Advanced Programming Exam 2015

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1 SubScript, Parser

The parser is built using the Parsec library. It is constructed by checking that the input is well formed, based on the grammar, and builds the internal SubsAst representation. The source code can be found E.1.

1.1 The Grammar

The grammar has been changed slightly. The Stms has been redefined to look like

This is equivalent to the handed out grammar except that the grammar can not be used for empty programs which I did not consider as a loss.

For Stm, though the grammar can not be expressed in the same way as it uses some auxillary function, it should behave exactly the same.

For Expr we wanted to avoid left recursion problems, as in the following (from the handed out grammar):

This is dealt with by converting the first Expr to an Expr1. When the grammer is left recursive, we can't determine where to go by looking at the first symbol (in top-down parsing).

We also wanted Expr1 to account for the fact that the arithmetic operators * and % binds stronger than + and - which in turn binds stronger than < and then ===. This was handled in the following way:

```
expr1 :: Parser Expr
expr1 = do
    rv <- r
    botbot rv

botbot :: Expr -> ParsecT String () Data.Functor.Identity.Identity Expr
botbot inval = do
    void % lexeme % string "==="
    rv <- r
    botbot (Call "===" [inval, rv])
    <|> return inval

r :: ParsecT String () Data.Functor.Identity.Identity Expr
r = do
    sv <- s
    bot sv

bot :: Expr -> ParsecT String () Data.Functor.Identity.Identity Expr
bot inval = (do
    void % lexeme % char '<'
    sv <- s
    bot (Call "<" [inval, sv]))
    <|> return inval
```

This is only for one level of precedence (=== binds weaker than <), but it applies the same principle to the following levels.

The rest of the grammar all have some relation to eachother, but the entire grammer is implemented. Note that it is not implemented in a straight forward manner as there are many auxillary functions and

some parts might be parsed a different place compared to the grammar, but a parsed program should correspond to abstract syntax tree that is handed out without changes to it.

1.2 Parser Solution and Testing

The following commands are supported for parsing a program

SubsParser> parseFile "Path to file with a program"

or

SalsaParser> parseString "Program as string"

To test the parser, there is used an HUnit testsuite, which executes a number of tests based on assertions. To run these tests, load the module ParserTest.hs (in ../src/subs or appendix D.1) and use the following command

ParserTest> runTestTT tests

The main test is the program intro.js, which produces a SubsAst which is (almost) identical to the one in the handouts. The only difference is that sometimes there is a space after a comma in the handouts, but not in this parser. The SubsAst's can be found in appendix A.1. This test covers most of the for and if aswell as array and parentheses in the grammer.

Other tests (denoted TestSuccX, where X is a number) include small programs that succeed in precedence, associativity, Ident names and FunName. These parse correctly (this can also mean that it fails to parse when it should). These tests are about other things in the grammar that is not in intro.js

1.3 Assessment

First, an assessment of the codestyle. No warnings are produced, but there are 7 suggestions when using hlint. All but on of these are "reduce duplication", which I have chosen to ignore. The last suggestion seem to break the code.

The parser itself correctly parses most of the input. It successfully parses the intro.js program which uses a great part of the grammar. Precedence also works as intended.

Testing could have been more thorough. Right now, I am aware that it does not fail when there is a space before an "." (but it should), but it breaks another part of the code to fix this, so we will call this a feature for now. I am sure there are a lot more edge cases that parses incorrectly, but the 'essential' aspects of the parser is working - I would have used QuickCheck to find the edge cases that parses incorrectly, but time constraints has kept me from this as I was not familiar with it.

2 SubScript, Interpreter

The source code can be found in appendix E.2.

2.1 The SubsM Monad

The implemented SubsM monad is very similar to the state monad. To construct a SubsM instance of type a, we go from a context to either an error (which is a string) or some (a, env) where the environment, env, is mapping from variable names to values. A context consists of an environment and another mapping, PEnv, from function names and operands to the haskell functions implementing them.

Utility function: Three auxillary functions has been implemented, namely getEnv, getPEnv and putEnv. We use these to update the environment, *env*, by getting the environment, inserting a key and value (overwriting if it exists), and putting the environment back in the context. We use them in the same manner to fetch values from the environment and getting function from the primitives environment, *PEnv*.

This function evalExpr implements the evaluation of expressions. The evaluation can raise errors when operands are not of the same type (besides the special case with a string and and integer in addition, which results in a string) or when a non-existent variable or function is referred to.

This function stm works in the same manner and the function program evaluates a statement and recursively calls itself until there are no more statements (end of program).

The last function, runProg, invokes the function runSubsM wrapped inside of the type contructor for SubsM. We construct an initial context that consists of an empty environment env and the primitives environment PEnv where the haskell functions have been implemented. Since there is no API for updating the primitives environment, this is the same throughout the entire program. Given the initial context and a statement, we get an error or a new environment. If it succeeds, the context is updated with the new environment. This is repeated until there are no more statements, in which the program terminates.

2.2 Missing Implementation

Array comprehension has not been implemented (which makes the utility function modify superfluous, so it is commented out). This obviously means that the implemented version of SubScript lacks a lot of functionality.

2.3 Interpreter Testing

The testing that has been done is "blackbox" testing. In appendix B.1 is the program simpleProg.js and the output from running the program. The program runs statements that should be legal and that they are evaluated correctly.

All statement should be legal, which is verified by the interpreter not generating any error. The most interesting cases are that

- Variable 'a' can be referred to after having been declared (line 2)
- Strings are compared by their lexographic order (var 'e' and 'f' in line 6-7)
- Variable 'i', which is a string, can be concatenated with integers and the other way around for 'j' (line 11 12). Note that "2 * 3" is evaluated first.
- var 'l' is initialized with value 'undefined'

The other cases are just statements that are evaluated correctly.

In appendix B.2, the errors that the interpreter can generate is listed. These are simply "bad types" and "Key does not exist" errors. However they state in what kind of expression, the error occurred.

All other errors are generated by the parser which is tested in Section 1. Note that all tests associated with the interpreter has the prefix "intrp_".

2.4 Assessment

The testing is very simple, but rightfully so, as array comprehension has not been implemented which would be a big part of it.

However, leaving that aside, the supported functionality is working satisfactory. It generates errors when it should and evaluates legal statements correctly. I have not been able to produce a statement that is evaluated wrong.

Running programs with the implemented parser might be faulty, but I feel confident that the interpreter is working as intended (what functionality is implemented) and if there are any "mistakes", I would suspect that the parser might have parsed something wrong.

3 Generic Replicated Server Library

The module gen_replicated has been implemented and the source code can be found in appendix E.3.

3.1 Implementation

The implementation for *coordinator* loops with the argument *Pids*, a list of process ID's on all the replicas.

The implementation of replica loops with the arguments State, the state, and Mod, the callback module.

Implementation of the client interface functions:

start(NumReplica, Mod): The function in the implementation works by calling the init() function in the given callback module. If it is succesfull, then {ok, State} is returned from init(). It then creates a new process, the coordinator with an enmpty Pids list, then sends a message to the newly created coordinator to spawn replicas corresponding to NumReplica with the Mod as its callback module and returned {ok, ServerRef}. If NumReplica is less than 2, an error occurs as the implementation uses one replica as a dedicated writer (the first one). If some error should occur in init(), then {error, Reason} is returned.

stop(Server): The function sends a message to the coordinator to shutdown all replica and itself. If successfull, then {ok, stopped} is returned. It has not been implemented that all clients get the error message {'ABORTED', server_stopped} if they are waiting for a read or write.

read(Server, Req): The function sends a message to the coordinator directly (non-blocking) with some read request Req. The implementation supports an answer which is a successfull read request, a stop request or if the callback function has made a throw exception.

write (Server, Req): The function sends a message to the auxillary function Blocking with some write request Req. The implementation supports an answer which is a successfull write request (both when an update is made to the state and when not), a stop request or if the callback function has made a throw exception.

Implementation of the coordinator and the replica

coordinator(Pids): The coordinator is the one that keep track of what happens. It initiates tasks for the *replica*. In the implementation it can match on the following messages:

- make_Replicas, a call from start that creates the replicas with the auxillary function createReplica which return a list of tuples which contain the process ID's and their status (free or busy, but this was used in the implementation).
- \bullet $\tt getPids$ which returns the list $\tt Pids$ only used for testing purposes.
- stop, which makes the coordinator send a message to all replicas with the message stop. When this happens, the server does not call itself and therefore dies.
- read, which picks a random reader in the interval [2..NumReplica] of Pids and assigns that replica to the read request. The original purpose was the make it find a process which was "free" (status in the tuple) and assign the request to that, but as this was not implemented, it was made randomized instead, so we do not pick the same over and over again. Note that it cannot pick the first element in the list as this is the dedicated writer.
- write, which assigns the write request to the first process in Pids.
- update, should the callback function handle_write return with a new state, the replica sends this message to the coordinator, which then sends a message to all replica with the new state.

replica(State, Mod): This function is the "worker", the one that actually performs the requests by calling the callback functions. It can match on the following messages:

- stop, if it gets this message, it will return stopped, self() and simply not loop and thus, dies.
- read, which calls the callback function handle_read. It then tries to match one of 2 cases: {reply, Reply or stop. If it gets the reply message, it send the term Reply back to the caller (the read function). If it gets the stop message, it sends this back and instruct the caller to call the stop function. If the callback function should throw an exception, it returns the value given by throw back.

• write, which calls the callback function handle_write. It then tries to match one of 3 cases: {noUpdate, Reply}, {updated, Reply, NewState} or stop. If it gets the noUpdate message, it simply returns the term Reply to the caller (as in read). If it gets the updated message, it will instruct the coordinator to update states (with the update message) in all replicas and returns the reply to the write function along with the new state. If it gets stop, it instructs the caller to call the stop function. It also matches a throw exception as read does.

3.2 Testing

To test the implementation, a module callback mod which can be seen in appendix C.1 was made. The idea is that it is a simple callback module, which an array is used as the state. We can then test the implementation by invoke the returns as specified in the implementation to see if they behave as intended. The idea is our initial state is an array containing the number from 1 to 9. Our request, Req, is defined by number which is treated as an index.

As such, the handle_read callback reads the number on the index Req in the state and returns the state. Otherwise it can return stop (in which case {ok, stopped} is returned and all servers are shut down. It can also make the throw exception.

The handle_write works in the same manner with stop and throw exceptions. The request is also an index, but it replaces the value on that index with 99 (always). It can return {noUpdate, Reply} (even though an update is made) where the Reply is the new state. It can return {updated, Reply, NewState} in which case it returns the old state in Reply and the new state in NewState.

The tests and the output can be seen in appendix C.2, where each return from the callback module is handled correctly. There are descriptions to each test, though "Test 2" is probably the most interesting one as it shows we correctly spawn 5 replicas with the correct state and that a write request is updated on all other servers.

3.3 Assessment

I know the testing is a bit laid back. But the tests all provide correct answer for all the different returns, which is actually quite exstensive as a lot of the edge cases lies in how the request is handlede which is not in the scope for this question.

It does lack the functionality (and testing) for concurrent read and write requests, but since the implementation was not fully completed, it was not completed. It did have the functionality to find a process that was not busy (the function findAvailable which is outcommented in the source code), but I did not get to implement the rest.

I think the solution lacks the last features, but the implementation that was done is correct.

4 AlzheimerDB

This implementation does not work, but I will go through what I have done so far. It is using gen_server. The source code can be found in E.4

4.1 Implementation

start: This is simply a call to start/3 from gen_server. This results in the callback function init/1 which in the implementation returns {ok, dict:new()} where the dictionary is out State.

query: This is a call to <code>gen_server</code>'s <code>call/2</code> where the request is <code>{read, P}</code> where P is a function. This results in the callback function <code>handle_call/3</code>. The idea was that it calls the auxillary function <code>filterWithError</code> which returns the list of <code>{Key, Value}</code> pairs in the dictionary (made into an array using <code>dict:to_list</code>) than returned true when P was applied on them. If an exception was thrown, we put that a <code>{error, Row}</code> in the front of the list that was returned, so we'd know whether to return the error or <code>{ok, Rows}</code>. This was also why I could not just use the filter function as it did not handle thrown exceptions.

upsert: This also called gen_server's call/2 with the request {write, Id, F} where F is a function. It would then look up the identifier Id in the dictionary using dict:find. If it existed, we call the

function F on the argument {existing, {Id, Value}} - Where Value is returned from dict:find). If the did not exists we call F on {new, Id}.

This function F can return {modify, NewData} (does not matter if there was a key or not) in which case we insert/replace the value under the Id with the value in NewData. This works with the function dict:store. This returns {modify, NewData}.

It could also return ignore, in which case we do nothing and return ignore.

In case F makes an exception, this is also what should be returned.

I could not finish the task due to time restraints.

A Parser

]

$\mathbf{A.1}$ intro.js The abstract syntax tree produced by the parser for intro.js Prog [VarDecl "xs" (Just (Array [Number 0, Number 1, Number 2, Number 3, Number 4, Number 5, Number 6, Number 7, Number 8, Number 9])), VarDecl "squares" (Just (Compr ("x", Var "xs", Nothing) (Call "*" [Var "x", Var "x"]))), VarDecl "evens" (Just (Compr ("x", Var "xs", Just (ArrayIf (Call "===" [Call "%" [Var "x", Number 2], Number 0]) Nothing)) (Var "x"))), VarDecl "many_a" (Just (Compr ("x", Var "xs", Just (ArrayForCompr ("y",Var "xs",Nothing))) (String "a"))), VarDecl "hundred" (Just (Compr ("i", Array [Number 0], Just (ArrayForCompr ("x", Var "xs", Just (ArrayForCompr ("y",Var "xs",Nothing))))) (Assign "i" (Call "+" [Var "i", Number 1]))))] The handed out abstract syntax tree for intro.js Prog [VarDecl "xs" (Just (Array [Number 0, Number 1, Number 2, Number 3, Number 4, Number 5, Number 6, Number 7, Number 8, Number 9])), VarDecl "squares" (Just (Compr ("x", Var "xs", Nothing) (Call "*" [Var "x", Var "x"]))), VarDecl "evens" (Just (Compr ("x", Var "xs", Just (ArrayIf (Call "===" [Call "%" [Var "x", Number 2], Number 0]) Nothing)) (Var "x"))), VarDecl "many_a" (Just (Compr ("x", Var "xs", Just (ArrayForCompr ("y",Var "xs", Nothing))) (String "a"))), VarDecl "hundred" (Just (Compr ("i", Array [Number 0], Just (ArrayForCompr ("x", Var "xs", Just (ArrayForCompr ("y", Var "xs", Nothing)))))

(Assign "i" (Call "+" [Var "i", Number 1]))))

B Interpreter

B.1 simpleProg.js

```
The program simlpeProg.js:
```

```
var a = 3+3*2;
1
2
     a = a-4\%3;
     b = a === 8;
     c = 'c' === 'd';
4
5
     var d = true === 2 < 4;
6
     e = 'ab' < 'ba';
7
     f = 'cab' < 'ba';
8
     g = 4 \% 2 < 3;
     h = 4 < 3;
9
10
     var i = 'i';
11
     i = i + 2 * 3;
    var j = 2 + 'j';
12
     k = [3, 2, 2\%2];
13
14
     var 1;
     var m = 'a' + 'b';
```

This is the output of running the program simpleProg.js with the command: "runhaskell Subs.hs tests/simpleProg.js" from the ./src folder.

```
a = 8
b = true
c = false
d = true
e = true
f = false
g = true
h = false
i = "i6"
j = "2j"
k = [3, 2, 0]
1 = undefined
m = "ab"
```

B.2 Errors

Errors than can be generated by the interpreter.

```
$ runhaskell Subs.hs tests/intrp_invalidVar
Subs.hs: Error "Key does not exist in 'getVar'"

$ runhaskell Subs.hs tests/intrp_isEqualBadTypes
Subs.hs: Error "Bad argument types in '==='"

$ runhaskell Subs.hs tests/intrp_lessThanBadTypes
Subs.hs: Error "Bad argument types in '<'"

$ runhaskell Subs.hs tests/intrp_minusBadTypes
Subs.hs: Error "Both operators must be in '-'"

$ runhaskell Subs.hs tests/intrp_moduloBadTypes
Subs.hs: Error "Both operator must be integers in '%'"

$ runhaskell Subs.hs tests/intrp_multiplyBadTypes
Subs.hs: Error "Both operators must be integers in '*'"</pre>
```

\$ runhaskell Subs.hs tests/intrp_plusBadTypes
Subs.hs: Error "Bad argument types in '+'"

C Generic Replicated Server Library

C.1

callback_mod

```
-module(callback_mod).
-export([init/0, handle_read/2, handle_write/2]).

init() ->
% {error, something_went_wrong}.
{ok, [1,2,3,4,5,6,7,8,9]}.

handle_read(Req, State) ->
% throw(something_happened).
% stop.
{reply, lists:nth(Req, State)}.

handle_write(Req, State) ->
% throw(something_happened).
% stop.
% throw(something_happened).
% stop.
% throw(something_happened).
% stop.
% foulpdate, lists:sublist(State, Req-1) ++ [99] ++ lists:nthtail(Req, State)}.
{updated, State, lists:sublist(State, Req-1) ++ [99] ++ lists:nthtail(Req, State)}.
```

C.2 Testing

```
%%%%%%% TEST 1 %%%%%%%
% Test if the error in init is handled correctly
1> c(gen_replicated).
{ok,gen_replicated}
2> c(callback_mod).
{ok,callback_mod}
3> {_, P1} = gen_replicated:start(5, callback_mod).
{error, something_went_wrong}
%%%%%%% TEST 2 %%%%%%%
% Test to see if handle_write (which returns updated) actually updates on all servers.
% That means the read requests should return the initial state with the change.
% Furthermore we test that 5 replpicas are actually made.
1> c(gen_replicated).
{ok,gen_replicated}
2> c(callback_mod).
{ok,callback_mod}
3> {_, P1} = gen_replicated:start(5, callback_mod).
\{ok, <0.47.0>\}
4> gen_replicated:write(P1, 4).
\{ok, [1,2,3,4,5,6,7,8,9], [1,2,3,99,5,6,7,8,9]\}
5> gen_replicated:read(P1, 4).
{ok,99}
6> gen_replicated:read(P1, 5).
\{ok, 5\}
7> gen_replicated:get_pids(P1).
{ok,[{<0.48.0>,free},
     {<0.49.0>,free},
     {<0.50.0>,free},
     {<0.51.0>,free},
     {<0.52.0>,free}]}
%%%%%%% TEST 3 %%%%%%%
% Test to see if handle_write (which now returns noUpdate) work.
% This is seen by the return from handle_read.
1> c(gen_replicated).
```

```
{ok,gen_replicated}
2> c(callback_mod).
{ok,callback_mod}
3> {_, P1} = gen_replicated:start(5, callback_mod).
\{ok, <0.47.0>\}
4> gen_replicated:write(P1, 4).
{ok,[1,2,3,99,5,6,7,8,9]}
5> gen_replicated:read(P1, 4).
\{ok, 4\}
%%%%%% TEST 4 %%%%%%%
% Test to see if the stop returned from handle_read stops the servers,
% but handle_write (which sends updated) still works.
1> c(gen_replicated).
{ok,gen_replicated}
2> c(callback_mod).
callback_mod.erl:8: Warning: variable 'Req' is unused
callback_mod.erl:8: Warning: variable 'State' is unused
{ok,callback_mod}
3> {_, P1} = gen_replicated:start(5, callback_mod).
\{ok, <0.47.0>\}
4> gen_replicated:write(P1, 4).
\{ok, [1,2,3,4,5,6,7,8,9], [1,2,3,99,5,6,7,8,9]\}
5> gen_replicated:write(P1, 3).
{ok,[1,2,3,99,5,6,7,8,9],[1,2,99,99,5,6,7,8,9]}
6> gen_replicated:read(P1, 3).
{ok,stopped}
%%%%%%% TEST 5 %%%%%%%%
% Test to see if the throw returned by handle_read works,
% while the write requests still works.
1> c(gen_replicated).
{ok,gen_replicated}
2> c(callback_mod).
callback_mod.erl:8: Warning: variable 'Req' is unused
callback_mod.erl:8: Warning: variable 'State' is unused
{ok,callback_mod}
3> {_, P1} = gen_replicated:start(5, callback_mod).
\{ok, <0.47.0>\}
4> gen_replicated:write(P1, 4).
\{ok, [1,2,3,4,5,6,7,8,9], [1,2,3,99,5,6,7,8,9]\}
5> gen_replicated:re
read/2
           replica/2
5> gen_replicated:read(P1, 3).
{'ABORTED', exception, something_happened}
%%%%%%% TEST 6 %%%%%%%%
% Test to see if the stop returned from handle_write works,
% while the read requests still work.
1> c(gen_replicated).
{ok,gen_replicated}
2> c(callback_mod).
callback_mod.erl:13: Warning: variable 'Req' is unused
callback_mod.erl:13: Warning: variable 'State' is unused
{ok,callback_mod}
```

```
3> {_, P1} = gen_replicated:start(5, callback_mod).
\{ok, <0.47.0>\}
4> gen_replicated:read(P1, 4).
\{ok,4\}
5> gen_replicated:read(P1, 3).
\{ok,3\}
6> gen_replicated:write(P1, 3).
{ok,stopped}
%%%%%%% TEST 7 %%%%%%%
\mbox{\ensuremath{\%}} Test to see if the throw returned from handle_write works,
% while the read requests still work.
1> c(gen_replicated).
{ok,gen_replicated}
2> c(callback_mod).
callback_mod.erl:13: Warning: variable 'Req' is unused
callback_mod.erl:13: Warning: variable 'State' is unused
{ok,callback_mod}
3> {_, P1} = gen_replicated:start(5, callback_mod).
\{ok, <0.47.0>\}
4> gen_replicated:read(P1, 4).
\{ok,4\}
5> gen_replicated:write(P1, 4).
{'Aborted', exception, something_happened}
```

D Unit Tests

D.1 ParserTest.hs

```
module ParserTest where
import Test.HUnit
import SubsParser
precedence2AST :: String precedence2AST = "Right (Prog [ExprAsStm (Call \"===\" [Call \"+\" [Number 7, Number 42], Call \leftarrow \"<\" [Number 12, Number 99]])]"
reservedIdents :: String reservedIdents = "Left \"Parsing error\" (line 1, column 8):\nunexpected illegal identifier"
introTest :: Test
testSucc1 :: Test
\texttt{testSucc1} = \texttt{TestCase} \hspace{0.1cm} (\texttt{do} \hspace{0.1cm} \texttt{parsedFile} \hspace{0.1cm} \leftarrow \hspace{0.1cm} \texttt{parseFile} \hspace{0.1cm} "\hspace{0.1cm} \texttt{tests}/\texttt{funName}"
                        assertEqual "funName and array test" funNameAST $ show parsedFile)
testSucc2 :: Test
\label{eq:testSucc2} \begin{array}{lll} \texttt{testSucc2} = \texttt{TestCase} & \texttt{(do parsedFile} < -\texttt{parseFile} "\texttt{tests/precedence1}" \\ & \texttt{assertEqual} "+ / - / * / \% \ \texttt{precedence} \ \texttt{test"} \\ & \texttt{precedence1AST} \$ \ \texttt{show} \ \texttt{parsedFile}) \end{array}
testSucc3 :: Test
< precedence
                         assertEqual
                                     precedence2AST $ show parsedFile)
testSucc4 :: Test
testSucc4 = TestCase (do parsedFile <- parseFile "tests/associativity" assertEqual "'=' associativity test"
                                         associativity
                                      associativityAST $ show parsedFile)
testSucc5 :: Test
{\tt testSucc5 = TestCase \ (do \ parsedFile <- \ parseFile \ "tests/allowedIdents" \\ assertEqual \ "allowed \ idents \ (using \ '-') \ test"}}
                                      "allowed idents (using '_') test"
allowedIdentsAST $ show parsedFile)
testSucc6 :: Test
testSucc6 = TestCase (do parsedFile <- parseFile "tests/illegalIdents" assertEqual "illegal ident starting with digit"
                                      illegalIdents $ show parsedFile)
testSucc7 :: Test
testSucc7 = TestCase (do parsedFile <- parseFile "tests/reservedIdents" assertEqual "reserved ident"
```

E Source Code

E.1 SubsParser.hs

```
module SubsParser (
  parseString,
  parseFile
) where
import SubsAst as S
import Text.Parsec import Text.Parsec.String
import Control. Monad
import Data.Functor.Identity
deriving (Show, Eq)-}
whitespace :: Parser ()
whitespace = void $ many $ oneOf " \n^n \t^n
lexeme :: Parser a -> Parser a
lexeme p = do
            x <- p
             whitespace
             return x
 - Reserved
reserved :: [String]
reserved = ["var", "true", "false", "undefined", "for", "of", "if"]
  - Ident implementation
ident :: Parser String ident = do
      s1 <- letters
       s2 <- many letDigs return (s1:s2)
     where
       letters = oneOf $ ['a'..'z'] ++ ['A'..'Z'] ++ "_"
letDigs = oneOf $ ['a'..'z'] ++ ['A'..'Z'] ++ "_" ++ ['0'..'9']
identParse :: Parser String
else return n
-- Grammar Implementation
prog :: Parser Program
prog = do
p <- stms
_ <- eof
      return (Prog p)
stms :: Parser [Stm]
stms = try stms1 < | > try stms2
stms1 :: Parser [Stm]
stms1 = do
      s1 <- lexeme stm
void $ lexeme $ char ';'</pre>
       s2 <- lexeme stms
       return (s1:s2)
stms2 :: Parser [Stm]
stm :: Parser Stm
\mathtt{stm} \ = \ \mathtt{try} \ \mathtt{varDecl} \ <| > \ \mathtt{try} \ \mathtt{exprAsStm}
varDecl :: Parser Stm
varDecl = try varDecl1 < | > try varDecl2
varDecl1 :: Parser Stm
varDecl1 = do
      void $ lexeme $ string "var"
iden <- lexeme identParse
a1 <- lexeme assignOpt
       return (VarDecl iden (Just a1))
\begin{array}{lll} {\tt varDecl2} & :: & {\tt Parser} & {\tt Stm} \\ {\tt varDecl2} & = & {\tt do} \end{array}
   void $ lexeme $ string "var"
```

```
iden <- lexeme identParse
        return (VarDecl iden Nothing)
 assignOpt :: Parser Expr
 assignOpt = do
        void $ lexeme $ char '='
        e1 <- lexeme expr
        return e1
 exprAsStm :: Parser Stm
 exprAsStm = do
      e1 <- lexeme expr
        return (ExprAsStm e1)
 expr :: Parser Expr
 \mathtt{expr} \; = \; \mathtt{try} \; \; \mathtt{exprExt} \; \; <|> \; \mathtt{try} \; \; \mathtt{exprEnd}
 exprExt :: Parser Expr
 exprExt = do
       e1 <- lexeme expr1
        void $ lexeme $ char ','
        e2 <- lexeme expr
        return (Comma e1 e2)
 exprEnd :: Parser Expr
exprEnd = lexeme expr1
   - Precedence for expressions
expr1 :: Parser Expr
expr1 = do
        rv <- r
        botbot rv
 botbot inval = do void $ lexeme $ string "===""
        rv <- r
        botbot (Call "==" [inval, rv])
   <|> return inval
\texttt{r} \ :: \ \texttt{ParsecT} \ \ \underline{\textbf{String}} \ \ () \ \ \texttt{Data}. \\ \underline{\textbf{Functor}}. \\ \underline{\textbf{Identity}}. \\ \underline{\textbf{Identity}} \ \underline{\textbf{Expr}}
r = do
        bot sv
bot inval = (do void $ lexeme $ char '<'
        sv <- s
        bot (Call "<" [inval, sv]))
   <|> return inval
s :: ParsecT String () Data.Functor.Identity.Identity Expr
s = do
        tv <- t
        mid tv
 mid :: Expr -> ParsecT String () Data.Functor.Identity.Identity Expr
mid inval = (do void $ lexeme $ char '+'
        tv <- t
        mid (Call "+" [inval, tv]))
   <|> (do
        void $ lexeme $ char '-'
        mid (Call "-" [inval, tv]))
   <|> return inval
{\tt t} \; :: \; {\tt ParsecT} \; \; {\tt String} \; \; () \; {\tt Data.Functor.Identity.Identity} \; {\tt Expr}
 t = do
       pv <- prim
        top pv
\texttt{top} \ :: \ \texttt{Expr} \ -\!\!\!\!> \ \texttt{ParsecT} \ \ \underbrace{\textbf{String}} \ \ () \ \ \texttt{Data} \, . \\ \ \ \textbf{Functor} \, . \, \texttt{Identity} \, . \, \texttt{Identity} \, \, \texttt{Expr}
top inval = (do void $ lexeme $ char '*'
        pv <- prim
        top (Call "*" [inval, pv]))
   <|> (do
        void $ lexeme $ char '%'
        <|> return inval
-- Try expressions prim :: Parser Expr
| \ \mathtt{prim} \ = \ \mathtt{try} \ \ \mathtt{number} \ <|> \ \mathtt{try} \ \ \mathtt{trueConst} \ <|> \ \mathtt{try} \ \ \mathtt{falseConst} \ <|> \ \mathtt{try} \ \ \mathtt{undef}
```

```
<|> try exprString <|> try array <|> try exprIdent <|> try parentheses
number :: Parser Expr
number = do
        d <- lexeme $ many1 digit
return (Number (read d))</pre>
exprString :: Parser Expr
\mathtt{exprString} \, = \, \frac{do}{}
          spaces
         void \ char ' \setminus ' '
         ss <- many1 letter void $ char '\''
         spaces
         return (String ss)
\begin{array}{lll} array & :: & Parser & Expr \\ array & = & try & array1 & <|> & try & array2 \end{array}
array1 :: ParsecT String () Identity Expr
array1 = do
         void $ lexeme $ char '['
         e1 <- lexeme exprs
void $ lexeme $ char ']'
return (Array e1)
array2 :: Parser Expr
array2 = try array3 < | > try array4
array3 :: Parser Expr
array3 = do
         void $ lexeme $ char '['
void $ lexeme $ string "for"
void $ lexeme $ char '('
         iden1 <- lexeme identParse
void $ lexeme $ string "of</pre>
         e1 <- lexeme expr
void $ lexeme $ char ')'
         a1 <- lexeme arrayCompr
e2 <- lexeme expr
void $ lexeme $ char ']'
return (Compr (iden1, e1, Just a1) e2)
array4 :: Parser Expr
array4 = do
         void $ lexeme $ char '['
void $ lexeme $ string "for"
void $ lexeme $ char '('
iden2 <- lexeme identParse
void $ lexeme $ string "of"</pre>
         e1 <- lexeme expr
void $ lexeme $ char ')'
         e2 <- lexeme expr
void $ lexeme $ char ']'
return (Compr (iden2, e1, Nothing) e2)
parentheses :: Parser Expr
parentheses = do
         void $ lexeme $ char '('
         e1 <- lexeme expr
void $ lexeme $ char ')'
         return e1
undef :: Parser Expr
undef = do
         void $ lexeme $ string "undefined" return Undefined
trueConst :: Parser Expr
trueConst = do
         void $ lexeme $ string "true" return TrueConst
falseConst :: Parser Expr
falseConst = do
         void $ lexeme $ string "false"
          return FalseConst
exprIdent :: Parser Expr
exprIdent = do
        spaces
          iden <- lexeme identParse
         afterIdent iden
\begin{array}{lll} {\tt afterIdent} & :: & {\tt Ident} & -{\tt >} & {\tt Parser} & {\tt Expr} \\ {\tt afterIdent} & {\tt iden} & = & {\tt try} & ({\tt afterIdent1} & {\tt iden}) \\ & & <|{\tt >} & {\tt try} & ({\tt funCall} & {\tt iden}) \end{array}
```

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```
<|> return (Var iden)
afterIdent1 :: Ident -> Parser Expr
{\tt afterIdent1 \ iden = \ do}
       spaces
        void $ lexeme $ char '='
        e1 <- lexeme expr1
        return (Assign iden e1)
funCall newId
funCall2 :: FunName -> ParsecT String () Identity Expr
funCall2 iden = do
       void $ lexeme $ char '('
        e1 <- lexeme exprs
       void $ lexeme $ char ') '
return (Call iden e1)
exprs :: Parser [Expr]
exprs = expr1 `sepBy` lexeme (char ',')
\label{eq:arrayCompr} \begin{array}{lll} \texttt{arrayCompr} & :: & \texttt{Parser ArrayCompr} \\ \texttt{arrayCompr} & = & \texttt{try for1} < |> & \texttt{try for2} < |> & \texttt{try if1} < |> & \texttt{try if2} \\ \end{array}
for1 :: Parser ArrayCompr
for1 = do
       void $ lexeme $ string "for"
void $ lexeme $ char '('
       iden <- lexeme identParse
void $ lexeme $ string "o
              <- lexeme expr
        void $ lexeme $ char ') '
a1 <- lexeme arrayCompr
       for2 :: Parser ArrayCompr
for2 = do
       void $ lexeme $ string "for"
        void $ lexeme $ char
       iden <- lexeme identParse
void $ lexeme $ string "of"</pre>
        e1 <- lexeme expr
void $ lexeme $ char ')'
        return (ArrayForCompr (iden, e1, Nothing))
if1 :: Parser ArrayCompr
if1 = do
       do void $ lexeme $ string "
        e1 <- lexeme expr
void $ lexeme $ char ')'
        a1 <- lexeme arrayCompr
        return (ArrayIf e1 (Just a1))
if2 :: Parser ArrayCompr
       void $ lexeme $ string "if" void $ lexeme $ char '('
        void $ lexeme $ char
       e1 <- lexeme expr
void $ lexeme $ char ')'
return (ArrayIf e1 Nothing)
\begin{array}{lll} \texttt{parseString} & :: & \texttt{String} \rightarrow & \texttt{Either} & \texttt{ParseError} & \texttt{Program} \\ \texttt{parseString} & = & \texttt{runParser} & \texttt{prog} & () & "\texttt{Parsing} & \texttt{error}" \end{array}
parseFile :: FilePath -> IO (Either ParseError Program)
{\tt parseFile\ path\ =\ fmap\ parseString\ \$\ readFile\ path}
```

E.2 SubsInterpreter.hs

```
module SubsInterpreter
           ( runProg
           , Error (..)
import SubsAst
   You might need the following imports
import Control. Monad
import Control.Applicative as App
import qualified Data. Map as Map
import Data.Map(Map)

- | A value is either an integer, the special constant undefined,
- true, false, a string, or an array of values.
- Expressions are evaluated to values.

--- ^ Any runtime error. You may add more constructors to this type
--- (or remove the existing ones) if you want. Just make sure it is
--- still an instance of 'Show' and 'Eq'.
data Value = IntVal Int
                 | UndefinedVal
                  TrueVal | FalseVal
StringVal String
                | ArrayVal [Value]
| deriving (Eq. Show)
data Error = Error String
  deriving (Show, Eq)
	ext{type} Env = Map Ident Value
type Primitive = [Value] -> SubsM Value
type PEnv = Map FunName Primitive
type Context = (Env, PEnv)
\verb"initialContext":: Context"
{\tt initialContext} \, = \, (\, {\tt Map.empty} \, \, , \, \, \, {\tt initialPEnv} \, )
   where initialPEnv =
               Map.fromList [ ("===""
                                                . isEqual)
                                   [ ( == , isEqual
, ("<", lessThan)
, ("+", plus)
, ("*", multiply)
, ("-", minus)
, ("%", modulo)
("Array new"
                                      ("Array.new", arrayNew)
newtype SubsM a = SubsM {runSubsM :: Context -> Either Error (a, Env)}
instance Functor SubsM where
fmap = Control.Monad.liftM
instance App. Applicative SubsM where
   (<*>) sf s = sf >>= \f -> fmap f s
- Initial Context
arrayNew :: Primitive arrayNew [IntVal n] | n > 0 = return $ ArrayVal(replicate n UndefinedVal) arrayNew _ = fail "Array.new called with wrong number of arguments"
isEqual :: Primitive
isEqual [IntVal e1, IntVal e2]
                                                        = return (if e1 == e2 then TrueVal
                                                        else FalseVal)
isEqual [StringVal e1, StringVal e2] = return (if e1 == e2 then TrueVal
                                                        else FalseVal)
\verb|isEqual| [TrueVal|, FalseVal|]
                                                        = return FalseVal
isEqual [FalseVal, TrueVal] isEqual [TrueVal, TrueVal] isEqual [FalseVal, FalseVal]
                                                        = return FalseVal
                                                       = return TrueVal
= return TrueVal
                                                       = fail "Bad argument types in '==='"
isEqual _
lessThan :: Primitive
lessThan [IntVal e1, IntVal e2]
                                                        = return (if e1 < e2 then TrueVal
                                                         else FalseVal)
{\tt lessThan} \ [\, {\tt StringVal} \ \ {\tt e1} \, , \ \ {\tt StringVal} \ \ {\tt e2} \, ] \ = \ {\tt return} \ \ (\, {\tt if} \ \ {\tt e1} \, < \, {\tt e2} \, \ {\tt then} \ \ {\tt TrueVal} \,
```

```
else FalseVal)
lessThan _
                                                  = fail "Bad argument types in '<'"
plus :: Primitive
plus :: Frimitive

plus [IntVal e1, IntVal e2] = return $ IntVal (e1 + e2)

plus [StringVal e1, StringVal e2] = return $ StringVal (e1 ++ e2)

plus [StringVal e1, IntVal e2] = return $ StringVal (e1 ++ show e2)

plus [IntVal e1, StringVal e2] = return $ StringVal (show e1 ++ e2)
                                            = fail "Bad argument types in '+
plus _
minus :: Primitive
minus [IntVal e1, IntVal e2] = return  IntVal (e1 - e2) minus _ = fail "Both operators must be in '-'"
modulo :: Primitive
modulo [IntVal e1, IntVal e2] = return $ IntVal (e1 'mod' e2)
modulo _ = fail "Both operator must be integers in '%'"
-- End initial Context
-- Utility Functions getEnv :: SubsM Env
getEnv = SubsM ((env, _) \rightarrow Right (env, env))
modify :: (Env -> Env) -> SubsM ()
modify f = do
    env <- getEnv</pre>
  putEnv (f env)
putEnv (Map.insert name val env)
getVar :: Ident -> SubsM Value
getVar name = do
  \mathtt{env} <\!\!- \ \mathtt{getEnv}
  case Map.lookup name env of
    Just a -> return a

Nothing -> fail "Key does not exist in 'getVar'"
{\tt getFunction} \ :: \ {\tt FunName} \ -\!\!\!\!> \ {\tt SubsM} \ {\tt Primitive}
{\tt getFunction\ name\ =\ } \frac{{\tt do}}{{\tt do}}
  penv <- getPEnv
case Map.lookup name penv of
     Just a -> return a
Nothing -> fail "Key does not exist in 'getFunction'"
-- End Utility Functions
  Expr and Stms Evaluation
= return $ IntVal n
= return $ StringVal s
= do
evalExpr (String s)
evalExpr (Array arr)
 a <- arrEval arr
return $ ArrayVal a
evalExpr (TrueConst)
evalExpr (FalseConst)
                                      = return TrueVal
                                    = return TrueVal
= return FalseVal
= return UndefinedVal
= getVar iden
evalExpr (Undefined)
evalExpr (Var iden)
evalExpr (Compr _ _)
evalExpr (Call f arr)
fun <- getFunction f
                                      = undefined
                                      = do
  a <- arrEval arr
 fun a
evalExpr (Assign iden e1)
                                      = do
  e <- evalExpr e1
updateEnv iden e
return e
evalExpr (Comma e1 e2)
                                      = do
        evalExpr e1
  evalExpr e2
\verb|arrEval| :: [Expr]| -> SubsM [Value]
```

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E.3 gen_replicated.erl

```
-module(gen_replicated)
-\operatorname{export}([\operatorname{start}/2, \operatorname{stop}/1, \operatorname{read}/2, \operatorname{write}/2, \operatorname{coordinator}/1, \operatorname{replica}/2, \operatorname{get\_pids}/1]).
case Mod:init() of {ok, _} -
                                    \rightarrow ServerRef = spawn_link(fun() \rightarrow coordinator([]) end),
                                          ServerRef ! {make_replicas, NumReplica, Mod},
                                          {ok, ServerRef};
        {error, Reason} -> {error, Reason}
    end.
stop(Server) ->
   Server ! \{self(), stop\},
    receive
       \{ stopped, \_ \} \longrightarrow \{ ok, stopped \}
\begin{array}{lll} \texttt{read}\,(\,\texttt{Server}\;,\;\; \texttt{Req}\,)\; -\!\!\!> \\ & \texttt{Server}\; !\;\; \{\,\texttt{self}\,(\,)\;,\;\; \{\,\texttt{read}\;,\;\; \texttt{Req}\,\}\,\}\;, \end{array}
        \{ok, Result\} \rightarrow \{ok, Result\};
        end.
write (Server, Req)
   blocking (Server, Req).
get_pids(Server) ->
    Server ! { self(), getPids},
    receive
        \{ok, Pids\} \rightarrow \{ok, Pids\}
%Helper Functions
blocking(Server, Req) ->
Server ! {self(), {write, Req}},
    receive
         \begin{array}{lll} \left\{ok\,,\; \text{Reply}\right\} & \longrightarrow & \left\{ok\,,\; \text{Reply}\right\}; \\ \left\{ok\,,\; \text{Reply}\,,\; \text{NewState}\right\} & \longrightarrow & \left\{ok\,,\; \text{Reply}\,,\; \text{NewState}\right\}; \end{array} 
                                               -> stop(Server);
        stop
        {throw, Val}
                                              -> { 'Aborted', exception, Val}
createReplica(NumReplica, _) when NumReplica == 0 -> []; createReplica(NumReplica, Mod) ->
    {_, State} = Mod:init(),
ReplicaRef = spawn_link(fun() -> replica(State, Mod) end),
[{ReplicaRef, free} | createReplica(NumReplica-1, Mod)].
\label{eq:model} \begin{array}{ll} \% find A\, vailable\, (N,\ \_) \ \ when \ N == \ 1 \ -\!\!\!> \ fail\, ; \\ \% find A\, vailable\, (N,\ Pids) \ -\!\!\!> \end{array}
% case element(2, lists:nth(N, Pids)) of

% free -> element(1, lists:nth(N, Pids));
      free -> element(1,
        busy -> findAvailable(N-1, Pids)
%Coordinator and Replicas
coordinator(Pids) -
    receive
       {make_replicas, NumReplica,
          {\tt NewPids} \ = \ {\tt createReplica} \, (\, {\tt NumReplica} \, , \ {\tt Mod} \, ) \, ,
           coordinator(NewPids);
       From, {read, Req}} ->
Reader = element(1, lists:nth(1+random:uniform(length(Pids)-1), Pids)),
Reader ! {From, {read, Req}},
coordinator(Pids);
        \{From, \{write, Req\}\}
           \label{eq:Reader} \begin{array}{ll} \texttt{Reader} = \underbrace{\mathsf{element}}(1), \; \texttt{lists:nth}(1), \; \texttt{Pids})) \,, \\ \texttt{Reader} \; ! \; \left\{ \underbrace{\mathsf{self}}(), \; \texttt{From} \,, \; \left\{ \texttt{write} \,, \; \texttt{Req} \right\} \right\}, \\ \texttt{coordinator}(\texttt{Pids}) \,; \end{array}
        {update, NewState} ->
Msg = {update, NewState},
            [element(1, Replica) ! Msg || Replica <- Pids],</pre>
            coordinator (Pids);
```

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```
[element(1, Replica) ! Msg || Replica <- Pids]
\tt replica(State\;,\;\;Mod\,)\;\;-\!\!>\;
   -> From ! stop
      catch
       throw : Val \rightarrow From ! \{throw, Val\}
      end;
   {Coordinator, From, {write, Req}} -> try Mod:handle_write(Req, State) of
       -> From ! stop
        stop
      catch
       throw : Val
                                    \rightarrow From ! \{throw, Val\}
      end;
    end;
{update, UpdatedState} ->
replica(UpdatedState, Mod);
{From, stop} ->
From ! {stopped, self()}
  end.
```

E.4 alzheimer

```
-module(alzheimer).
-behavior(gen_server).
-export([start/0, upsert/3, query/2, testFun/1]).
-export([init/1, handle_call/3]).
 -define(SERVER, ?MODULE).
%% API
%%%=
% Client Interface Functions
 start() ->
      gen_server:start_link(?MODULE, [], []).
 query(Aid, P) ->
      gen_server:call(Aid, {read, P}).
 \mathtt{upsert}\,(\,\mathtt{Aid}\;,\;\;\mathtt{Id}\;,\;\;\mathtt{F}\,)\;\;-\!\!>\;
      gen_server:call(Aid, {write, Id, F}).
% Helper Function
 \begin{array}{lll} & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & \\ & & \\ & & \\ & \\ & & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & 
       \mathtt{try} \ \mathtt{P}(\,\mathtt{Elem}\,) \ \mathbf{of}
          true -> filterWithError(P, List, lists:append([Rows, [Elem]]));
false -> filterWithError(P, List, Rows)
      catch
              \_ : \_ -> filterWithError(P, [], lists:append([[{error, element(2, Elem)}], Rows]))
% Callback Functions
init(_Args) ->
     \{ok, dict: new()\}.
 handle_call(Req, From, State) ->
       case Req of
             {read, P} \rightarrow case filterWithError(P, dict:to_list(State), []) of
                                                             \{ \texttt{write} \;,\;\; \texttt{Id} \;,\;\; \texttt{F} \} \; -\!\!\!> \; \underset{}{\texttt{case}} \;\; \texttt{dict:find} (\; \texttt{Id} \;,\;\; \texttt{State} \;) \;\; \underset{}{\texttt{of}} \;\;
                                                                               {modify, NewData};
                                                                                                                                                                                                     -> ignore
                                                                                                                                           ignore
                                                                                                                                          {\bf throw} \; : \; \; {\tt Reason}
                                                                                                                                                                                                     -> throw(Reason)
                                                                                                                         end;
-> try F({new, Id}) of
   {modify, NewData} -> dict:store(Id, NewData, State),
                                                                                 error
                                                                                                                                                                                                                  {modify, NewData};
                                                                                                                                                                                                     -> ignore
                                                                                                                                          ignore
                                                                                                                                    catch
                                                                                                                                         throw : Reason
                                                                                                                                                                                                    -> throw(Reason)
                                                                                                                                    end
                                                                         end
     end.
% Test Functions
 testFun(X) \rightarrow
      case X of
                                                                                   \rightarrow {modify, 99};
          {new, _}
               \{existing, \{\_, \_\}\} \rightarrow ignore
```