

# Generalized algorithm

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- arguments:
  - value to partition
  - max partition summands
  - set of partition summands
- initialization
  - set the number of summands -  $n_{sub\ s}$ 
    - value of partition if 0
    - else max partition summands
  - create array of values for summands
    - set of partition summands as argument
    - otherwise 1 ... num summands otherwise
  - initialize coefficients array of size  $n_{sub\ s}$  to 0
  - initialize remainder array of size  $n_{sub\ s}$  to 0
    - set `remainder[n_sub_s - 1] = x`
    - set `remainder[n_sub_s] = x`
  - store the value to partition,  $x$
  - initialize count to 0
  - set level,  $l$ , to  $n_{sub\ s} - 1$
  - set coefficient temporary,  $c_{sub\ t}$ , to 0
  - set remainder temporary,  $r_{sub\ i}$ , to  $x$

```
x = n
ns = num_summands ? num_summands else x
summands = [1 ... n]
coeff = [0 ... 0]
remainder = [0 ... x , x]
count = 0
level = ns - 1
c_sub_t = 0
r_sub_i = x
```

1. if the current level is greater than or equal to the number of summands return the number of summands

```
if level is >= ns return ns
```

1. set the remainder at level  $i$  to  $r_{\text{sub } i}$  (the value to partition to start) set the coefficient at level  $i$  to  $c_{\text{sub } i}$  (0 to start)

```
remainder[level] =  $r_{\text{sub } i}$  // x to start  
coeff[level] =  $c_{\text{sub } i}$  // 0 to start
```

1. if the current level is not 0

- if the remainder at the current level (index of last summand to start) is greater than 0
  - set coefficient at index level - 1 to 0
  - set remainder at level - 1 = remainder at level
  - decrement level
  - repeat 3.

2. if the current level is 0

- if remainder at current level is not 0
  - calculate  $\text{rmdr} / \text{summand}$  for level, set to var  $d$  (number of times summand goes into remainder)
  - $\text{rmdr at level} = \text{rmdr at level} - d * \text{summand at level}$  (remainder is  $\text{summand} \times (\text{floor}(\text{remainder} / \text{summand}))$ ) i.e.  $r - (\text{floor}(r / x))$
  - coefficient at level =  $d$  (i.e.  $\text{remainder} / \text{summand}$ )

3. if remainder at current level is 0

- increment count
- go to ... with level

4. increment level

- if level is  $\geq$  number of summands go to ... with level number of summands

5. remainder at level equals remainder - value (i.e. reduce remainder by on value of current index)

- increment coefficient at level
- go to 3.

6. level equals current level (from 5.) or number of summands (from 6.)

- set coefficients and remainders up to current level equal to 0
- increment level
- $r_{\text{sub } i} = \text{remainder at level} - \text{value at level}$
- $c_{\text{sub } i} = \text{coefficient at level} + 1$

- if the current level is less than the number to partition go to 1.