

91) Single Source Shortest Paths: Dijkstra's Algorithm

CODE:

```
import heapq
def dijkstra(graph, start):    distances = {vertex: float('infinity') for vertex in graph}
    distances[start] = 0

    priority_queue = [(0, start)]
    while priority_queue:
        current_distance, current_vertex = heapq.heappop(priority_queue)
        if current_distance > distances[current_vertex]:
            continue
        for neighbor, weight in graph[current_vertex].items():
            distance = current_distance + weight
            if distance < distances[neighbor]:
                distances[neighbor] = distance
                heapq.heappush(priority_queue, (distance, neighbor))

    return distances

if __name__ == "__main__":
    graph = {
        'A': {'B': 1, 'C': 4},
        'B': {'A': 1, 'C': 2, 'D': 5},
        'C': {'A': 4, 'B': 2, 'D': 1},
        'D': {'B': 5, 'C': 1}
    }
    start_vertex = 'A'
    shortest_distances = dijkstra(graph, start_vertex)

    print(f"Shortest distances from {start_vertex}:")
    for vertex, distance in shortest_distances.items():
        print(f"To {vertex}: {distance}")
```

OUTPUT:

```
C:\Windows\system32\cmd.e: × + ▾  
Shortest distances from A:  
To A: 0  
To B: 1  
To C: 3  
To D: 4  
Press any key to continue . . . |
```

TIME COMPLEXITY : $O((V+E)\log V)$