Department of Electronic and Telecommunication Engineering University of Moratuwa, Sri Lanka

EN2550 - Fundamentals of Image Processing and Machine Vision



ASSIGMENT 4

Submitted By

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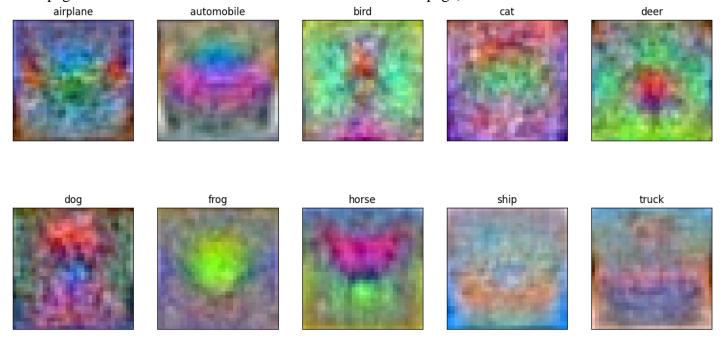
 $Full\ code:\ \underline{https://github.com/Ravindu-Yasas-Nagasinghe/EN2550-Computer-Vision-and-Image-Processing-Assignments}$

1)Linear Classification using gradient descent.

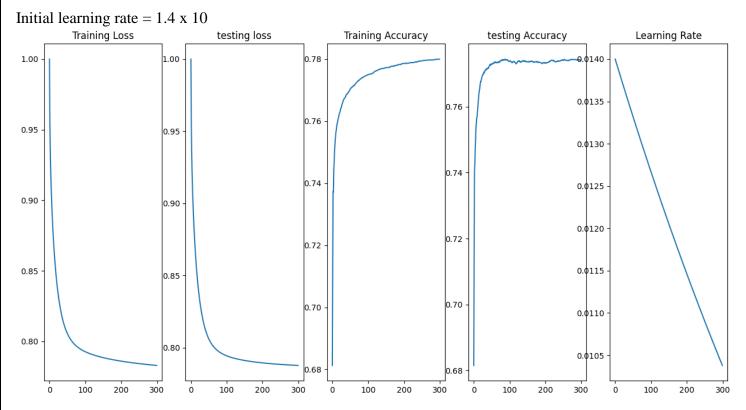
Here our data set is CIFAR-10. There are 10 different classes in this data set. I use tensorflow to import the data set to python. Our score function for the linear classifier is f(x) = W x + b, and the loss function is the mean sum of squared errors function. I run for 300 epochs as instructed in the assignment. The code for 1 layer linear classifier using gradient descent is as follows.

```
def preprocessing(normalize,reshape):
    Ntr = x_train.shape[0] # Number of training data=50,000
Nte = x_test.shape[0] # Number of testing data=10,000
Din = 3072 # CIFAR10 = 3072 = 32x32x3
    if normalize:
     mean image = np.mean(x train, axis=0)
     x_train = x_train - mean_image
    x_test = x_test - mean_image
y_train = tf.keras.utils.to_categorical(y_train, num_classes=K)
     y_test = tf.keras.utils.to_categorical(y_test, num_classes=K)
        x_train = np.reshape(x_train,(Ntr,Din))
x_test = np.reshape(x_test,(Nte,Din))
     x_train = x_train.astype('float32')
    x_test = x_test.astype('float32')
return x_train,y_train,x_test,y_test,K,Din,Ntr,Nte
    loss_history = []
loss_history_testing = []
    train_acc_history = []
val_acc_history = []
    rng = np.random.default_rng(seed=seed)
    std=1e-5#standard deviation to generate random values for w1 and b1
         = std*np.random.randn(Din, K)#weight matrix
    b1 = np.zeros(K)#k dimensional bias matrix
    for t in range(iterations):
         indices = np.arange(Ntr)
         rng.shuffle(indices)
         y=y train[indices]
         y_pred=x.dot(w1)+b1
         y pred test=x test.dot(w1)+b1
         val=y_pred_test.shape[0]
         train_loss=(1/batch_size)*(np.square(y_pred-y)).sum()+reg*(np.sum(w1*w1))
         loss history.append(train_loss)
test_loss=(1/val)*(np.square(y_pred_test-y_test)).sum()+reg*(np.sum(w1*w1))
         loss_history_testing.append(test_loss)
          train_accuracy=1-(1/(10*batch_size))*(np.abs(np.argmax(y,axis=1)-np.argmax(y_pred,axis=1))).sum()
          train_acc_history.append(train_accuracy)
          test\_accuracy=1-(1/(10*Nte))*(np.abs(np.argmax(y\_test\_axis=1)-np.argmax(y\_pred\_test\_axis=1))).sum()
          val acc history.append(test accuracy)
              print('epoch %d/%d: train loss= %f || ,test loss= %f || ,train accuracy= %f || , test accuracy= %f || , learning rate= %f ||'
% (t,iterations,train loss,test loss,train accuracy,test accuracy,lr))
          dy_pred=(1./batch_size)*2.0*(y_pred-y)#partial deravative of L w.r.t y_pred
          dw1=x.T.dot(dy_pred)+reg*w1
db1=dy_pred.sum(axis=0)
          w1-=lr*dw1#update weight matrix
b1-=lr*db1#update bias matrix
reg = 5e-6 #lambda=regularization parameter
x_train,y_train,x_test,y_test,K,Din,Ntr,Nte=preprocessing(normalize=True,reshape=True)
w1,b1,loss_history,loss_history_test,train_acc_history,val_acc_history,lr_array=layer1LinearClassifier(x_train,y_train,x_test,y_test,K,Din,lr,lr_decay,reg,Mtr,Nte)
```

After that I plot the weight matrix W, as 10 images and plot the training loss, testing loss, training accuracy, testing accuracy and learning rate. W1 weight array is of the shape 3072 x 10. (Code for plotting is not included due to page constraints. Full code is available at the link on cover page).



Weight matrix as 10 images



Loss, testing loss, training accuracy, testing accuracy, learning rate of the linear classifier for 300 epochs.

After 300 epochs loss= 0.783117, test loss= 0.787730, train accuracy= 0.779958, test accuracy= 0.774120, learning rate= 0.010474.

2) 2 layer fully connected network

Here I use a two-layer dense network with H=200 hidden nodes. Code for this part is as follows.

```
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Here gradients are computed in the direction from output to input layers and combined using chain rule.

• Input layer to hidden layer

$$h(W_1, b_1) = \frac{1}{1 + \exp(-W_1 x - b_1)}$$

Hidden layer to the output layer

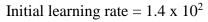
$$y_pred(W_2, b_2) = W_2h + b_2$$

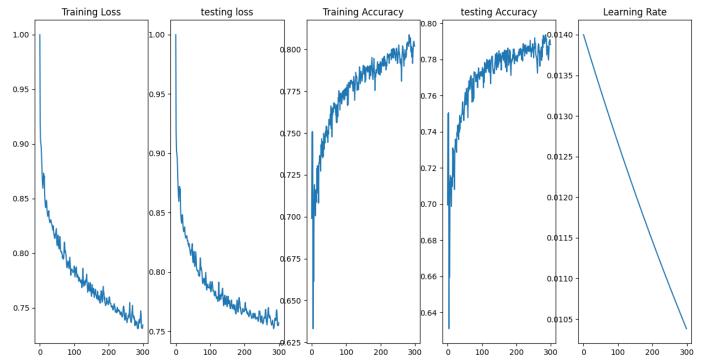
• Total number of learnable parameters in the network = $(200 \times 3072 + 200) + (10 \times 200 + 10) = 616,610$

We preprocess the input data set without pixel normalization to avoid underfitting.

As we can see from the below results when the number of iterations increase the loss decreases and accuracy increases. But the rate of the loss decreasing and accuracy increasing reduces with the iterations.

As we can see from the results, when we use 2 layer fully connected network instead of single layer as in part 1, we can reduce the train and test loss and increase training and testing accuracy. So, if we increase the number of layers further, we can achieve more and more accuracy and reduce loss.





Loss, testing loss, training accuracy, testing accuracy, learning rate of the 2 layer fully connected network for 300 epochs.

After 300 epochs, loss= 0.735866, test loss= 0.759436, train accuracy= 0.795186, test accuracy= 0.784170 and learning rate= 0.01047|.

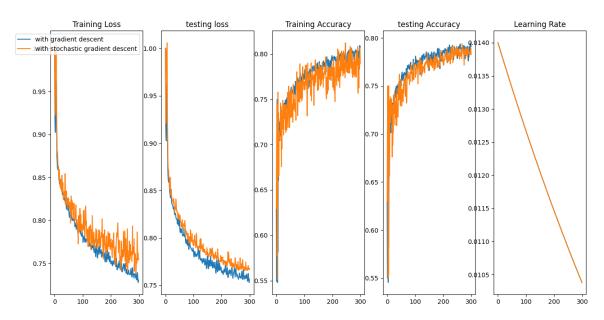
3) Stochastic gradient descent with a batch size of 500.

Here instead of using 50,000 samples I only uses 500 samples which are selected randomly. The code for this part is as follows. (only the parts different from the code in part 2 is included. The full code is available in the link at cover page).

```
#part 3
# Function for two layer dense network with stochastic gradient descent
def mini_batching(x_train,y_train,x_test,y_test,Din,lr,lr_decay,H,reg,K,Mtr,Mte):
    loss_history = []
    loss_history = []
    val_acc_history = []
    lr_array = []
    seed = 0
    rng = np.random.default_rng(seed=seed)
    batch_size=500 mmake batch size =500 for stochastic gradient descent
```

```
batch_size = 500
#=200/iniden layer nodes
iterations = 500/gradient descent iterations
Ir = 1.4e-2
Ir_decay = 0.609
reg = 50 followide-regularization parameter
X_train_layer_y_train_layer_x_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer_y_test_layer
```

Here we compute the gradients off the loss function w.r.t to the functions constructed only using 500 samples. It is advantageous to use stochastic gradient descent instead of gradient descent because we can avoid being stuck at a local minimum instead of global minimum when finding loss. By using SGD we can compute errors and updates weights much faster as batch size is low. SGD often converges much faster compared to GD. One disadvantage of SGD is that loss function can be much noisier than GD.



Loss, testing loss, training accuracy, testing accuracy, learning rate of the 2 layer fully connected network using gradient descent and stochastic gradient descent for 300 iterations.

After 300 iterations for stochastic gradient descent with batch size =500, loss =0.737830, test loss =0.765587, train accuracy =0.808400, test accuracy =0.783190 and learning rate =0.010474.

By comparing the plots from part2(GD) and SGD, we can state that accuracy has been slightly increased when using SGD instead of GD. By observing the loss plots we can state that SGD has reached the convergence much faster than GD, but SGD is much noisier and has higher loss than GD.

4) CNN

Here I preprocess data without normalization of pixels and without reshaping the images. As seen from the results, we can clearly state that CNN is overfitting. Here I used sgd optimizer with momentum. The code is as follows.

from tensorflow.keras import layers,models,optimizers
x_train_CNN,y_train_CNN,x_test_CNN,y_test_CNN,K,Din,Ntr,Nte=preprocessing(normalize=True,reshape=False)
model = models.Sequential()
elayers
model.add(layers.Conv2D(32,(3,3),activation='relu',input_shape=(32,32,3)))
model.add(layers.Conv2D(64,(3,3),activation='relu'))
model.add(layers.NaxPool2D((2,2)))
model.add(layers.NaxPool2D((2,2)))
model.add(layers.NaxPool2D((2,2)))
model.add(layers.NaxPool2D((2,2)))
model.add(layers.Platten())
model.add(layers.Platten())
model.add(layers.Dense(da))
sgd = keras.optimizers.SGD(lr=1.de-2, momentum=0.9, decay=1e-6)#lr =learning rate, decay =learning rate decay
model.compile(optimizersgd,loss=tf.keras.losses.CategoricalCrossentropy(from_logits=True),metrics=["accuracy"])
print(model.summary())
history=model.fit(x_train_CNN,y_train_CNN,epochs=50,batch_size=50,validation_data=(x_test_CNN,y_test_CNN))
print(model.optimizer.get_config())
plt.plot(history.history['loss'],label='training loss')#plotting the graphs
plt.xlabel('epoch')
plt.legend(loc='lower right')
plt.show()

(In plotting code part, only code for plotting loss is included)

Here I used,

learning rate = 0.014

momentum = 0.9.

learning rate decay =1e-6

There are 73,418 total learnable parameters in this network.

After 50 epochs loss: 0.2491, accuracy: 0.9164, testing loss: 1.7655, testing accuracy: 0.6914

