Assignment 1

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Download all python codes from

https://github.com/ka-raja-babu/Matrix-Theory/tree/main/Assignment1/Codes

and latex-tikz codes from

https://github.com/ka-raja-babu/Matrix-Theory/ tree/main/Assignment1

1 Question No. 2.12

Draw $\triangle PQR$ with PQ=4,QR=3.5 and PR=4.what type of triangle is this?

2 EXPLANATION

Let

$$\mathbf{P} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 4 \\ 0 \end{pmatrix}, \mathbf{R} = \begin{pmatrix} a \\ b \end{pmatrix}$$
 (2.0.1)

The vertex \mathbf{R} can be expressed in *polar coordinate form* as

$$\mathbf{R} = PR \begin{pmatrix} \cos \theta \\ \sin \theta \end{pmatrix} \tag{2.0.2}$$

where,

$$PQ(\sin\theta \div 2) = QR \div 2 \tag{2.0.3}$$

$$\theta = 2\sin^{-1}\left(QR \div 2PQ\right) \tag{2.0.4}$$

$$\theta = 2\sin^{-1}(3.5 \div 8) \tag{2.0.5}$$

$$\theta = 51.88$$
 (2.0.6)

$$\mathbf{R} = 4 \begin{pmatrix} 0.6173 \\ 0.786 \end{pmatrix} \tag{2.0.7}$$

$$\mathbf{R} = \begin{pmatrix} 2.47 \\ 3.15 \end{pmatrix} \tag{2.0.8}$$

so, the vertices of $\triangle POR$ are

$$\mathbf{P} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 4 \\ 0 \end{pmatrix}, \mathbf{R} = \begin{pmatrix} 2.47 \\ 3.15 \end{pmatrix} \tag{2.0.9}$$

Lines PQ, QR and RP are then generated and plotted using these coordinates to form $\triangle PQR$.

then,

$$\mathbf{PQ} = \|\mathbf{Q} - \mathbf{P}\|^2 = \|\mathbf{Q}\|^2 = 4^2 = 16 \quad (: \mathbf{P} = 0)$$
(2.0.10)

$$\mathbf{QR} = \|\mathbf{R} - \mathbf{Q}\|^2 = \left\| \begin{pmatrix} 2.47 \\ 3.15 \end{pmatrix} - \begin{pmatrix} 4 \\ 0 \end{pmatrix} \right\|^2 = 12.2$$
(2.0.11)

$$\mathbf{PR} = \|\mathbf{R} - \mathbf{P}\|^2 = \|\mathbf{R}\|^2 = 2.47^2 + 3.15^2 = 16.02 \quad (: \mathbf{P} = 0)$$
(2.0.12)

Here

$$PO = PR \tag{2.0.13}$$

(: Twosidesareequal)

Hence $\triangle PQR$ is a isosceles triangle. Plot of the isosceles $\triangle PQR$:

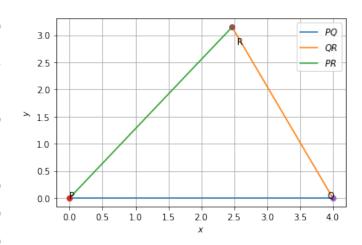


Fig. 2.1: isosceles $\triangle PQR$