

# LA\_RubanrajRavichandran\_180410\_02\_Exercise1\_MaxL

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Let's suppose we have a set of observations  $x = (x_1, \dots, x_N)^T$ , that are drawn independent and identically distributed (i.i.d) from a Gaussian distribution with unknown mean  $\mu$  and variance  $\sigma^2$

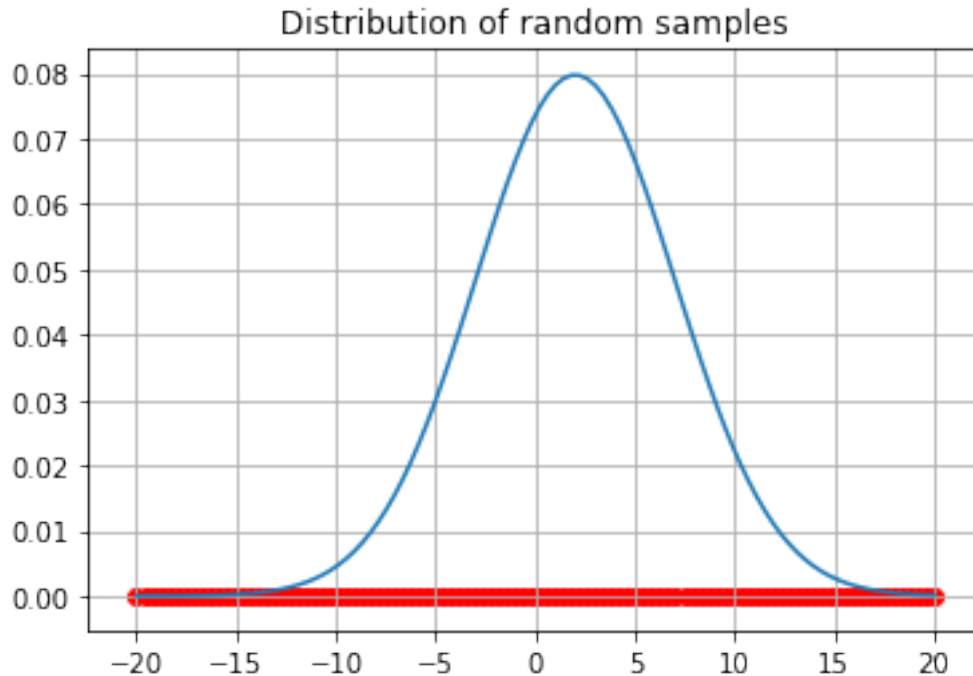
For this example, we are going to assume that the unknown parameters are  $\mu=2$  and  $\sigma^2=25$  and the number of samples  $N=100$ .

```
In [4]: import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
from scipy.stats import norm
from scipy.stats import multivariate_normal
import seaborn as sns
import scipy
from scipy import stats
from scipy.optimize import minimize
```

## 2 Task1:

Plot this (unknown) distribution together with the samples in the range  $[-20, 20]$ .

```
In [5]: mu = 2.
sigma = 5.
N = 100
x = np.linspace(-20, 20, N)
fig, ax = plt.subplots(1,1)
ax.plot(x, norm.pdf(x, mu, sigma))
ax.scatter(x, np.zeros(N), color="r")
ax.grid(True)
plt.title('Distribution of random samples')
plt.show()
```



### 3 Task2:

- Implement the likelihood function in python (you can simply use the existing python implementations)
- Use a general optimization method to find the values for  $\mu$  and  $\sigma^2$ .

```
In [6]: mu = 2.
        sigma = 5.
        N = 100
        x = np.linspace(-20, 20, N)
        y = np.random.normal(mu, sigma, 100)

        print "actual mean : " + str(y.mean())
        print "actual standard deviation : " + str(y.std())

        def likelihood_function(params):
            predicted_mean = params[0]
            std = params[1]
            log_likelihood = -np.sum(norm.logpdf(y, predicted_mean, std))
            return(log_likelihood)

        init_params = [1, 1]
        results = minimize(likelihood_function, init_params, method='Powell')
        print "predicted mean using likelyhood function: " + str(results.x[0])
        print "predicted standard deviation using likelyhood function : " + str(results.x[1])
```

```
actual mean : 2.596122301769203
actual standard deviation : 4.833335849703718
predicted mean using likelyhood function: 2.5961703683890742
predicted standard deviation using likelyhood function : 4.833325914474777
```

## 4 Task3:

Given:  $\mu = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$   $\Sigma = \begin{bmatrix} 0.5 & 0 \\ 0 & 0.5 \end{bmatrix}$  1. Visualise a Gaussian with the given parameters. 2. Visualise a marginal Gaussian. 3. Visualise a slice of Gaussian.

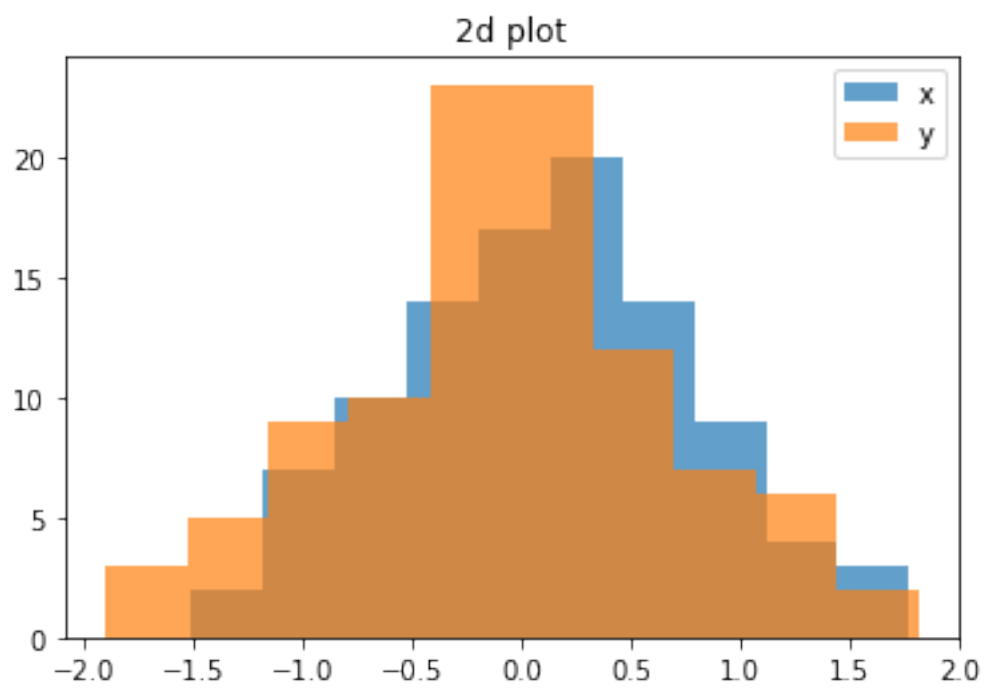
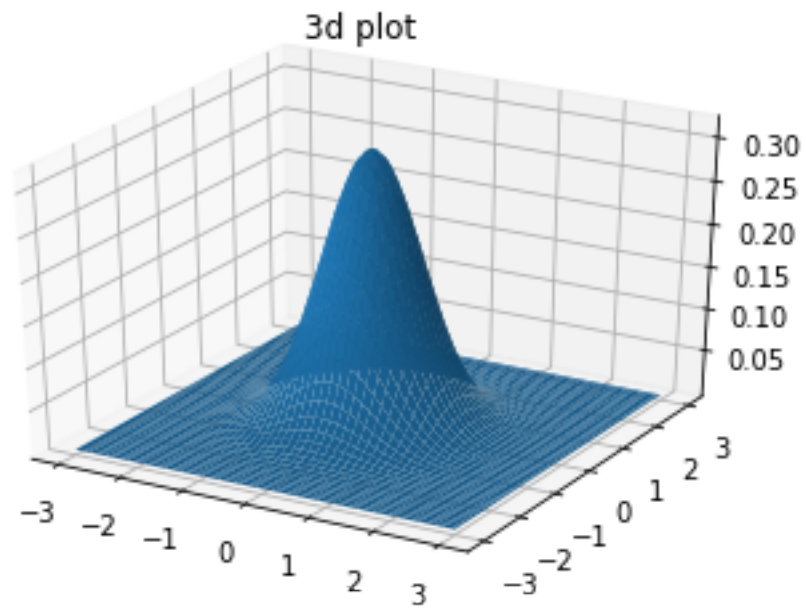
```
In [7]: mu = np.array([0,0])
        cov = np.array([[0.5, 0],[0, 0.5]])

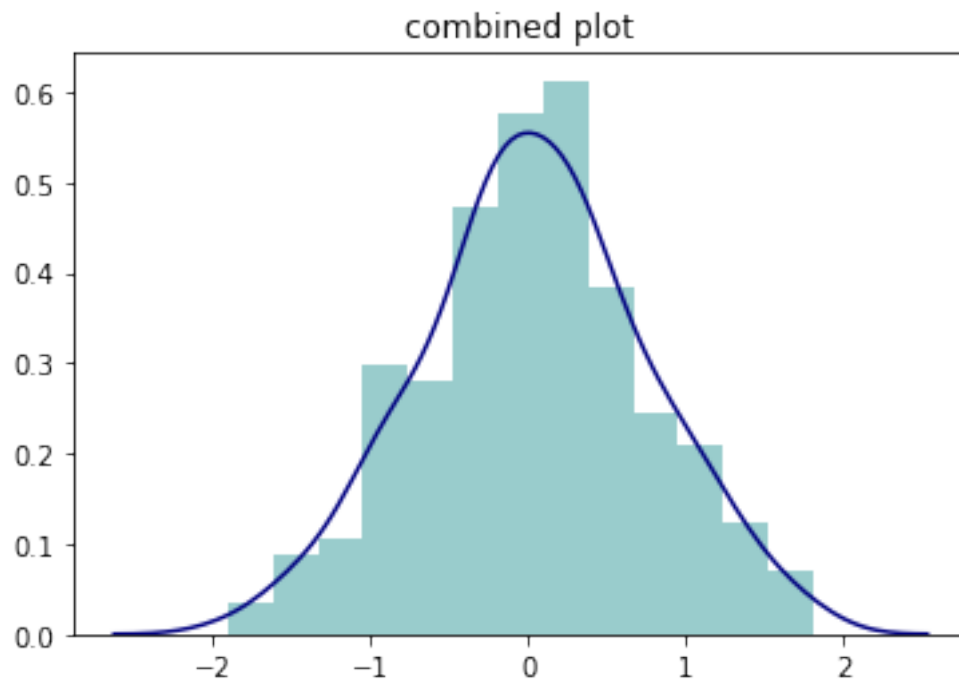
In [14]: # 1. Visualise a Gaussian with the given parameters.
         #3d plot
         x = np.linspace(-3, 3, 100)
         y = np.linspace(-3, 3, 100)
         X, Y = np.meshgrid(x, y)
         pos = np.dstack((X, Y))
         rv = multivariate_normal(mu, cov)
         Z = rv.pdf(pos)
         fig = plt.figure()
         ax = fig.add_subplot(111, projection='3d')
         ax.plot_surface(X, Y, Z)
         plt.title('3d plot')
         fig.show()

         #2d plot
         x, y = np.random.multivariate_normal(mu, cov, 100).T
         plt.figure()
         plt.hist(x, alpha=0.7, bins=10, label='x')
         plt.hist(y, alpha=0.7, bins=10, label='y')
         plt.title('2d plot')
         plt.legend()

         #Combine plot
         combined = np.concatenate((x,y))
         plt.figure()
         plt.title('combined plot')
         sns.distplot(combined, hist_kws={'color': 'Teal'}, kde_kws={'color' : 'Navy'})

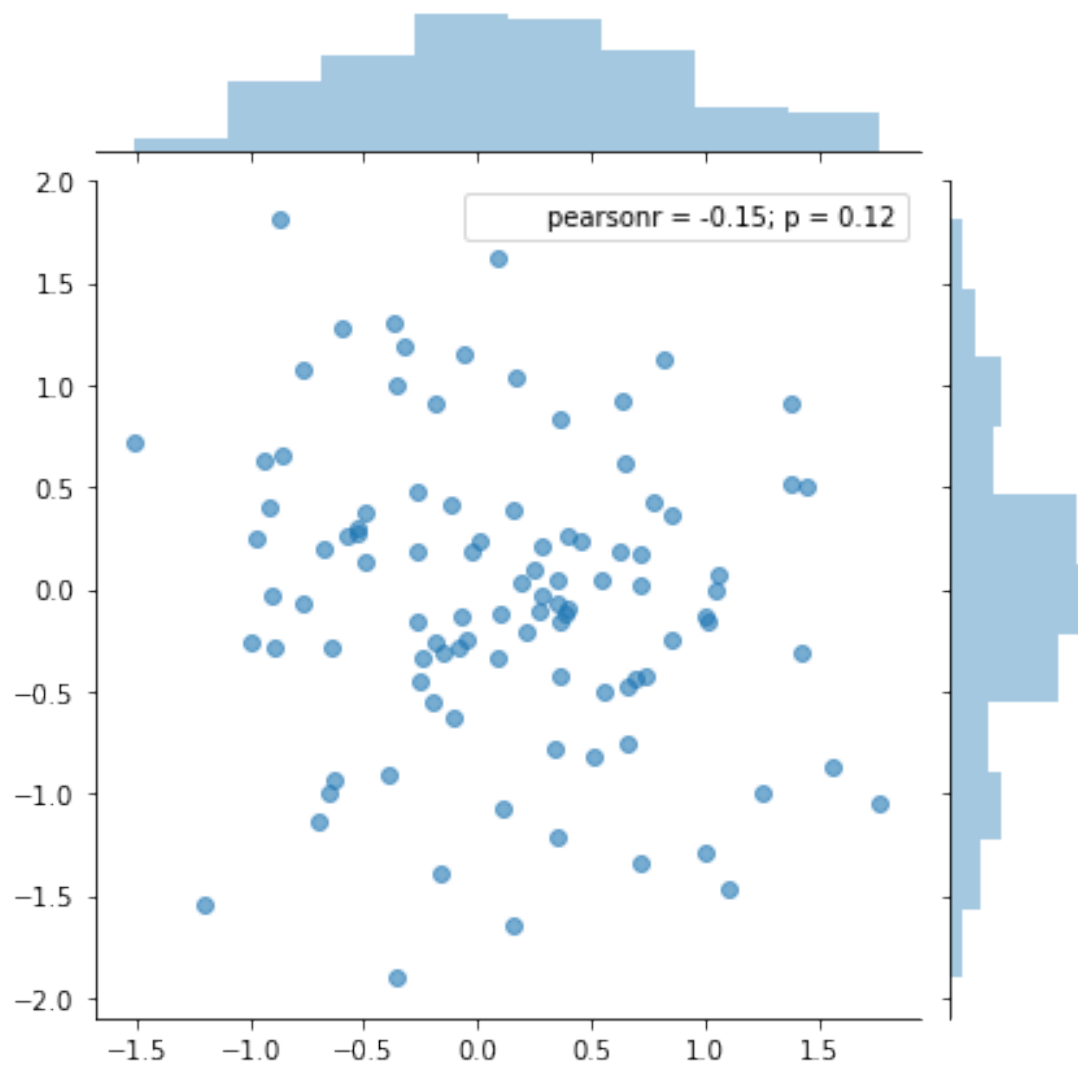
Out[14]: <matplotlib.axes._subplots.AxesSubplot at 0x7f52e4712490>
```





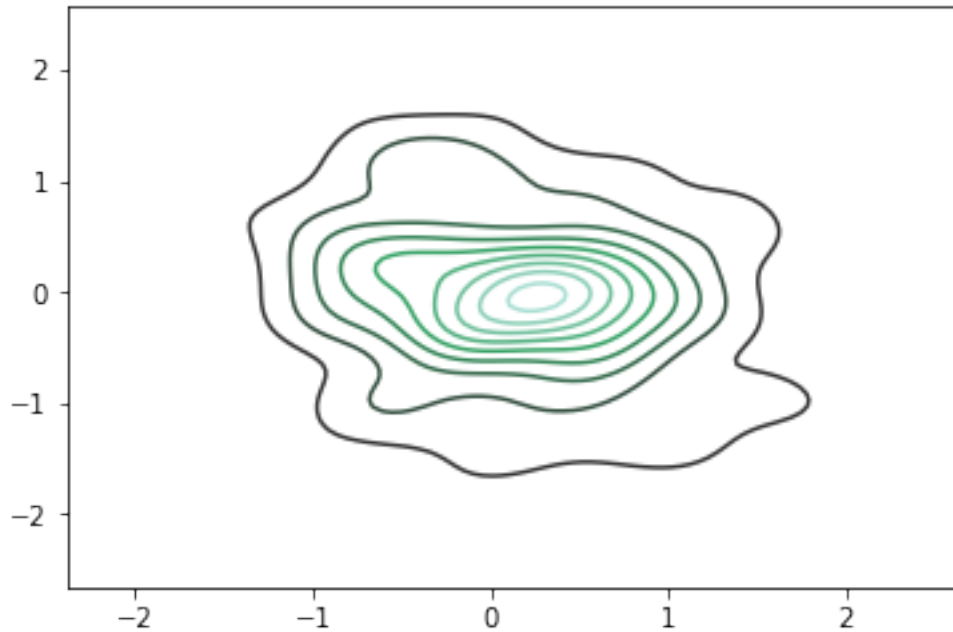
```
In [15]: #2. Visualise a marginal Gaussian.  
sns.jointplot(x,y, alpha=0.6)
```

```
Out[15]: <seaborn.axisgrid.JointGrid at 0x7f52e4233550>
```



```
In [16]: #3. Visualise a slice of Gaussian.  
sns.kdeplot(x, y)
```

```
Out[16]: <matplotlib.axes._subplots.AxesSubplot at 0x7f52e446e990>
```



## 5 Task4:

Given: Number of samples is 1000 from them 330 samples are labeled as class A and 670 samples are labeled as class B. There are 2 features X1 and X2. It is observed that  $p(A, X1)=248$ ,  $p(A, X2)=82$ ,  $p(B, X1)=168$ ,  $p(B, X2)=502$  Compute: Prior  $p(A)$ ,  $p(B)$  Likelihood  $p(X1|A)$ ,  $p(X1|B)$  Posterior  $p(A|X1)$

```
In [10]: p_A = 330.0/1000.0
         p_B = 670.0/1000.0
         print "Prior"
         print "probability of A: " + str(p_A)
         print "probability of B: " + str(p_B)
```

```
Prior
probability of A: 0.33
probability of B: 0.67
```

```
In [19]: p_A_X1 = 248
         p_B_X1 = 168
         p_X1_A = p_A_X1 / p_A
         p_X1_B = p_B_X1 / p_B
         print "Likelihood"
         print "p(X1|A): " + str(p_X1_A)
         print "p(X2|A): " + str(p_X1_B)
```

Likelihood

$p(X1|A)$ : 751.515151515

$p(X2|A)$ : 250.746268657

```
In [22]: posterior_p_A_X1 = (p_X1_A*p_A) / ((p_X1_A*p_A) + (p_X1_B*p_B))
          print "Posterior"
          print "p(A|X1): " + str(posterior_p_A_X1)
```

Posterior

$p(A|X1)$ : 0.596153846154