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Probability

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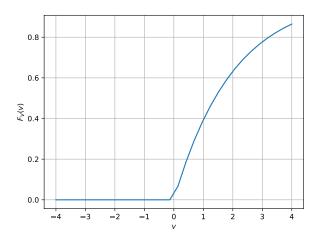


Fig. 1.1. The CDF of X

1 From Uniform to Other

1.1 Generate samples of

$$V = -2\ln(1 - U) \tag{1.0.1}$$

and plot its CDF. **Solution:** The python code is at

The CDF is plotted in Figure given below

1.2 Find a theoretical expression for $F_V(x)$.

Solution: We know that from uniform random variable pdf:

$$f(x) = \begin{cases} 0 & x \le 0 \\ x & 0 \le x \le 1 \\ 1 & x > 1 \end{cases}$$
 (1.0.2)

Therefore,

$$0 \le U \le 1$$
= 1 - 0 \ge 1 - U \ge 1 - 1
= 1 \ge 1 - U \ge 0
= 0 \le 1 - U \le 1
= -\infty \le \ln(1 - U) \le 0
= -\infty \le \le 2 \ln(1 - U) \le 0
= \infty \ge -2 \ln(1 - U) \ge 0
= 0 \ge 2 \ln(1 - U) \ge \infty

For $u \in U, v \in V$

$$V = -2\ln(1 - U)$$

$$= \frac{-V}{2} = \ln(1 - U)$$

$$= e^{(\frac{-V}{2})} = 1 - U$$

$$= U = 1 - e^{(\frac{-V}{2})}$$

$$F_V(v) = F_V(1 - e^{(\frac{-v}{2})})$$
 (1.0.3)

$$F_V(x) = \begin{cases} 1 - e^{(\frac{-x}{2})} & x \ge 0\\ 0 & x < 0 \end{cases}$$
 (1.0.4)