	EE 102: Signal Processing and Linear Systems
	Instructor: Ayush Pandey
	Homework #1: Introduction to Signals
Name:	Submission Date:

Problem 1

[Adapted from Problem 3 in Vierinen and Jensen] A time scaling system adjusts the scaling of the independent variable: $y(t) = x(\alpha t)$, when x(t) is the signal fed into the system and y(t) is the output. Answer the following questions for this system:

- 1. [5 points] Draw a block diagram for the system. Label the input, output, and the system.
- 2. [5 points] What is the effect on the signal when $0 < \alpha < 1$. What about $\alpha > 1$?
- 3. [5 points] Prove that the system is linear.
- 4. [5 points] Give an example of a real-world application where studying this system can be useful. Then, for this example, propose a nonlinear modification to the system, which captures a real situation.

[use more pages if needed]

Due: September 7, 2025

Problem 2 Consider the signal $x(t) = a^{-tu(t)}$, where u(t) is the unit step function.

- 1. [5 points] Sketch x(t) for time -2 < t < 2 for a > 0. You are not allowed to use computer programs to do this.
- 2. [5 points] Sketch y(t) for time -2 < t < 2 for a > 0, where y(t) = 2x(5 0.5t)
- 3. [5 points] Find out whether the signal y(t) is time-invariant.
- 4. [5 points] Find out whether the signal y(t) converges to 0 as $t \to \infty$ for a > 0.
- 5. [5 points] Find the value of a such that y(1) = 0.1.
- 6. [5 points] Think of a signal that you can relate x(t) with. Analyze the properties of x(t) to find out a real-world signal that shares similar characteristics.

[use more pages if needed]

Problem 3 For each of the signals below, you have four tasks:

1. [2 points, per signal] Sketch the signal (clearly label the amplitude and axes)

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2. [8 points, per signal] Compute E_{∞} and P_{∞} using the definitions provided in the lecture notes.

3. [3 points, per signal] Using Python (or MATLAB), plot the signal over an appropriate interval and confirm your findings.

4. [3 points total] Briefly discuss a relevant example where the properties of the signal can be important.

You must do the three parts above for each of the three signals below

(a)
$$x_1[n] = (\frac{1}{3})^n u[n]$$

(b)
$$x_2(t) = e^{j(3t+\pi/7)}$$

(c)
$$x_3[n] = e^{j(\frac{\pi}{3}n + \pi/10)}$$

Hint: To sketch a signal, compute its values for multiple values of time to understand the pattern. Remember that u(n) is the continuous-time unit step function and u[n] is the discrete-time unit step function. For signals in complex polar form, you can sketch the real part and the imaginary part on separate axes.

[use more pages if needed]

Problem 4 Please write a short reflection on how many hours you dedicated to completing this homework assignment (do not include the time spent on the pre-requisite assignment). Also, please rate the difficulty of this assignment according to you. [2 points]