

- NOTE: for each API that requires a specific Node as input, think of it as two calls, call() and call(Node)

# APIs

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## Generalized List

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```
void      addFront(Item item)
void      addBack(Item item)
Item      deleteFront()
Item      deleteBack()
void      delete(Item item)
void      add(int i, Item item)
Item      delete(int i)
boolean   contains(Item item)
boolean   isEmpty()
int       size()
```

## Bag

---

```
void      add(Item item)
boolean   isEmpty()
int       size()
```

## Queue

---

```
void      enqueue(Item item)
Item      dequeue()
boolean   isEmpty()
int       size()
```

## Generalized Queue (similar to List)

---

```
boolean   isEmpty()
int       size()
void      insert(Item x)
Item      delete(int k)
```

# Set

---

```
void      add(Key key)
void      delete(Key key)
boolean   contains(Key key)
boolean   isEmpty()
int       size()
```

## Mathematical set operations

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```
Set<Key>   complement() -> all keys not in set
void       union(Set<Key> a)
void       intersection(Set<Key> a)
```

## Stack (LIFO/Pushdown)

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```
void       push(Item item)
Item       pop()
boolean    isEmpty()
int        size()
```

## Deque

---

```
boolean    isEmpty()
int        size()
void       pushLeft(Item item)
void       pushRight(Item item)
Item       popLeft()
Item       popRight()
```

## Generalized Buffer

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```
void       insert(Item item)
Item       delete()
void       left(int k)
void       right(int k)
int        size()
```

# Stopwatch

---

```
void      start()
double    elapsedTime()
```

# Maximum Priority Queue (or min)

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```
void      insert(Key k)
boolean   contains(Value v)
Key       max() / min()
Key       deleteMax() / deleteMin()
boolean   isEmpty()
int       size()
```

# Heaps

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# Symbol Table

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```
void      put(Key key, Value val)
Value     get(Key key)
void      delete(Key key)
boolean   contains(Key key)
boolean   isEmpty()
int       size()
(keys)    keys()
(values)  values()
```

```
// additional
Key       min()
Key       max()
Key       floor(Key key)
Key       ceiling(Key key)
int       rank(Key key)
Key       select(int k)
void      deleteMin()
void      deleteMax()
int       size(Key low, Key hi)
(keys)    keys(Key low, Key hi)
(keys)    keys()
```

## Search Tree (as symbol table)

---

```
int      size()
int      size(Node x)
Value    get(Key key)
Value    get(Node x, Key key)
void     put(Key key, Value value)
void     put(Node x, Key key, Value value)

// additional
Key      select(int k)
Node     select(Node x, int k)
int      rank(Key key)
int      rank(Node x, Key key)
void     deleteMin()
Node     deleteMin(Node x)
void     deleteMax()
Node     deleteMax(Node x)
void     delete(Key key)
Node     delete(Node x, Key key)

(keys)   keys()
(keys)   keys(Key low, Key hi)
void     keys(Node x, Queue<Key> queue, Key low, Key hi)
```

## Hash Symbol Table (in addition to above)

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```
int      hash(Key key)

// additional
void     resize() // for linear probing
```

## Undirected Graph

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```
int      numVertices()
int      numEdges()
void     addEdge(int v, int w)
(vertices) adjacentVertices(int v)

// additional
int      degree(Graph G, int v)
int      maxDegree(Graph G)
int      avgDegree(Graph G)
int      numberOfSelfLoops(Graph G)

// find connections (dfs/bfs)
Search(Graph G, int s)
```

```

void      search(Graph G, int v) (dfs/bfs)
boolean   marked(int v)
int       count()

// find paths
          Paths(Graph G, int s)
boolean   hasPathTo(int v)
(ints)    pathTo(int v)

// connections
          ConnectedComponent(Graph G)
boolean   connected(int v, int w)
int       count() // number of connected components)
int       id(int v) // component id

```

## Symbol Graph (degrees of separation)

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## Directed Graphs

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```

// same as undirected graph with additional
Digraph   reverse()

// cycles
boolean   hasCycle()
(ints)    cycle()

```

## Topological Sort

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- NOTE: a graph must be directed and acyclic to have a topological sort order (DAG)

## Strong Connectivity of Graphs

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## Edge (for edge-weighted graph and minimum spanning tree)

---

```

double    weight()
int       either()
int       other(int v)
int       compareTo(Edge that)

```

## Edge-weighted graph (as above)

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## MST (Prim, Kruskal)

---

## Shortest Path (edge-weighted (acyclic) digraph)

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- Dijkstra
- Acyclic
- Bellman-Ford

## Strings

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```
copy
length
compare
concatenate
indexing
substrings

// sorts
key-indexed counting for sorting
LSD (least significant digit) string sort
MSD (most significant digit) string sort

insertion-sort
quicksort
three-way quicksort
three-way string quicksort
mergesort
```

## Tries (uses same API as search trees above)

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- a search tree built from the characters of the search string as keys

## Ternary Search Trees

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## String symbol table types

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- BST
- 2-3/red-black
- linear probing

- trie (r-way trie)
- trie search (TST)

## Search

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- key-indexed search
- sequential search
- binary search
- radix search
- external searching

## Substring search

- brute force
- Knuth-Morris-Pratt (relate to DFAs)
- Boyer-Moore
- Rabin-Karp fingerprint search

## Regular Expressions

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- NOTE: uses NFAs and digraphs

## Data Compression

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- (bit operations)
- run-length encoding
- bitmaps
- Huffman compression
- LZW compression
- LZ77

## Context

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- event-driven simulation
- collisions
- B-trees
- B-tree set
- suffix arrays
- network flow
- Ford-Fulkerson max flow

- Reductions (shortest path and max flow)

## NP-complete problems

- Boolean satisfiability
- integer linear programming
- load balancing
- vertex cover
- Hamiltonian path
- Protein folding
- Ising model
- Risk portfolio for a return

## Sorting

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- stable-sort
- selection
- insertion
- bubble sort
- shellsort
- mergesort
- quicksort (fastest general purpose)
  - 3-way quicksort/3-way radix quicksort
  - partitioning & stack size
  - recursive & non-recursive
  - binary quicksort
- heapsort
- priority queue sort
- radix sort
  - MSD sort
  - LSD sort
- special purpose sorts
  - Batcher's odd-even mergesort
  - shuffle/unshuffle



- network sorts
  - split-interleave merging
  - external sorting
  - 3-way merge
  - block sort
- 
- (timsort)
- 
- (comb sort)
- 
- (counting sort)
- 
- (radix sort)
- 
- (shuffling and Fisher-Yates shuffle)
- 
- array sorting
- 
- index and pointer sorting
- 
- in-place sorting
- 
- linked-list sorting
- 
- sorting by key-indexed counting

## Hashing

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- hash functions
  - modular hash functions for integers
  - modular hash functions for characters
  - hash functions for string keys
    - character strings
    - universal hash function
- separate chaining
- linear probing
- double hashing
- dynamic hash tables

## Numerical Methods

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- polynomial interpolation
- least-squares estimation
- solution of equations

# Encryption

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- DES
- RSA

# Geometric

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- line segment intersections, points, etc
- convex hulls
- arc length on spherical surfaces

# Graph Algorithms

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- properties and representations
- graph search
  - mazes
  - dfs
    - dfs algorithms
  - separability & biconnectivity
  - bfs
  - generalized search
  - backtracking
  - (Bloom filter)
- digraphs and dags
  - search
  - reachability and transitive closure
  - equivalence relations and partial orders
  - topological sorting
  - strong components
- minimum spanning trees
  - Prim
  - Kruskal
  - Boruvka
  - Euclidean MST

- shortest paths
  - Dijkstra
  - all-pairs shortest path
  - acyclic networks
  - Euclidean networks
  - reduction
  - negative weights
- network flow
  - flow networks
  - augmenting path maxflow
  - preflow-push maxflow
  - maxflow reductions
  - mincost flows
  - network simplex algorithm
  - mincost-flow reductions
- coloring

## Representations

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### Lists (stack, queue, bag, etc)

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- linked list
  - circular
  - doubly-linked
  - singly-linked
  - head only
  - dummy head
  - head, dummy tail
  - head, tail
  - dummy head, dummy tail
  - no container, only head node reference

- statically sized array
- dynamically sized array
- array with pointers/references to nodes (review this in C++ algs)

## Sets

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- lists (all types)
- BST
- B-tree
- hash table (for unordered)

## Symbol Table

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- associative arrays
- search tree
- hash table
- symbol graphs

## Graphs

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- list of sets
- list of lists
- adjacency map/dictionary/table with edge weights
- map/dictionary/table with adjacency sets
- adjacency matrix (with arrays/lists, rows & columns represent vertices)
- incidence matrix (rows represent vertices, columns represent edges)
- weight matrix (using infinity for missing edges)
- union find-style (an array of connected components with the index of the component base)
- lists of edges (pairs representing an edge or an "Edge" type)
- NOTE: adjacency lists work well for sparse graphs, matrices work well for dense graphs

## Trees

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- list of lists
- nodes with children and/or parent
  - children can be pointers/references as members
  - children can be list of pointers/references
- binary string

- string of parens
- (connected acyclic graph)

## list types

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- skip list
- doubly connected list
- (more)

## Tree types

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- general tree
- rooted trees
- ordered trees
- binary trees
- m-ary trees
- free trees
- BST
  - randomized
  - splay
  - top-down 2-3-4
  - red-black
  - skip-lists
- binary search tree
- 2-3 trees
- red-black trees
- AVL trees
- B-trees
- digital search trees
- tries
  - Patricia tries
  - multiway tries

- TSTs
- heaps
- (R-tree, R\* tree, R+ tree)
- (hash tree?)
- (left child, right sibling)
- (multiway trees)
- (space-partitioning trees)

## Graph types

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- sparse
- dense
- directed
- undirected
- cyclic
- acyclic
- connected
- disconnected
- (relationship to trees)
- NOTE:
  - see [https://en.wikipedia.org/wiki/List\\_of\\_data\\_structures](https://en.wikipedia.org/wiki/List_of_data_structures)
  - see [https://en.wikipedia.org/wiki/List\\_of\\_algorithms](https://en.wikipedia.org/wiki/List_of_algorithms)

## Later

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- simple custom memory management when given a block of memory using:
  - block partition pools
  - Arenas
  - Spans?
  - general partitioning
- Descriptions of simplified dynamic memory management techniques are in Modern Compiler Design and TAOC v1