# Reliable Neural Network

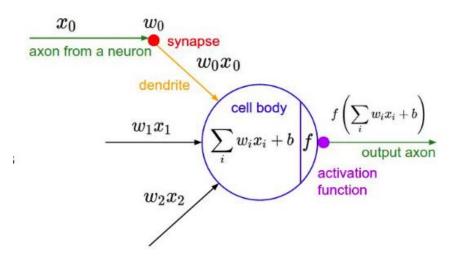
### **Reliability Theory**

Reliability is defined as the probability that a product, system, or service will perform its intended function adequately for a specified period of time, or will operate in a defined environment without failure.

#### Failure:

- According to its specification, it was correct at time t=0.
- At time t, the operation of a system may no longer meet its specification

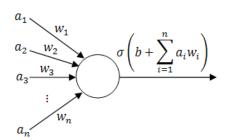
## **Basics of NN**



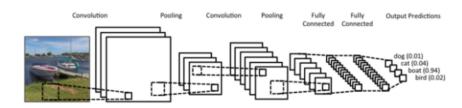
#### Activation function:

- It takes in the output signal from the previous cell and converts it into some form that can be taken as input to the next cell.
- deciding what is to be fired to the next neuron.
- help the network learn complex patterns in the data.
- Introduces nonlinearity

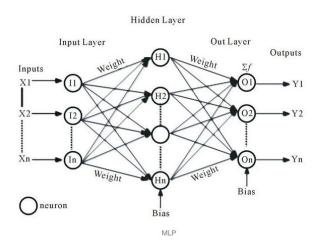
# Types of NN



Simple Perceptron



CNN for image classification



Multi Layer Perceptron

### Distribution

- One of the features of neural network's computation which is a major incentive for their application in solving problems is that of distribution.
- Two distinct forms of this property can be considered to exist:
  - Distributed Information Storage
  - Distributed Processing.
- Distributed processing refers to how every unit performs its own function independently of any other units in the neural network.
- However, correctness of its inputs may be dependant on other units.
- The global recall or functional evaluation performed by the entire neural network results from the joint (parallel) operation of all the units.

## Drawback

- Faults cannot be located easily.
- In an implementation each component would require extra circuitry to detect and signal the occurrence of a fault.
- The cost and reduction in overall reliability of the system might render this approach unsatisfactory.

# Advantage

- However, neural networks also have another important property, they can learn.
- This feature will allow a faulty system, once detected, to be retrained either to remove or to compensate for the faults without requiring them to be located.
- The re-learning process will be relatively fast compared to the original learning time since the neural network will only be distorted by the faults, not completely randomised.

- distributing information across all units within a neural network is also beneficial if the information load on every unit is approximately equivalent.
  - decrease the chance of having critical components which might cause system failure, even if the remainder are free from faults

Generalisation.

This refers to the ability of a neural network which has been trained using a limited set of training data, to supply a reasonable output to an input which it did not encounter during training.

- As an adaptive system, generalisation in a neural network can be considered to represent the underlying problem rather than just memorising the particular inputs in the training set.
- Robustness to noisy inputs in classification systems can be a product of generalisation.

### Local vs. Global Generalisation

 Two distinct computational techniques by which a neural network generalises [identified by considering the nature of the response of internal units to inputs ranging over the input space.]

### Local:

- Some neural networks employ units which only activate for inputs in a limited bounded region of input space, e.g. Radial Basis Function networks.
- An unknown input will only activate those units whose activation regions includes the new input.
- Global: This is where the internal units of a neural network respond to all inputs lying anywhere within the input space.

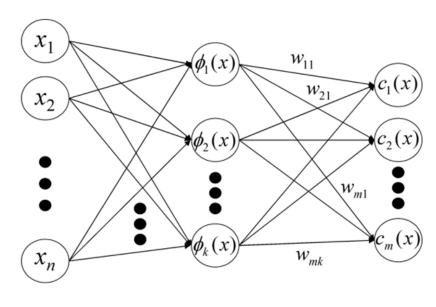
### Radial basis function network (RBF)

Radial basis function network is an artificial neural network that uses radial basis functions as activation functions.

The output of the network is a linear combination of radial basis functions of the inputs and neuron parameters.

Radial basis function networks have many uses, including function approximation, time series prediction etc.

[Universal approximation theorems imply that neural networks can *represent* a wide variety of interesting functions when given appropriate weights.]



Input Layer

Hidden Layer

**Output Layer** 

Radial basis function (RBF) networks typically have three layers: an input layer, a hidden layer with a non-linear RBF activation function and a linear output layer.

The input can be modeled as a vector of real numbers  $\mathbf{x} \in \mathbb{R}^n$ 

The output of the network is then a scalar function of the input vector,  $\varphi(\mathbf{x}) = \sum_{i=1}^{N} a_i \rho(||\mathbf{x} - \mathbf{c}_i||)$ 

Where,  $\varphi: \mathbb{R}^n \to \mathbb{R}$ 

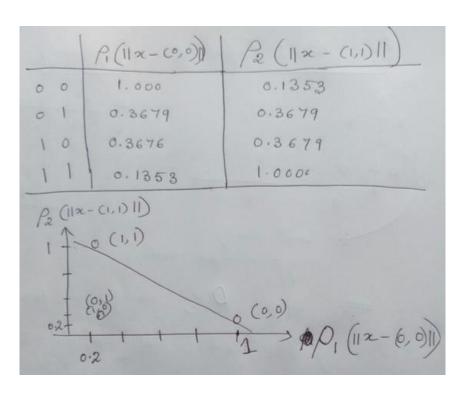
where N is the number of neurons in the hidden layer,  $\mathbf{c}_i$  is the center vector for neuron i, and  $a_i$  is the weight of neuron i in the linear output neuron.

Radial basis function network (RBFN) RBFN is an ANN that use radial Caus functions as activation functions. - only one hidden node separable 000000 L) complex data not linearly -> increasing dimension sefarable et is separable · Consider a centre of the points (or and draw co-centre circles neurous · Draw the radius -> from the centre.

Input: vector of real numbers Outful & Scalor function of the input vector q(x) = Saip (11x-cill) N: Number of neuron, ai = weight. P(11x-cill) = multiquadric/inverse mutequadric Gaussian mostly used P(11x-C:11) = exp [-B: 11x-C:11] lim p (11x-cill) = 0. I input values. for away from centre I has very small effect That implies the local general zation

FOR RBFNN:

Eg: XOR: simplest form of nonlinearity B JAB+AB >. Cannot classify using a simple line -> Apply. P(x) in Gaussian form. P(11x-cill) = exp[-Billx-cill] · Considering Bi=1, Ci=0, p(x) = exp[-x2] > Now, Consider two centres (0,0) and (1) and calculate the distances.



# Why local generalization

The radial basis function is commonly taken to be Gaussian:

$$hoig(\|\mathbf{x}-\mathbf{c}_i\|ig)=\exp\Bigl[-eta_i\|\mathbf{x}-\mathbf{c}_i\|^2\Bigr].$$

The Gaussian basis functions are local to the center vector in the sense that

$$\lim_{||x|| o \infty} 
ho(\|\mathbf{x} - \mathbf{c}_i\|) = 0$$

 Changing parameters of one neuron has only a small effect for input values that are far away from the center of that neuron.

### Generalisation and fault tolerance of a neural network

### If local:

- Unreliable in limited regions of input space.
- Only when an input falls into a region where the neural network's operation is affected will the effect of faults be apparent and possible failure occur.
  - if a large number of extra units are used in a locally generalising neural network, the degree of overlap between the input space regions of each unit can be increased such that a general improvement in fault tolerance will be achieved.

### If Global:

 Global generalisation will cause a small loss of generalisation for any input pattern.