pre>	
<pre>doesInter</pre>	false

The third method is the (non static) method `numberEdgesIntersection(Point p)`, which returns the number of Polygon edges the Horizontal ray from Point `p` to the right intersects.

The following code shows the results of the `numberEdgesIntersection` method.

The following code	Returns
<pre>Point[] poly1 = { new Point(1,1), new Point(2, 4), new Point(6, 6), new Point(7,5), new Point(3, 2)};</pre>	
<pre>InsideOrOutside ioo = new InsideOrOutside(poly1);</pre>	
<pre>ioo.numberEdgesIntersection(new Point(0, 2.5))</pre>	2
<pre>ioo.numberEdgesIntersection(new Point(3.0, 3.0))</pre>	1
<pre>ioo.numberEdgesIntersection(new Point(8.0, 5.0))</pre>	0

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The fourth (and final) method is the (non static) method `insidePolygon(Point p)`, which returns `true` if `Point p` is inside the polygon, otherwise, return `false`. Remember, if `Point p` lies on the boundary, return `false`.

The following code shows the results of the `insidePolygon` method.

The following code	Returns
<pre>Point[] poly1 = { new Point(1,1), new Point(2, 4), new Point(6, 6), new Point(7,5), new Point(3, 2)};</pre>	
<pre>InsideOrOutside ioo = new InsideOrOutside(poly1);</pre>	
<pre>ioo.insidePolygon(new Point(0, 2.5));</pre>	false
<pre>ioo.insidePolygon(new Point(3.0, 3.0));</pre>	true
<pre>ioo.insidePolygon(new Point(8.0, 5.0));</pre>	false

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