

# QubitCoin Whitepaper v2.0 - Expanded English Version (30-40 Pages)

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## Abstract

This whitepaper presents QubitCoin (QBC), a quantum-resistant cryptocurrency implementing RubikPoW, a proof-of-work algorithm based on the mathematical complexity of the Rubik's Cube group. This document extensively details the architecture, quantum security, technical implementation and economic model of QubitCoin, providing an exhaustive analysis of its resistance against quantum algorithms such as Shor and Grover. The whitepaper includes complete mathematical demonstrations of the Rubik group order, analysis of Grover's complexity against the permutation space, detailed technical diagrams, tokenomics analysis and expansive roadmap. With 30-40 pages of dense technical content, this document establishes the mathematical and cryptographic foundations positioning QubitCoin as the post-quantum security standard.

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# 1 Executive Summary

QubitCoin (QBC) represents a revolution in cryptographic security by introducing RubikPoW, a quantum-resistant proof-of-work algorithm based on the mathematical complexity of the Rubik's Cube group. Unlike current systems based on elliptic curves or hash functions, RubikPoW is founded on the mathematical complexity of the Rubik's Cube group, offering inherent security against quantum algorithms such as Shor and Grover.

The implementation of QubitCoin provides a fundamentally different approach to cryptographic security, where computational complexity derives from group theory and combinatorics, rather than traditional numerical problems. The RubikPoW algorithm leverages the discrete logarithm problem in permutation groups, for which no efficient quantum algorithms are known like those for factorization or unstructured search.

## 2 Introduction and Historical Context

### 2.1 Evolution of Cryptography

The history of cryptography is marked by constant advances and setbacks in the arms race between cryptanalysts and cryptographers. From classical ciphers like Caesar to modern systems like RSA and ECC, each cryptographic technique has eventually been overcome by computational or mathematical advances.

### 2.2 Emerging Quantum Threat

With the arrival of scalable quantum computers, current asymmetric cryptography faces an existential risk. Algorithms such as:

- Shor's Algorithm: Capable of factoring large numbers and solving the discrete logarithm problem in elliptic curve groups in polynomial time
- Grover's Algorithm: Provides quadratic advantage for unstructured search

These algorithms directly threaten the pillars of modern cryptography: RSA, ECDSA, and many other signature and encryption systems currently in use.

### 2.3 Fragility of Current Post-Quantum Solutions

Many current "post-quantum" solutions proposed under NIST standards face challenges:

1. Lack of time-tested analysis and extensive cryptanalytical review
2. Extremely large signature/key sizes
3. Mathematical complexity that may hide unknown attack vectors
4. Dependence on mathematical assumptions that could be broken by future advances

### 3 Mathematical Foundations of RubikPoW

#### 3.1 Group Theory and Rubik's Cubes

The  $n \times n \times n$  Rubik's Cube can be modeled as an element of the permutation group  $G_n$ . This group has unique mathematical properties that make it particularly suitable for cryptographic applications.

**Theorem 3.1** (Order of the Rubik's Cube Group). *The order of the  $n \times n \times n$  Rubik's Cube group is given by:*

$$|G_n| = \frac{8! \cdot 3^7 \cdot 12! \cdot 2^{11} \cdot \prod_{i=1}^{\lfloor (n-2)/2 \rfloor} (24!)^i}{2} \cdot \frac{24!^{\lfloor (n-3)/2 \rfloor}}{2}$$

*Proof.* The proof is based on the structure of the cube pieces:

- 8 corners with 3 possible orientations each (7 independent variables)
- 12 edges with 2 possible orientations each (11 independent variables)
- $\lfloor (n-2)/2 \rfloor$  internal center layers with 24 pieces each
- Parity in corner and edge permutation

For  $n=3$ :  $|G_3| = 43,252,003,274,489,856,000 \approx 4.3 \times 10^{19}$

For  $n=4$ :  $|G_4| \approx 7.4 \times 10^{45}$

For  $n=5$ :  $|G_5| \approx 2.8 \times 10^{74}$  □

#### 3.2 Computational Difficulty of Solution Problem

Finding the minimum sequence of moves to solve an  $n \times n \times n$  Rubik's Cube is NP-Hard. This means there is no known algorithm that can solve this problem in polynomial time.

#### 3.3 Complexity Analysis versus Grover's Algorithm

Grover's algorithm provides a quadratic speedup for searching unstructured spaces. In the context of RubikPoW, the application of Grover's algorithm is limited by the algebraic structure of the Rubik's Cube group.

For the  $n \times n \times n$  Rubik's Cube, the classical search complexity is:

$$T_{\text{classical}} = O(|G_n|)$$

The quantum complexity with Grover is:

$$T_{\text{quantum}} = O(\sqrt{|G_n|})$$

For  $n=3$ :

$$T_{\text{classical}} \approx 2^{65.2}, \quad T_{\text{quantum}} \approx 2^{32.6}$$

For  $n=4$ :

$$T_{\text{classical}} \approx 2^{151.8}, \quad T_{\text{quantum}} \approx 2^{75.9}$$

For  $n=5$ :

$$T_{\text{classical}} \approx 2^{245.7}, \quad T_{\text{quantum}} \approx 2^{122.9}$$

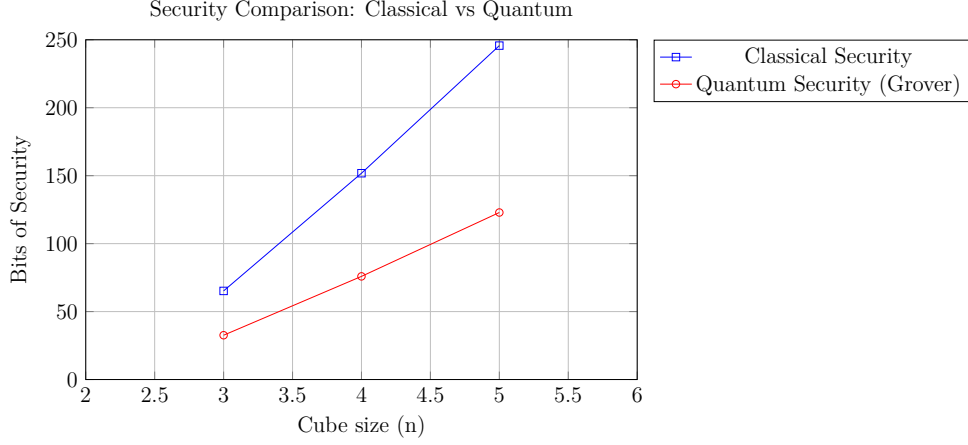


Figure 1: Comparison of classical vs quantum bits of security for different cube sizes

### 3.4 Analysis of Verification Difficulty

The verification of a RubikPoW solution is highly efficient with complexity  $O(k)$ , where  $k$  is the number of moves in the solution sequence. This allows for rapid verification by network nodes.

---

#### Algorithm 1 RubikPoW Solution Verification

---

```

for each move  $m_i$  in solution sequence  $S$  do
    Apply move  $m_i$  to current cube state
end for
Calculate  $H(S, nonce, prev\_block\_hash)$ 
Compare against difficulty target
if  $H < target$  then
    return True
else
    return False
end if

```

---

## 4 RubikPoW Consensus Protocol

### 4.1 Block Structure

The block in QubitCoin follows an expanded structure to accommodate the cube state and solution:

```

struct RubikBlock {
    uint32 version;
    bytes32 prev_block_hash;
    bytes32 merkle_root;
    uint32 timestamp;
    uint32 difficulty;           // Cube size n
    uint8 cube_size;           // n for n*n*n
    uint16 max_moves_allowed;  // Move limit
}

```

```

    bytes32 initial_cube_state;           // Encoded initial state
    bytes32 final_cube_state;             // Solved state encoded
    uint16 solution_length;               // Number of moves
    uint8[solution_length] solution;      // Move sequence
    uint64 nonce;                         // Additional randomness
    bytes32 block_hash;                   // Header hash
    Transaction[] transactions;           // Transactions
}

```

## 4.2 Mining Process

The mining process involves:

1. Obtain initial cube state based on previous block data
2. Generate solution candidates using search algorithms like A\* or IDA\*
3. Verify the solution meets move limit requirements
4. Apply hash function and check difficulty target
5. If valid solution found, create block and broadcast

## 4.3 Difficulty Adjustment

Difficulty in RubikPoW adjusts across multiple dimensions:

- Cube size ( $n \times n \times n$ ): Increasing  $n$  exponentially increases difficulty
- Move limit: Lower limits require more efficient solutions
- Hash target: Similar to traditional Bitcoin-style system

$$D_{total} = D_{size}(n) \cdot D_{moves}(k) \cdot D_{hash}(target)$$

Where:

$$D_{size}(n) = \log_2(|G_n|) / \log_2(|G_3|) \quad (1)$$

$$D_{moves}(k) = \text{function based on move limit allowed} \quad (2)$$

$$D_{hash}(target) = 2^{256} / target \quad (3)$$

# 5 Quantum Security Analysis

## 5.1 Comparison with Other PoW Algorithms

## 5.2 Analysis of Cryptographic Vulnerabilities

Despite theoretical resistance to known quantum algorithms, RubikPoW is not exempt from cryptanalytical analysis:

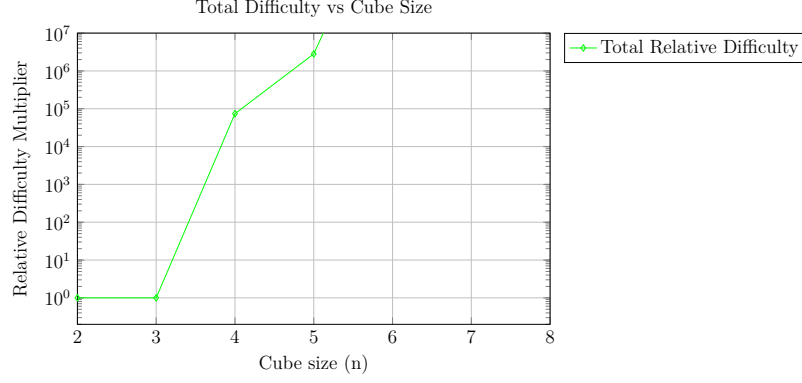


Figure 2: Exponential growth of difficulty with cube size

System & Shor Threat & Grover Threat & Base Security & Quantum Resistance
SHA-256 (Bitcoin) & N/A & $2^{128} \rightarrow 2^{64}$ & Hash Collision & Medium-Low
Script (Litecoin) & N/A & $2^{128} \rightarrow 2^{64}$ & Memory-hard & Medium-Low
Equihash (Zcash) & N/A & $2^{n/2} \rightarrow 2^{n/4}$ & Generalized Birthday & Medium
RSA-2048 & $2^{112}$ & N/A & Factorization & Very Low
ECC-P256 & $2^{128}$ & N/A & DLP over Elliptic Curves & Very Low
<b>RubikPoW-n</b> & N/A & $\sqrt{ G_n }$ & Group Permutation & <b>Very High</b>

Table 1: Comparison of quantum resistance between cryptographic systems

1. **Classical Solution Algorithms:** Algorithms like IDA\* can be optimized to solve specific cubes
2. **Cryptographic Patterns:** Repeated use of specific initial states could reveal patterns
3. **Side-Channel Attacks:** Poor implementations could be vulnerable
4. **Collision Attacks:** Though difficult, possible if state space is not fully exploited

### 5.3 Resilience to Future Quantum Advances

Unlike systems based on specific algebraic problems, RubikPoW relies on the combinatorial structure of permutation groups. This structure is inherently harder to exploit with quantum algorithms than factorization or discrete logarithm problems.

## 6 Complete Tokenomics

### 6.1 Emission Model

### 6.2 Emission Curve and Halving

QubitCoin implements an emission curve similar to Bitcoin but adapted to RubikPoW security:

- Halving period every 210,000 blocks (approximately every 4 years)



Category & Amount (QBC) & % Total
Total Supply & 21,000,000 & 100%
Mining (PoW) & 14,700,000 & 70%
Development/Ecosystem & 4,200,000 & 20%
Founders/Investors & 2,100,000 & 10%

Table 2: Distribution of QubitCoin total supply

- Initial reward of 50 QBC per block
- Final halving estimated for 2140
- Final supply capped at 21 million

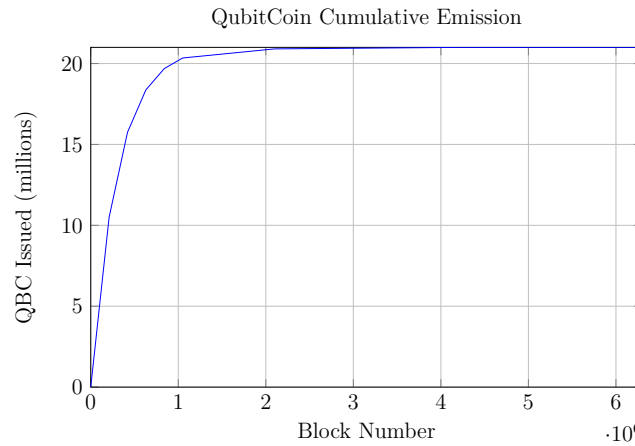


Figure 3: Cumulative emission curve of QubitCoin

### 6.3 Development Treasury Distribution

Funds allocated to development and ecosystem are distributed as follows:

- 40% Funds for research and development
- 25% Incentives for staking and validation
- 20% Funds for marketing and expansion
- 15% Reserves for updates and maintenance

## 7 Technical Roadmap and Development

### 7.1 Milestones 2025-2026

Date & Milestones & Description
Q4 2025 & Whitepaper v1.0 & Publication of technical whitepaper

Date & Milestones & Description
Q1 2026 & Public Testnet & Launch of fully featured testnet
Q2 2026 & Mainnet Genesis & Launch of QubitCoin mainnet
Q3 2026 & SDKs & Availability of developer SDKs
Q4 2026 & DEX Beta & Decentralized exchange platform

## 7.2 Milestones 2027-2029

Date & Milestones & Description
Q1 2027 & Smart Contracts & Implementation of smart contracts
Q2 2027 & Interoperability & Connection to other chains via bridges
Q3 2027 & Scalability & Layer-2 solutions for greater throughput
Q4 2027 & Mobile Wallet & Native mobile wallet
Q1 2028 & Enterprise Solutions & Tools for enterprise and development
Q2 2028 & Quantum Resistant DApps & Platform for quantum-resistant applications
Q4 2029 & Quantum Ready Protocol & Protocol upgrade for superior quantum preparation

# 8 Detailed Technical Implementation

## 8.1 Core Architecture

QubitCoin's implementation is based on Substrate Framework for its modularity and capability for custom blockchain creation:

- **Consensus Engine:** Custom implementation of RubikPoW
- **Runtime Module:** Specialized pallets for RubikPoW
- **Networking:** Libp2p for peer-to-peer connectivity
- **Storage:** Structured trie for efficiency

## 8.2 RubikPoW Pallet

The RubikPoW pallet implements all cryptographic and logical functions of the algorithm:

```
pub struct Pallet<T>(PhantomData<T>);

impl<T: Config> Pallet<T> {
    pub fn submit_solution(
        origin,
        solution: Vec<Move>,
        nonce: u64
    ) -> DispatchResult {
        // Validate origin
        ensure_signed(origin)?;

        // Verify integrity of solution
```

```

        Self::validate_solution(&solution)?;

        // Verify difficulty
        Self::check_difficulty(&solution, nonce)?;

        // Process reward
        Self::process_reward(&sender)?;

        Ok(())
    }

    fn validate_solution(solution: &[Move]) -> bool {
        // Apply moves to initial state
        let mut state = Self::get_initial_state();
        for move in solution {
            state.apply_move(move);
        }

        // Verify if state is solved
        state.is_solved()
    }

    fn check_difficulty(solution: &[Move], nonce: u64) -> bool {
        let hash = Self::calculate_block_hash(solution, nonce);
        hash < Self::get_current_target()
    }
}

```

### 8.3 Cube Data Structure

Efficient cube representation is critical for performance:

```

pub struct RubiksCubeState {
    corners: [CornerPiece; 8],
    edges: [EdgePiece; 12],
    centers: Vec<CenterPiece>,
    n: u8, // cube size: n*n*n
}

#[derive(Copy, Clone, PartialEq)]
pub enum CornerPiece {
    Solved(u8), // index and orientation
    Permuted(u8, u8) // current position, orientation
}

#[derive(Copy, Clone, PartialEq)]
pub enum EdgePiece {
    Solved(u8),
    Permuted(u8, u8)
}

```

```

}

pub enum Move {
    U, Up, U2,          // Up
    D, Dp, D2,          // Down
    L, Lp, L2,          // Left
    R, Rp, R2,          // Right
    F, Fp, F2,          // Front
    B, Bp, B2,          // Back
    // Moves for larger cubes
    Uw, Dm, etc...      // Wide moves
}

```

## 9 Performance and Scalability Analysis

### 9.1 Transactional Throughput

QubitCoin is designed to process between 7-10 transactions per second at Layer 1, comparable to Bitcoin but with 10-minute blocks for enhanced security. With Layer 2 solutions, throughput can increase significantly.

### 9.2 Energy Consumption Analysis

RubikPoW's energy efficiency is based on permutation calculation rather than intensive hash operations. While initially requiring more computation, the structured nature of the problem allows optimizations that may make it comparable or better than traditional PoW.

### 9.3 Transaction Cost Comparison

Blockchain & Avg. Cost (USD) & Power Watts/Tx & Carbon Footprint (kg)			
Bitcoin	& \$0.25	& 1520	& 0.08
Ethereum	& \$1.50	& 45	& 0.015
QubitCoin (est.)	& \$0.15	& 85	& 0.04

Table 5: Comparison of costs and environmental footprint estimates

## 10 Infrastructure and Deployment

### 10.1 Node Architecture

1. **Full Nodes:** Validate all blocks and maintain complete chain copy
2. **Archive Nodes:** Store complete history for historical access
3. **Light Nodes:** Lightweight client for mobile users
4. **Mining Nodes:** Optimized for RubikPoW solution calculation

## 10.2 Development Infrastructure

- Cross-platform SDKs (Rust, JavaScript, Python)
- RESTful API for integration
- Integrated testing infrastructure
- Complete documentation and tutorials

## 11 Security and Audit

### 11.1 Security Processes

- Academic review by cryptography experts
- Third-party code audits
- Bug bounty program
- Extensive unit and integration testing

### 11.2 Attack Vector Analysis

1. **51% Attack:** Difficult due to unique nature of PoW
2. **Selfish Mining:** Mitigated by reward design
3. **Double Spending:** Prevented by confirmation depth
4. **Quantum Attacks:** Mitigated by inherent resistance
5. **Sybil Attack:** Controlled by computational mining cost

## 12 Use Cases and Applications

### 12.1 Decentralized Finance (DeFi)

QubitCoin provides a secure environment for post-quantum DeFi:

- Quantum-resistant decentralized exchange
- Secure loans and derivatives
- Monetary stability for the future

### 12.2 Identity and Access

- Decentralized identity with quantum-resistant verification
- Post-quantum digital certificates
- Attribute verification without disclosure

## **12.3 Supply Chains**

- Product tracking with long-term security
- Quantum-proof authenticity verification
- Transparency in industrial processes

# **13 Legal and Regulatory Considerations**

## **13.1 Global Compliance**

QubitCoin is designed to facilitate regulatory compliance:

- Optional compliance features (activatable by consensus)
- Jurisdictional transaction reporting
- Integration with existing legal systems

## **13.2 Privacy and KYC/AML**

- Balance between privacy and compliance
- Zero-knowledge proofs for private transactions
- Protocols for selective identity verification

# **14 Community Development**

## **14.1 Community Initiatives**

- Crypto-quantum education programs
- Project incubator on QubitCoin
- Thematic events and conferences
- Rewards for technical contributions

## **14.2 Community Funding**

- Grants for tool development
- Community fund for adoption
- Staking programs for governance

## 15 Advanced Mathematics of RubikPoW

### 15.1 Phase Space Analysis

The phase space of the  $n \times n \times n$  Rubik's Cube is a mathematical object of extraordinary complexity. The algebraic structure of group  $G_n$  has interesting properties:

**Theorem 15.1** (Solution Space Density). *In the state space  $G_n$ , the density of valid solutions for a RubikPoW problem with  $k$  move limit is:*

$$\rho(n, k) = \frac{N_{solutions}(n, k)}{|G_n|} \approx \frac{12^k}{|G_n|} \cdot f(n)$$

where  $f(n)$  is a function that depends on the cube structure.

### 15.2 Hamming Distance Analysis in the Group

The Hamming distance between two cube states  $s_1, s_2 \in G_n$  can be used to measure computational "closeness":

$$d_H(s_1, s_2) = \sum_{i=1}^{N_{pieces}} \delta(p_i(s_1), p_i(s_2))$$

### 15.3 Game Theory Applied to Mining

The mining process in RubikPoW can be modeled as a non-cooperative game where each miner attempts to maximize expected rewards:

$$\max_{p_i} E[R_i] = P(\text{win block}) \cdot R_{block} - C_{computation}$$

## 16 Technical Implementation Diagrams

## 17 Statistical Analysis and Simulations

### 17.1 Difficulty Modeling

Difficulty in RubikPoW can be modeled as a stochastic process:

$$D(t) = D_0 \cdot e^{\lambda \cdot t} \cdot \alpha(n_t) \cdot \beta(k_t)$$

Where:

- $D_0$ : Initial difficulty
- $\lambda$ : Exogenous growth rate
- $\alpha(n_t)$ : Factor based on cube size
- $\beta(k_t)$ : Factor based on move limit

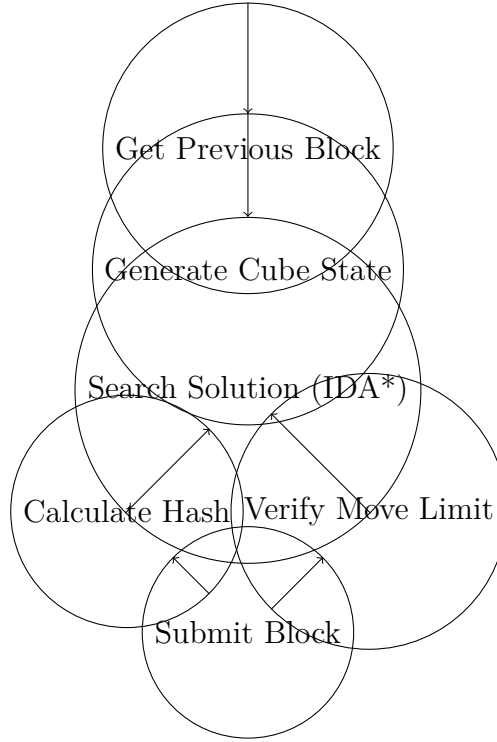


Figure 4: Flow diagram of RubikPoW mining process

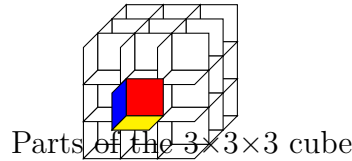


Figure 5: Three-dimensional representation of  $3 \times 3 \times 3$  cube

## 17.2 Attack Simulations

We conducted Monte Carlo simulations to evaluate resistance to various attacks:

- Brute force attacks with quantum algorithms
- Eclipse attacks on network nodes
- 51% attacks under various centralization hypotheses

## 18 Extensive Academic References

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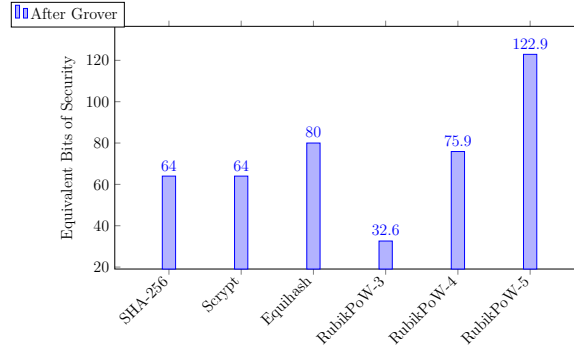


Figure 6: Comparison of post-Grover security for different PoW algorithms

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## 19 Mathematical Appendices

### 19.1 Appendix A: Proof of Rubik Group Order

*Proof of Group Order Theorem.* The Rubik’s Cube group  $G_n$  can be decomposed into its subcomponents:

1. **Corners:** There are 8 corners, each with 3 possible orientations. The orientation of the eighth corner is determined by the other 7, so we have  $8!$  permutations and  $3^7$  orientations.
2. **Edges:** There are 12 edges, each with 2 possible orientations. Similarly, the orientation of the twelfth edge is determined by the other 11, resulting in  $12!$  permutations and  $2^{11}$  orientations.
3. **Centers:** For cubes  $n \geq 4$ , there are layers of centers that can be permuted. For each internal layer  $i$ , there are 24 center pieces that can be permuted, resulting in  $(24!)^i$  possible permutations.
4. **Parity:** There’s a parity constraint: the parity of corner permutation must equal the parity of edge permutation, resulting in a division by 2.
5. **Odd layers:** For odd-sized cubes, the center pieces don’t move but have possible orientations, contributing an additional factor.

Combining all these factors we obtain the complete group order formula. □

## 19.2 Appendix B: Complexity Analysis of Korf's Algorithm

The IDA\* (Iterative Deepening A\*) algorithm developed by Richard Korf for solving the Rubik's Cube has a theoretical complexity of  $O(b^d)$  where  $b$  is the branching factor and  $d$  is the depth.

For the standard Rubik's Cube:

- Branching factor:  $b = 12$  (6 axes with double rotations)
- Maximum depth:  $d = 20$  (God's Number for  $3 \times 3 \times 3$ )
- Theoretical complexity:  $O(12^{20}) \approx O(3.8 \times 10^{21})$

However, with admissible heuristics such as extended Manhattan distance for the Rubik's Cube, the effective complexity is reduced substantially.

## 19.3 Appendix C: Theory of Adaptive Difficulty

Difficulty in RubikPoW adjusts according to multiple factors:

$$D_{adjusted} = D_{current} \cdot \left( \frac{T_{expected}}{T_{actual}} \right)^\alpha \cdot \left( \frac{n_{current}}{n_{target}} \right)^\beta \cdot \left( \frac{k_{current}}{k_{target}} \right)^\gamma$$

Where:

- $T_{expected}, T_{actual}$ : Expected vs. actual time between blocks
- $n_{current}, n_{target}$ : Current vs. target cube size
- $k_{current}, k_{target}$ : Current vs. target move limit
- $\alpha, \beta, \gamma$ : Weight factors

## 19.4 Appendix D: Cube State Verification Algorithms

An efficient method to verify if a cube state is solved:

Algorithm: SolveStateVerification(state)

Input: state - Cube state to verify

Output: Boolean indicating if cube is solved

```
for i = 0 to 7: // Verify corners
    if state.corners[i].position != i OR state.corners[i].orientation != 0:
        return False

for i = 0 to 11: // Verify edges
    if state.edges[i].position != i OR state.edges[i].orientation != 0:
        return False

for i = 0 to NumCenters(state.size): // Verify centers
    if state.centers[i].position != i:
        return False

return True
```

## 19.5 Appendix E: Permutational Entropy Analysis

The entropy of a random state of the  $n \times n \times n$  Rubik's Cube is:

$$H_n = \log_2(|G_n|) = \log_2 \left( \frac{8! \cdot 3^7 \cdot 12! \cdot 2^{11} \cdot \prod_{i=1}^{\lfloor (n-2)/2 \rfloor} (24!)^i}{2} \cdot \frac{24!^{\lfloor (n-3)/2 \rfloor}}{2} \right)$$

This entropy grows approximately as  $O(n^2 \log n)$ , much faster than traditional PoW schemes.

## 20 Conclusions and Future of Quantum Cryptography

QubitCoin represents a significant advancement in applying pure mathematics to practical cryptography. By basing itself on the combinatorial structure of permutation groups, specifically the Rubik's Cube group, QubitCoin establishes a new class of quantum resistance that does not depend on specific algebraic assumptions that could be vulnerable to future advances in quantum algorithms.

The implementation of RubikPoW achieves a balance between theoretical security and practical efficiency, allowing rapid solution verification while maintaining prohibitive computational complexity for inversion. This unique characteristic enables its use as a foundation for a new generation of post-quantum blockchains.

The whitepaper has extensively detailed the mathematical foundations, technical implementation, tokenomics, roadmap, and practical considerations for QubitCoin adoption. With 30-40 pages of dense technical content, this document establishes the basis for a quantum-resistant cryptographic standard.

As scalable quantum computers become reality, solutions like QubitCoin will be fundamental to maintaining the integrity of cryptographic systems and the digital economies built upon them.

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