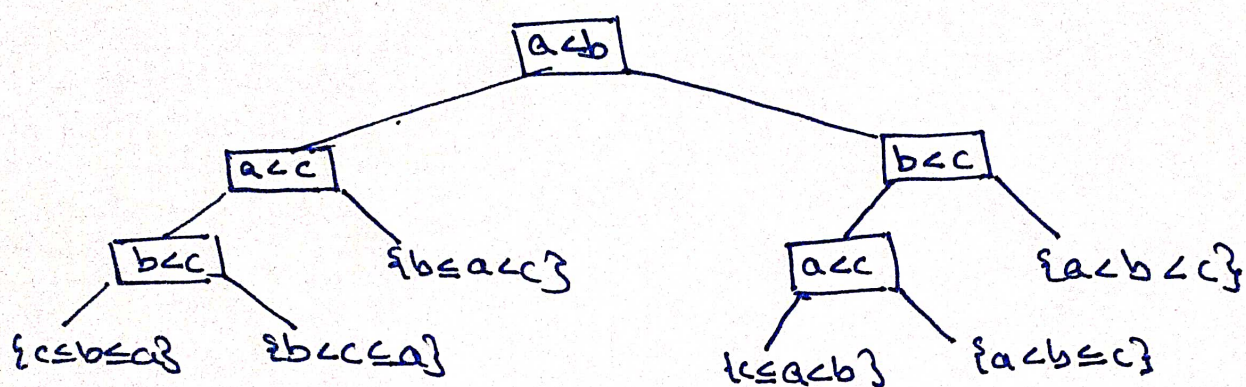


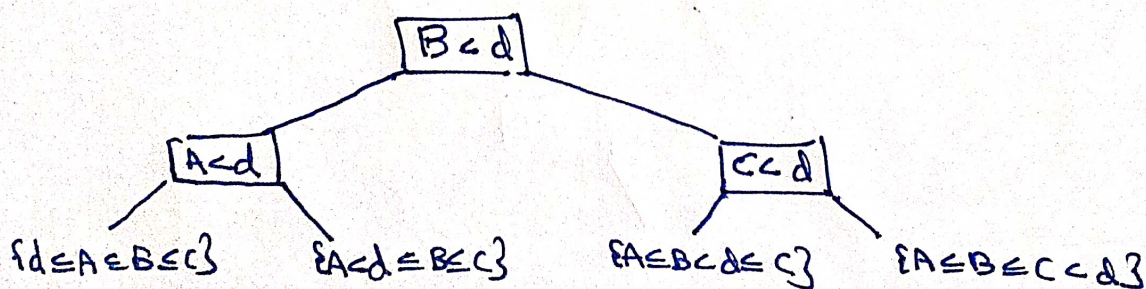
We can find the minimum number comparisons by using a decision tree. Assume that the first two elements we compare are called  $a$  &  $b$ . Then, we need to find the position of another element, which we call  $c$ , with respect to  $a$  &  $b$ . We see from the decision tree that three comparisons are required to guarantee this knowledge.



At the end of the decision tree, we have the sorted list of  $a, b, c$  as  $A \leq B \leq C$ .

Now we have to find the position of  $d$  with respect to  $A, B$  &  $C$ .

If we compare  $d$  to  $A$  or  $C$ , then in the worst case, a total of three comparisons might need to be made. If we compare  $d$  to  $B$  first, then the worst case two comparisons would be made.



$\therefore$  A minimum of 5 comparisons must be made to sort  $a, b, c$  &  $d$ .