

$$1. (9, 11, 14, 15, 16, 20, 22, 23, 31, 32, 34, 35, 40, 45, 46, 55)$$

→ Ideal Gas Law : $PV = nRT$

$$\text{1.11 } \forall \text{ if } n=1 \text{ of air, } T=300K \rightarrow P = 1atm = 1.013 \times 10^5 Pa$$

$$\Rightarrow PV = nRT \Rightarrow V = \frac{nRT}{P} = \frac{(1mol)(0.31J/mol \cdot K)(300K)}{1.013 \times 10^5 Pa \cdot m^2} = 0.0246 m^3$$

(Using 16L)

$$1.11 V_b = V_a, T_a > T_b, P_a = P_b \approx 1atm \quad (\text{Using 16L})$$

$$\rightarrow PV = nRT = nNa_kT = \frac{N}{A} N_a kT = Constant.$$

$$\therefore \frac{N_a}{A} N_a kT_a = \frac{N_b}{A} N_b kT_b \Rightarrow N_a T_a = N_b T_b \Rightarrow \frac{N_b}{N_a} = \frac{T_b}{T_a}, \therefore T_a > T_b, N_b > N_a$$

$$1.11 M_2(0.78), O_2(0.21), Ar(0.01), M \text{ of 1 mol?} \text{ Where } M = M_n \quad (\text{remembered from chemistry})$$

$$\rightarrow M_{dm} = M_{Ar}(0.78) + M_{O_2}(0.21) + M_{Ar}(0.01) = 28.034(0.78) + 31.968(0.21) + 32.969(0.01) = 28.9695 \text{ g/mol}$$

$$\therefore M_{dm} = M_{dm} n = 28.9695 \text{ g/mol} \cdot 1 \text{ mol} = 28.9695 \text{ g}$$

$$1.15 \bar{T}?, \text{ If } M_T = 500 \text{ kg, } M_a? \text{ Assuming } P = 1atm \rightarrow V = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi(8 \text{ m})^3 = 2144.66 \text{ m}^3 \quad (\bar{T} \text{ of a sphere})$$

$$\text{a) } P = \frac{F}{A}, V = \frac{nRT}{P}, \frac{M}{P} = \frac{N_A}{RT} = \frac{M}{RT}$$

$$\text{To keep pressure const, there needs to be a buoyant force equal to the weight}$$

$$\therefore \Delta F = -\frac{\rho_{air} A}{\bar{V}} \Rightarrow P_{ext} - P_{air} = \frac{\rho_{air}}{\bar{V}} \Rightarrow \frac{P_{ext}}{T_b} - \frac{P_{air}}{T_b} = \frac{\rho_{air}}{T_b} \Rightarrow \frac{1}{T_b} = \frac{1}{T_0} - \frac{P_{air}}{\rho_{air} \bar{V}}, \text{ assuming air Temp (}T_0\text{) is } \sim 23^\circ\text{C} = 296 \text{ K}$$

$$\Rightarrow \frac{1}{T_b} = \frac{1}{296K} - \frac{(500kg)}{(0.085kg)(1.013 \times 10^5 Pa)(2144.66 \text{ m}^3)} = \frac{1}{296K} - \frac{1}{151.12K} \therefore T \approx 368 \text{ K}$$

$$\text{b) } PV = nRT, n = \frac{M}{M_u} = \frac{M}{RT} \therefore M = \frac{PV_u}{RT} = \frac{(1.013 \times 10^5 Pa)(2144.66 \text{ m}^3)}{(0.085 kg)(368 K)} = 2053.13 \text{ kg} \quad (\text{Using 16L})$$

→ Which is about 4 times the mass of payload + unfilled balloon, if the assumptions are right.

$$1.16 \quad \begin{array}{c} F_x = \dot{m} P(z) \\ \downarrow \\ \frac{d}{dz} \dot{m} = \dot{m}_0 e^{-\frac{P(z)}{P_0}} \\ \downarrow \\ \dot{m} = \dot{m}_0 e^{-\frac{P(z)}{P_0}} \end{array}$$

$$\text{a) } F_z = -A \cdot P(z) - A \cdot P_0 = -\dot{m}_0 \Rightarrow P(z) - P_0 = -\frac{\dot{m}}{A} z = -\dot{m} dz \cdot z \quad (\text{From Newton's 2nd law})$$

$$\therefore \frac{dP}{dz} = -\frac{\dot{m}}{A} \Rightarrow -\frac{dP}{dz} = \dot{m} \frac{dp}{dz}$$

$$\text{b) Using } PV = nRT = MRT \quad (\text{Using 16L})$$

$$\rightarrow \frac{dP}{dz} = -\frac{\dot{m}}{M} \Rightarrow \frac{dP}{dz} = -\frac{\dot{m}_0}{M} e^{-\frac{P(z)}{P_0}}$$

$$\text{c) Isothermal from b):}$$

$$\rightarrow \frac{dP}{dz} dz = -\frac{\dot{m}_0}{M} P_0 dz \Rightarrow \int_P^0 \frac{1}{P} dP = -\frac{\dot{m}_0}{M} \int_0^z dz \Rightarrow ln(\frac{P}{P_0}) = -\frac{\dot{m}_0 z}{M} \Rightarrow e^{\frac{\dot{m}_0 z}{M}} = \frac{P}{P_0}$$

$$\therefore P(z) = P_0 e^{\frac{-\dot{m}_0 z}{M}}, \text{ where } P_0 \text{ is at } z=0$$

$$\text{d) } z_1 = 1420 \text{ m}, z_2 = 3070 \text{ m}, z_3 = 4420 \text{ m}, z_4 = 8840 \text{ m}, P_0 = 1atm \rightarrow \bar{T} \approx 210 \text{ K for all regions}, \frac{\dot{m}_2}{\dot{m}_1} \approx \frac{z_2}{z_1}, M = 0.0289 \text{ kg} \cdot R = 8.31 \frac{J}{K}, \therefore P_2(z) = \frac{0.0289 \text{ kg} \cdot z_2}{8.31 \frac{J}{K} \cdot z_1} = 0.4548 \text{ atm}, P_3(z) = 0.5948 \text{ atm}, P_4(z) = 0.3538 \text{ atm} \quad (\text{Higher you go, pressure decreases})$$

$$(e.g. 1.16) \quad (\text{from chemistry})$$

$$1.17 T=300K, V_{rms} = (\frac{kT}{m})^{1/2}, K = \frac{R}{Na} = \frac{1}{Na} \cdot M = \frac{1}{Na} \cdot \frac{M}{M_u} = \frac{1}{Na} \cdot \frac{M_u}{M_u \cdot M_A} = \frac{1}{Na} \cdot \frac{M_u}{M_u \cdot M_A} = \frac{(3RT)^{1/2}}{(NA)^{1/2}}$$

$$\cdot \text{ For } 238: M = M_p + M_u = 14.6 + 238 = 352.6, V_{rms} = \frac{(3(8.31 \frac{J}{K})(300K))^{1/2}}{352.6} = 145.76 \frac{m}{s}$$

$$\cdot \text{ For } 235: M = 19.6 + 235 = 354.6, V_{rms} = \frac{(3(8.31 \frac{J}{K})(300K))^{1/2}}{354.6} = 146.39 \frac{m}{s}$$

... for $M_{u,235} > M_{u,238}, (V_{rms})_{235} > (V_{rms})_{238}$ by a factor of 1.0045

1.18 Effusion: gas leaking out of a small hole

$$\text{a) Show: } N = \frac{PV}{kT} \quad (\text{Using 16L})$$

$$\rightarrow PV = NRT = NmV^2 = PAV \Rightarrow PA = Nm \frac{V^2}{A}, \Delta t = \frac{2L}{Vx}, \therefore N = \frac{PA \Delta t}{kT Vx} = \frac{PA \Delta t}{2kT}$$

$$\text{b) } \rightarrow PV = NKT = NmV^2 \therefore N = \frac{K}{m} = \frac{RT}{Vx}$$

$$\text{c) From a + b) } \rightarrow N = \frac{\Delta N}{\Delta T} = \frac{\frac{PA}{2kT} \Delta t}{\Delta T}, P = \frac{N}{\frac{RT}{Vx}} \Rightarrow \frac{\Delta N}{\Delta T} = -\frac{N}{Vx} \frac{R}{T^2}, \therefore \frac{\Delta N}{\Delta T} = -\frac{RT}{Vx} \frac{R}{T^2} = \frac{R^2}{Vx^2} \frac{1}{T}$$

$$\therefore \frac{dN}{dt} = \frac{d}{dt} \left(\frac{N_0}{Vx^2} e^{-\frac{RT}{Vx}} \right) \Rightarrow \frac{dN}{dt} = \frac{N_0}{Vx^2} \frac{R}{Vx} \frac{1}{T^2} dt, \text{ For Isothermal, } \Rightarrow ln(\frac{N}{N_0}) = \frac{-\frac{R}{Vx} (t-T_0)}{T_0^2} = \frac{-\frac{R}{Vx} t}{T_0^2} \Rightarrow \frac{N(t)}{N_0} = e^{-\frac{Rt}{Vx T_0^2}}$$

d) ??

$$T = 1L = 10^3 \text{ m}^3, A = 10^{-4} \text{ m}^2, \bar{T} = 300K \text{ (assuming room temp)}, \text{ assume } M = 1.013 \text{ atm}$$

$$\rightarrow \frac{1}{T} = \frac{A}{2kT} = \frac{10^{-4} \text{ m}^2}{2 \cdot 8.31 \frac{J}{K} \cdot 300K} = 0.1468 \text{ s}^{-1} \therefore \bar{t} = 6.81 \text{ s}$$

c) flow W/m in an hour (3600s), size of hole?

Stretching the tube's tube, we can assume it's a cylinder, ∴ $\bar{t} = \pi r^2 l$, assuming $r = 0.1 \text{ m}, l = 0.1 \text{ m}^3$

$$\rightarrow \bar{t} = \frac{2\pi r^2 l}{\frac{A}{2kT}} = \frac{2\pi (0.1 \text{ m})^2 (0.1 \text{ m}^3)}{0.1468 \text{ s}^{-1} (3600s)} = 1.902 \times 10^2 \text{ m}$$

f) Most def. NOT! There is no pressure in the Vacuum of space, so if you open a hatch from a ship in space, the ship being pressurized, you will be blown out into space bc the pressure from inside the ship is forcing it open. Which is why the door would open towards the outside, not inside, so it's easier to open.

Hence the name Vacuum of Space bc it acts as a vacuum does, sucking everything out

Assuming \bar{t} of spacecraft is 30 m^3 , area of the hatch is 2 m^2 , & breathable air inside:

$$\rightarrow \bar{t} = \frac{2\pi r^2 l}{\frac{A}{2kT}} = 30 \left(\frac{0.0289 \text{ kg}}{8.31 \frac{J}{K}} \right)^{1/2} = 0.1025 \text{ m} \quad \therefore \text{No human can act this fast to throw a dog across into space}$$

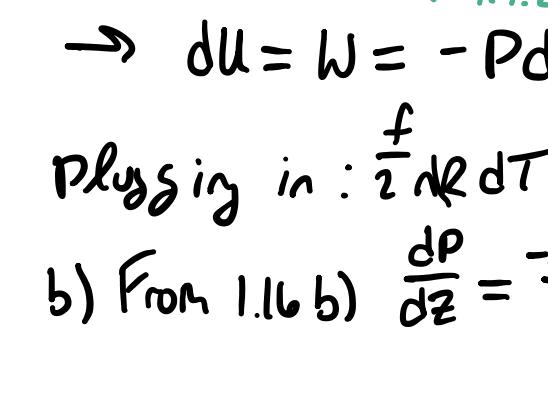
$$1.19 T=300K, P=1atm = 1.013 \times 10^5 Pa \quad (\text{e.g. 1.23})$$

$$\text{a) } 1L = 0.01 \text{ m}^3 \text{ of He} \rightarrow U_{Th} = Nf \frac{1}{2} kT = Nf \frac{1}{2} RT \Rightarrow PAV = Nf \frac{1}{2} RT, \text{ He is monoatomic} \therefore f=3, = \frac{3}{2}(1.013 \times 10^5 Pa)(0.01 \text{ m}^3) = 151.95 \text{ J}$$

$$\text{b) } .001 \text{ m}^3 \text{ of air (which is a diatomic gas bc it's mostly N}_2 \text{ & O}_2 \text{)} \rightarrow U_{Th} = \frac{5}{2} Pk = \frac{5}{2}(1.013 \times 10^5 Pa)(.001 \text{ m}^3) = 253.25 \text{ J}$$

$$1.20 V_b = 1L, P_0 = 1atm, V_f = 3L \rightarrow P_f = 3atm$$

a) P-V Diagram:



$$\text{b) } W = -\Delta P \Delta V = -1atm \cdot 2L = -1000 \text{ mPa} \cdot (99.9 - 1)L = 1.013 \times 10^5 Pa \cdot .001 \text{ m}^3 = 101.3 \text{ J}$$

$$W = -\bar{P} \Delta V, \text{ instead of } \Delta P \text{ we assume avg } P(\bar{P}) \text{ which is } \frac{P_0 + P_f}{2} = 1.5atm$$

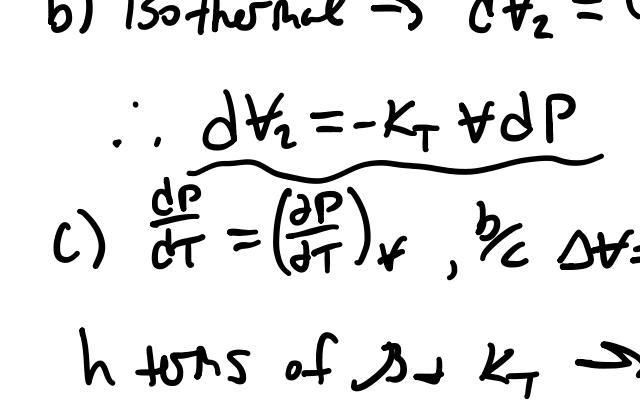
$$(e.g. 1.28) \quad \rightarrow W = -\frac{1}{2} \bar{P} \Delta V = -\frac{1}{2} \cdot 1.5atm \cdot 2L = -150 \text{ J}$$

$$Q = \Delta H - W \Rightarrow Q = U_f - U_i - W = 300K \cdot 3L - 150 \text{ J} = 750 \text{ J}$$

c) To allow the P to rise w/ \bar{t} , you need an increase in T, meaning holding the piston in a furnace or heating it up somehow.

$$1.21 \bar{P} = 200 \text{ atm, Assuming } P_0 = 1atm, \bar{t} = 1L, V_f = .99V_0 = .99L$$

P-V Diagram:



$$W = -\bar{P} \Delta V, \text{ instead of } \Delta P \text{ we assume avg } P(\bar{P}) \text{ which is } \frac{P_0 + P_f}{2} = 1.013 \times 10^5 Pa + 200 \times 10^5 Pa = 101.3 \text{ J}$$

$$W = -\frac{1}{2} \bar{P} \Delta V = -\frac{1}{2} \cdot 101.3 \text{ J} = -50.65 \text{ J}$$

$$(e.g. 1.28) \quad \rightarrow Q = U_f - U_i + W = 200K \cdot .99L - (-50.65 \text{ J}) = 195.94 \text{ J}$$

$$\text{Q = } U_f - U_i \text{ since } U_i = U_f \text{ bc } T_i = T_f \text{ (constant pressure expansion)}$$

$$(e.g. 1.28) \quad \rightarrow U_f = U_i + Q = 1.013 \times 10^5 Pa \cdot .001 \text{ m}^3 + 195.94 \text{ J} = 200.94 \text{ J}$$

$$\text{1.22 } U \text{ Using } F_g \text{ 1.10b, diatomic gas } f=5 \text{, quasi-static}$$

$$(e.g. 1.28) \quad (e.g. 1.23) \quad (e.g. 1.24) \quad \rightarrow 1st law of Therm$$

$$\text{a) } A: W = 0 \text{ bc } \Delta V = 0, \Delta U = \frac{1}{2} (P_2 - P_1) V, \therefore Q = \Delta U - W = \frac{1}{2} (P_2 - P_1) V$$

$$\text{b) } W = -P_1 \Delta V, \Delta U = \frac{1}{2} P_1 \Delta V, \therefore Q = \Delta U - W = \frac{1}{2} (P_1 - P_2) V_2$$

$$\text{c) } W = 0 \text{ bc } \Delta V = 0, \Delta U = \frac{1}{2} (P_2 - P_1) V_2, \therefore Q = \Delta U - W = \frac{1}{2} (P_2 - P_1) V_2$$

$$\text{d) } W = -P_2 \Delta V, \Delta U = \frac{1}{2} P_2 \Delta V, \therefore Q = \Delta U - W = \frac{1}{2} (P_2 - P_1) V_1$$

$$\text{e) } A: \text{ bc no } \Delta V, \text{ heat is being applied increasing w/ } P \text{ but not } \bar{t}$$

B: $\Delta \bar{t}$ is positive, so expansion is happening but not at a rate for heat to still be applied w/ P being constant

C: $\Delta \bar{t}$ is negative bc decrease in P, meaning heat is being taken out, meaning T is decreasing

D: $\Delta \bar{t}$ is negative meaning compression is happening, but not at a rate for T to be increasing w/ constant P

C) \sum