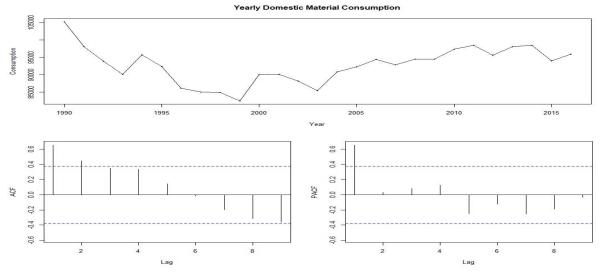
Data set: dmc_ch contains yearly data on domestic material consumption (in thousand tonnes) for Switzerland from 1990 to 2016.

VISUALIZATION



- Non seasonal data
- Increasing and decreasing trend
- Non stationary data

MODEL ESTIMATION

ETS model

Model used ("AAN", "MAN", "MMN", "AAN", "MAN", "MMN") with and without damping. All relevant models performance are compared together with other models in the end.

| AICC | MASE_train | MASE_test | RMSE_train | RMSE_test | Damping |
|--------------|------------|-----------|------------|-----------|---------|
| AAN 423.2965 | 0.9946192 | 0.5834944 | 3725.262 | 2074.092 | O |
| AMN 421.8353 | 0.9067382 | 1.0183884 | 3597.887 | 3870.136 | 0 |
| MAN 423.5865 | 1.0051628 | 0.5181176 | 3720.140 | 1722.215 | 0 |
| MMN 423.5777 | 0.8992168 | 1.0025049 | 3600.030 | 3815.697 | 0 |
| AAN 426.1649 | 0.9841416 | 0.5015751 | 3626.238 | 1643.319 | 1 |
| AMN 423.5930 | 0.9116304 | 0.8489322 | 3410.844 | 3246.759 | 1 |
| MAN 426.7450 | 0.9996347 | 0.5068132 | 3650.373 | 1658.640 | 1 |
| MMN 424.4039 | 0.9312584 | 0.5394759 | 3431.250 | 1810.373 | 1 |

ARIMA model

Stationary data: Number of diff comes as 1 and 0. We will inspect booth.

Depending on ACF and PACF ARIMA(0,1,0) is initial expected model for d = 1

Depending on ACF and PACF ARIMA(1,0,1) is initial expected model for d = 0

| | р | d | q | AICc | MASE_train | MASE_test | RMSE_train | RMSE_test |
|------------------|--|--------|---------------------------------|--|--|--|--|--|
| n | 1 0 | 1 | 0 | 388.6518 | 0.9540 | 0.5141 | 3704.946 | 1763.811 |
| m | 12 0 | 1 | 1 | 391.0964 | 0.9503 | 0.5141 | 3701.081 | 1812.190 |
| m | 13 0 | 1 | 2 | 393.8182 | 0.9622 | 0.5058 | 3694.053 | 1724.735 |
| m | 4 1 | 1 | 0 | 391.1031 | 0.9502 | 0.5144 | 3701.782 | 1806.181 |
| m | | | | 393.8921 | 0.9415 | 0.5365 | 3700.697 | 2001.982 |
| n | 6 1 | 1 | 2 | 396.9538 | 0.9626 | 0.5039 | 3690.966 | 1704.105 |
| n | 7 2 | 1 | 0 | 393.7347 | 0.9669 | 0.5011 | 3685.047 | 1694.215 |
| n | 18 2 | 1 | 1 | 396.8481 | 0.9668 | 0.4993 | 3679.343 | 1661.739 |
| | | | | 396.8556 | 0.8090 | 0.5799 | 3096.752 | 2032.578 |
| | | | | | | | | |
| | | | | | | | | |
| | | d | a | ATCC | MASE thain | MASE tost | DMSE thain | BMSE tost |
| | | d | q | | | | RMSE_train | |
| | 1 0 | 0 | o | 423.6649 | 1.3459 | 1.6735 | 5204.142 | 5383.384 |
| | | 0 | o | 423.6649 | | | | 5383.384 |
| n | 1 0 | 0 | 0 | 423.6649 | 1.3459 | 1.6735 | 5204.142 | 5383.384 |
| n | 1 0 12 0 | 0 | 0 | 423.6649 418.2144 415.6286 | 1.3459 1.1207 | 1.6735 1.3941 | 5204.142 4244.001 | 5383.384 4524.313 |
| n | 1 0 12 0 13 0 | 0000 | 0 1 2 0 | 423.6649 418.2144 415.6286 | 1.3459 1.1207 0.9868 | 1.6735 1.3941 1.1411 | 5204.142 4244.001 3645.845 | 5383.384 4524.313 3921.075 |
| n n n | n1 0 n2 0 n3 0 n4 1 | 0000 | 01201 | 423.6649 418.2144 415.6286 412.5208 | 1.3459 1.1207 0.9868 1.0389 | 1.6735 1.3941 1.1411 0.5109 | 5204.142 4244.001 3645.845 3643.664 | 5383.384 4524.313 3921.075 1727.720 |
| n | 11 0 12 0 13 0 14 1 15 1 | 000000 | 0 1 2 0 1 2 | 423.6649 418.2144 415.6286 412.5208 415.3469 | 1.3459 1.1207 0.9868 1.0389 1.0338 | 1.6735 1.3941 1.1411 0.5109 0.5319 | 5204.142 4244.001 3645.845 3643.664 3620.172 | 5383.384 4524.313 3921.075 1727.720 1835.016 |
| n n n n | n1 0 n2 0 n3 0 n4 1 n5 1 n6 1 | 000000 | 0 1 2 0 1 2 0 | 423.6649 418.2144 415.6286 412.5208 415.3469 418.8101 | 1.3459 1.1207 0.9868 1.0389 1.0338 | 1.6735 1.3941 1.1411 0.5109 0.5319 0.5690 | 5204.142 4244.001 3645.845 3643.664 3620.172 3617.537 | 5383.384 4524.313 3921.075 1727.720 1835.016 2045.123 |

MODEL SELECTION

| | | | MASE | MASE | RMSE | RMSE | | |
|----|-------|----------|--------|--------|-----------|-----------|---------|------|
| SR | MODEL | Aicc | TRAIN | TEST | TRAIN | TEST | Damping | d |
| 1 | AMN | 421. 835 | 0. 907 | 1. 018 | 3597. 887 | 3870. 136 | 0 | |
| 2 | AAN | 426. 165 | 0. 984 | 0. 502 | 3626. 238 | 1643. 319 | 1 | |
| 3 | AMN | 423. 593 | 0. 912 | 0. 849 | 3410. 844 | 3246. 759 | 1 | |
| 4 | ANN | 416. 478 | 0. 953 | 0. 514 | 3704. 890 | 1763. 727 | | Auto |
| 5 | 2,1,2 | 396. 856 | 0. 809 | 0. 580 | 3096. 752 | 2032. 578 | | 1 |
| 6 | 2,1,1 | 396. 848 | 0. 967 | 0. 499 | 3679. 343 | 1661. 739 | | 1 |
| 7 | 1,0,0 | 412. 521 | 1. 039 | 0. 511 | 3643. 664 | 1727. 720 | | 0 |
| 8 | 2,0,2 | 415. 348 | 0. 672 | 0. 772 | 2539. 282 | 2800. 472 | | 0 |

Best model from all considered model is **ARIMA (2,1,1).** It also Succeeded in LjungBox Test.

Final Forecast with best model

