

Define and update preconditioners

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A preconditioner is defined for a bilinear-form, and aims at providing a cheap, approximative inverse of the matrix. The matrix is restricted to the non-dirichlet (free) degrees of freedom, provided by the underlying FESpace.

The canonical way is to define the preconditioner after the bilinear-form, but before calling Assemble:

```
[ ]: a = BilinearForm(fes)
      a += SymbolicBFI(grad(u)*grad(v))
      c = Preconditioner(a, "local")
      a.Assemble()
```

The preconditioner registers itself with the bilinear-form. Whenever the form is updated, the preconditioner is updated as well.

You can define the preconditioner after assembling, but then you have to call manually `c.Update()`

The ratio if this ordering is that some preconditioners (e.g. bddc, amg, ...) require access to the element-matrices, which are only available during assembling.

The preconditioners included in NGSolve are the following. Additional user-defined preconditioners can be implemented in plug-ins. An example is given in MyLittleNGSolve

Name	Preconditioners
local	Jacobi / block-Jacobi
direct	a sparse direct factorization
multigrid	h-version and high-order/low-order multigrid
bddc	p-version domain decomposition